



Manipal Institute of Technology, Manipal



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(A Constituent Institute of Manipal University)

IV SEMESTER B.TECH (AERONAUTICAL/AUTOMOBILE ENGINEERING)

END SEMESTER EXAMINATIONS, MAY 2016

SUBJECT: LINEAR CONTROL THEORY [AAE 2204]

REVISED CREDIT SYSTEM

Time: 3 Hours

MAX.MARKS: 50

Instructions to Candidates:

- ✤ Answer ALL the questions.
- Missing data may be suitable assumed.
- **1A.** Write down the governing differential equations of the system shown figure 1 (03) in page 2 and find the transfer function $X_3(s)/X_1(s)$
- **1B.** Using the block diagram reduction technique, find the C/R ratio for the black **(05)** diagram shown in figure 2
- **1C.** A system is described by the following differential equation:

 $\frac{d^3y}{dt^3} + 3\frac{d^2y}{dt^2} + 5\frac{dy}{dt} + y = \frac{d^3x}{dt^3} + 4\frac{d^2x}{dt^2} + 6\frac{dy}{dt} + 8x$. Determine the transfer function Y(s)/X(s).

- 2A. Convert the block diagram in the figure 2 to signal flow graph and find the (04) transfer function.
- **2B.** A unity feedback control system has an open loop transfer function given by, (02) $C(a) = \frac{10}{10}$

 $G(s) = \frac{10}{s(s+2)}$. Find the rise time and percentage overshoot for a step input

of 12 units.

2C. The open loop transfer function of a unity feedback control system is given by **(04)** $G(s) = \frac{100}{s(s+1)(s+2)}$ Find the steady state error when it is subjected to the

input, $r(t) = 1 + 2t + 1.5t^2$.

3A. Sketch the Bode plot for the following open loop transfer function (04)

$$G(s) = \frac{30(1+0.1s)}{s(0.01s+1)(s+1)}$$

- **3B.** Determine the phase margin and gain margin from the plot in 3A. (02)
- **3C.** Sketch the polar plot of the following transfer function (04)

$$G(s) = \frac{1}{s(s+4)(s+8)}$$

4A. Consider a unity feedback system with open loop transfer function, **(05)**

$$G(s) = \frac{K}{s(s+8)}$$

Design a suitable lead compensator so that the system meets the following specifications. I) Percentage overshoot = 9.5%, II) Natural frequency of

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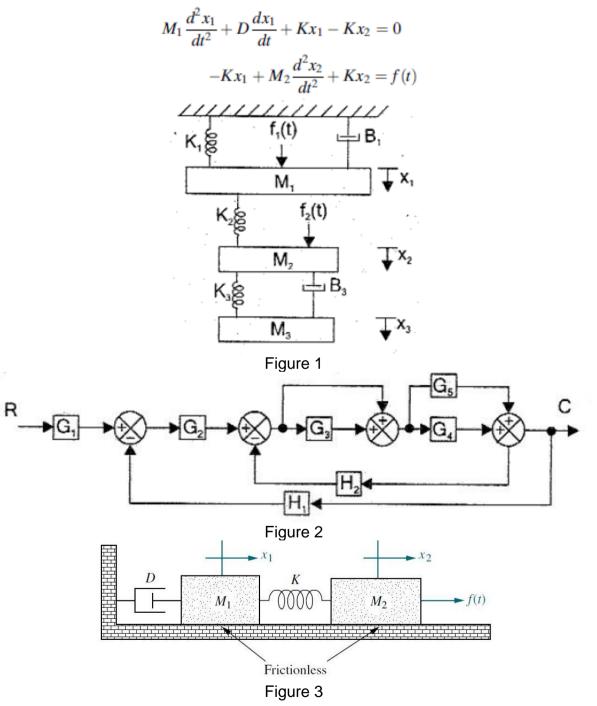
oscillation, ω_n = 12 rad/sec and III) velocity error constant K_v≥10.

4B. The open loop transfer function for a system is given as

$$G(s) = \frac{\kappa}{s(s+2)(s+4)}$$

Find the asymptotes, centroid and breakaway and break in points

- **4C.** What is the difference between controller and compensator? (02)
- **5A.** What are the critical considerations while selecting state variables? (02)
- **5B.** State the advantages of State space model over classic transfer function. **(03)**
- **5C.** Derive the state space representation from the given differential equation for a **(05)** translational mechanical system given below (Figure 3).



(03)