

Dr. GRK

Reg.No



MANIPAL UNIVERSITY, MANIPAL
SECOND SEMESTER M.Sc. (Physics)
END SEMESTER EXAMINATION-2016
Numerical Methods and Computational Physics (PHY – 604)
(CREDIT SYSTEM)

Time: 3 Hrs.

Max. Marks: 50

NOTE: (a) Answer any FIVE full questions. (b) All questions carry equal marks.

1. (a) Write a C program to multiply two 4X4 matrices.
(b) Obtain Lagrange's interpolation formula from the properties of divided differences.
2. (a) Obtain Simpson's $1/3^{\text{rd}}$ integration rule from Newton's forward difference formula
(b) Write a C program to obtain linear least square fit for a given set of data
3. (a) Fit a 3^{rd} degree polynomial to the following data: (1, -5), (2, -5), (3, 9), (4, 43), (5, 103).
(b) Solve the following system of equations by Gauss-Jordan method:
$$\begin{aligned}10k - 2l + m - n &= 3 \\ -2k + 10l - m - n &= 15 \\ -k - l + 10m - 2n &= 27 \\ -k - l - 2m + 10n &= -9\end{aligned}$$
4. (a) Using Trapezoidal rule, evaluate $\int_0^1 \sqrt{1-x^2} dx$ with step-size $h=0.1$.
(b) Given that $y' = x - y^2$ and $y(0) = 1$. Using Taylor series for $y(x)$, find $y(0.1)$ correct to 4 decimal places.
5. (a) Solve the equation $\partial^2 u / \partial t^2 = \partial^2 u / \partial x^2$ (from time interval $k=1$ to $k=3$) with the conditions $u(0, t) = u(1, t) = 0$, $u(x, 0) = \sin^3(\pi x)$, $0 \leq x \leq 1$ and $u(i, -1) = u(i, 1)$
(b) Write a C program to simulate the radioactive decay process by Monte-Carlo technique. The results of the simulation must be stored in the file *D:\simulation.dat*.
6. (a) Write a C program to generate forward difference table for the given set of data
(b) Write a C program to find $\sin^{-1}(x)$ using following series. The number of terms in the series and the value of x are to be input by the user.
$$\sin^{-1}(x) = x + (1/2)(x^3/3) + (1/2)(3/4)(x^5/5) + \dots$$
