



## MANIPAL INSTITUTE OF TECHNOLOGY

Manipal University

## THIRD SEMESTER B.TECH (E &amp; C) DEGREE END SEMESTER

EXAMINATION - NOV/DEC 2016

SUBJECT: ELECTROMAGNETIC WAVES (ECE - 2102)

TIME: 3 HOURS

MAX. MARKS: 50

**Instructions to candidates**

- Answer **ALL** questions.
- Missing data may be suitably assumed.

- 1A. Derive an expression for the electric field of a line charge distribution of infinite length.
- 1B. Given three points  $A(4, 3, 2)$ ,  $B(-2, 0, 5)$ , and  $C(7, -2, 1)$ , i) Specify the vector **A** extending from the origin to the point A, ii) Calculate the perimeter of triangle  $ABC$ .
- 1C. A vector of magnitude 10 is directed from  $(5, 5\pi/4, 0)$  in cylindrical coordinates toward the origin. Express the vector in Cartesian coordinates. (5+3+2)
- 2A. A point charge at  $(1, -1, -3)$ m of charge  $300\mu\text{C}$  experiences a force of  $\mathbf{F} = 8\mathbf{a}_x - 8\mathbf{a}_y + 4\mathbf{a}_z$  N due to a charge  $Q$  at  $(3, -3, -2)$ m. Determine  $Q$ .
- 2B. Determine total charge within a sphere of radius 4m if volume charge density  $\rho_v = 10/(r\sin\theta)$  C/m<sup>3</sup>
- 2C. Show that if  $\mathbf{D} = (100/\rho)\mathbf{a}_\phi + 40\mathbf{a}_z$  in a certain region then there is no free charges in that region. (5+3+2)
- 3A. Given  $\mathbf{D} = 30x\mathbf{a}_x - 2z\mathbf{a}_z$ , evaluate both sides of the divergence theorem for the region defined by  $-1 < x < 1$ ,  $-1 < y < 1$  and  $-1 < z < 1$
- 3B. i) State Gauss's law ii) Discuss the divergence theorem.
- 3C. If the conduction current density in a lossy dielectric as  $0.02 \sin(10^9 t)$  A/m<sup>2</sup>, determine the displacement current density if the conductivity is  $10^3$  S/m and relative permittivity is 6.5. (5+3+2)
- 4A. Starting from the concept of reflection and refraction of plane waves at an interface, derive an expression for the Brewster angle.
- 4B. State the Maxwell's equations in point form and using appropriate theorems, convert them into the integral form.
- 4C. Given  $\mathbf{D} = -4\mathbf{a}_y + 1.5\mathbf{a}_z$  C/m<sup>3</sup> in free space ( $x > 0$ ), calculate  $\mathbf{P}$  in the dielectric ( $x < 0$ ), with  $\epsilon_r = 5$ . (5+3+2)
- 5A. A linearly polarized sinusoidal plane wave is incident from region-1 normal to the interface separating this region from another region-2. Region-1 is perfect dielectric and region-2 is perfect conductor. Derive expressions for total Electric and magnetic fields in region-1.
- 5B. A parallel polarized (p-polarized) EM wave is incident at oblique angle on the interface separating two perfect dielectric media. Derive expression for reflection coefficient.
- 5C. What is Poynting vector? In free space,  $\mathbf{E}(z, t) = 50\cos(\omega t - \beta z)\mathbf{a}_x$  V/m. Find the average power crossing a circular area of radius 2.5 m in the plane  $z = \text{constant}$ . (5+3+2)

