

## III SEMESTER B.TECH (ELECTRICAL & ELECTRONICS ENGINEERING)

MAKE UP EXAMINATIONS, DEC 2015 / JAN 2016

SUBJECT: ELECTROMAGNETIC THEORY [ELE 2104]

REVISED CREDIT SYSTEM

Time: 3 Hours

07 January 2016

MAX. MARKS: 50

### Instructions to Candidates:

- ❖ Answer **ALL** the questions.
- ❖ Missing data may be suitable assumed.

- 1A.** Determine the field intensity at a point 'P' at a distance 'h' metres above a straight, uniformly charged wire with a linear density of  $+\lambda$  coulomb per meter length. Find the electric field intensity if the point under consideration is along the perpendicular bisector of the wire. 4
- 1B.** A uniform sheet charge with  $\rho_s = (1/3\pi)$  nC/m<sup>2</sup> is located at  $z = 5$  m and a uniform line charge with  $\rho_L = - (25/9)$  nC/m at  $z = -3$ ,  $y = 3$  m. Find **E** at  $(x, -1, 0)$  3
- 1C.** If  $\mathbf{D} = (2y^2 + z) \mathbf{a}_x + 4xy \mathbf{a}_y + x \mathbf{a}_z$  C/m<sup>2</sup>, find 3
- a) The volume charge density at  $(-1, 0, 3)$
  - b) The flux through the cube defined by  $0 \leq x \leq 1, 0 \leq y \leq 1, 0 \leq z \leq 1$
  - c) The total charge enclosed by the cube
- 2A.** Two extensive homogeneous isotropic dielectric meet on  $z = 0$ . For  $z \geq 0$ ,  $\epsilon_r = 4$  and for  $z \leq 0$ ,  $\epsilon_r = 2$ . A uniform electric field  $\mathbf{E}_1 = 6\mathbf{a}_x + 2\mathbf{a}_y - 3\mathbf{a}_z$  exists for  $z \geq 0$ . Find 4
- a)  $\mathbf{E}_2$
  - b) Angle made by  $\mathbf{E}_2$  to the interface.
- 2B.** A spherical capacitor with  $a = 1.5$  cm and  $b = 4$  cm has an inhomogeneous dielectric of  $\epsilon = (10\epsilon_0) / r$ . Calculate capacitance of the capacitor. 3
- 2C.** The positive y-axis with a semi-infinite line with respect to origin carries a current of 2 A in the  $-\mathbf{a}_y$  direction. Find **H** at : 3
- a) A  $(2, 3, 0)$
  - b) B  $(3, 12, -4)$
- 3A.** Derive the expression for **H** at any point due to infinite sheet carrying current in the x-y plane using Ampere's circuital law. 4

**3B.** Given  $\mathbf{H} = y^2 z \mathbf{a}_x + 2(x+1)yz\mathbf{a}_y - (x+1)z^2\mathbf{a}_z$ .

- Find the total current enclosed in the square path from P (0, 2, 0) to Q (0, 3, 0) to R (0, 3, 1) to S (0, 2, 1) to P
- Prove that the line integral of  $\mathbf{H}$  over a closed path is equal to the surface integral of curl of  $\mathbf{H}$  for the given field.

3

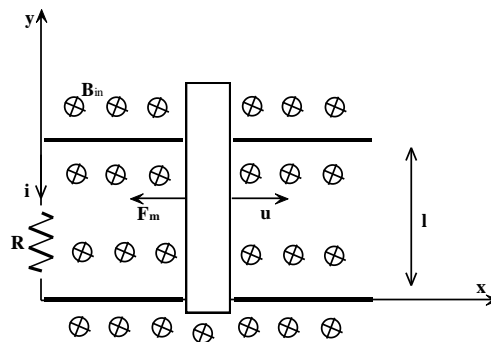
**3C.** A current filament carrying 8 A in the  $\mathbf{a}_z$  direction lies along the entire  $z$ -axis in free space. A rectangular loop connecting A (0, 0.2, 0) to B (0, 0.2, 0.3) to C (0, 0.7, 0.3) to D (0, 0.7, 0.2) to A lies in the  $x = 0$  plane. The loop current is 3 mA and it flows in the  $\mathbf{a}_z$  direction in the AB segment.

- Find force  $\mathbf{F}$  on the side AB
- Find force  $\mathbf{F}$  on the side DA

3

**4A.** Consider the loop of **Fig.1**. If  $\mathbf{B} = 0.5 \mathbf{a}_z$  Wb/m<sup>2</sup>,  $R = 20 \Omega$ ,  $l = 10$  cm, and the rod is moving with a constant velocity of  $8 \mathbf{a}_x$  m/s, find:

- The induced emf in the rod
- The current through the resistor
- The motional force on the rod



**Fig.1**

4

**4B.** In a medium characterized by  $\sigma = 0$ ,  $\epsilon = \epsilon_0$ ,  $\mu = \mu_0$   $\mathbf{E}(z, t) = 20\sin(10^8 t - \beta z)\mathbf{a}_y$  V/m. Calculate  $\beta$  and  $\mathbf{H}$ .

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**4C.** In free space ( $z \leq 0$ ) a plane wave with  $\mathbf{H}_i = 100 \sin(10^8 t - \beta z) \mathbf{a}_x$  A/m is incident normally on a lossless medium ( $\epsilon = 2\epsilon_0$ ,  $\mu = 8\mu_0$ ) in region  $z \geq 0$ . Determine reflected wave  $\mathbf{E}_r$  and the transmitted wave  $\mathbf{H}_t$ .

4

**5A.** Derive Poynting theorem and show that total power leaving the volume is equal to rate of decrease in energy stored in electric and magnetic fields minus power dissipated

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**5B.** In free space,  $\mathbf{H}(z, t) = 0.2\sin(\omega t - \beta z)\mathbf{a}_y$  A/m. Find the total power passing through the circular disk of radius 5 cm on plane  $z = 1$ .

2

**5C.** An EM wave travels in free space with electric field component  $\mathbf{E}_s = 60e^{j(0.5y + 0.866z)} \mathbf{a}_x$  V/m. Determine

- $\omega$  and  $\lambda$
- The magnetic field component
- The time average power in the wave.

4