



# Manipal Institute of Technology, Manipal

(A Constituent Institute of Manipal University)



## IV SEMESTER B.TECH (ELECTRICAL & ELECTRONICS ENGINEERING)

MAKEUP EXAMINATIONS, JUNE 2016

SUBJECT: SIGNALS AND SYSTEMS [ELE 2201]

REVISED CREDIT SYSTEM

Time: 3 Hours

30 JUNE 2016

MAX. MARKS: 50

### Instructions to Candidates:

- ❖ Answer **ALL** the questions.
- ❖ Missing data if any may be suitable assumed.
- ❖ Transform Table may be supplied

1A. Given the sequence  $x[n] = \{1, -2, 2, -1, 3, 1\}$ , sketch and label the following

(i)  $x[n]$ ; (ii)  $x[-n]$ ; (iii)  $x[n+1]$  (03)

1B. If the input to an LTI system is  $x[n] = 1$  for  $3 \leq n \leq 6$  and its impulse response is  $h[n] = \alpha^n u[n]$ , determine the response of the system  $y[n] = x[n] * h[n]$  using convolution sum.  $|\alpha| < 1$  (04)

1C. (i) Find whether the following signals is periodic. If periodic find its fundamental period.

$x[n] = 2e^{j\frac{3\pi}{5}\left(n + \frac{1}{2}\right)}$  (ii) Determine whether the continuous-time signal  $x(t) = tu(t)$  is energy or power signal or neither. (03)

2A. Determine whether the system represented by input-output relation is (i) causal (ii) time-invariant. Justify the answer.

(i)  $y[n] = nx[n]$  (ii)  $y[n] = x[n]e^{t}$  (03)

2B. A discrete-time LTI system is described by the following difference equation.

$$y[n] + \frac{3}{4}y[n-1] + \frac{1}{8}y[n-2] = x[n] + x[n-1]$$

Given:  $y[-1] = 1$  and  $y[-2] = -1$  and input  $x[n] = \left(\frac{1}{2}\right)^n u[n]$ .

Using time domain method obtain (i) the Zero-input response (ii) Zero-state response. (07)

- 3A. Using defining equation find the time domain signal  $x(t)$  corresponding to continuous-time Fourier Transform (CTFT) representation given as:

$$X(j\omega) = \begin{cases} \cos\left(\frac{\omega}{2}\right) + j \sin\left(\frac{\omega}{2}\right); & |\omega| \leq \pi \\ 0; & \text{otherwise} \end{cases} \quad (04)$$

- 3B. Find the Exponential Fourier coefficient of the wave form shown in Fig. Q3B. (04)

- 3C. Determine the continuous time Fourier transform of the signal using properties.

$$x(t) = te^{-2t} u(t) \quad (02)$$

- 4A. Obtain the time-domain signal  $x[n]$  corresponding to the DTFT representation

$$X(e^{j\Omega}) = \begin{cases} 1; & \frac{\pi}{2} \leq |\Omega| \leq \pi \\ 0; & \text{otherwise} \end{cases} \quad \text{and } \angle X(e^{j\Omega}) = -4\Omega \quad (04)$$

- 4B. Find discrete-time periodic signal  $x[n]$  if its DTFS coefficient is given by

$$X[k] = \cos\left(\frac{6\pi}{17}k\right) \quad (03)$$

- 4C. If the DTFT of  $x[n] = n\left(\frac{-3}{2}\right)^n u[n]$  is  $X(e^{j\Omega})$ , without evaluating  $X(e^{j\Omega})$  find  $y[n]$  in each of the following.

$$(i) Y(e^{j\Omega}) = e^{-j2\Omega} X(e^{j\Omega}) \quad (ii) \frac{d}{d\Omega} \{j^{2\Omega} X(e^{j\Omega})\} \quad (03)$$

- 5A. Find the DTFT of non-periodic signal  $x[n]$  using properties

$$x[n] = \left(\frac{\sin\left(\frac{\pi(n)}{4}\right)}{\pi n}\right) * \left(\frac{\sin\left(\frac{\pi(n-2)}{4}\right)}{\pi(n-2)}\right). \text{ Also plot magnitude and phase spectra.} \quad (04)$$

- 5B. Find the inverse Z-transform of  $X(z) = \frac{z+2}{z^2+z+1}; |z| > 1$  (03)

- 5C. Determine the Z-transform of the signal  $x[n]$  using properties and also find the region of convergence.

$$x[n] = \left(\frac{1}{2}\right)^n u[n] + \left(\frac{1}{3}\right)^n u[-n] \quad (03)$$

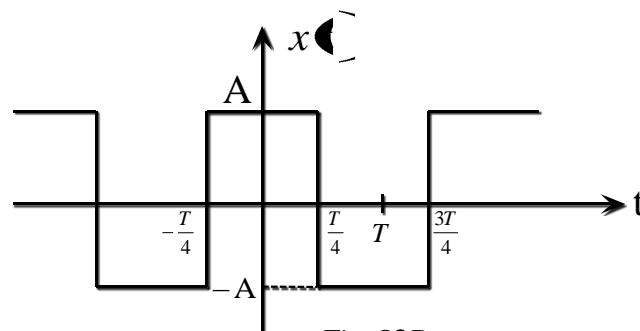


Fig. Q3B