

III SEMESTER B.TECH END SEMESTER EXAMINATIONS, NOV/DEC 2015

SUBJECT: ELECTROMAGNETIC THEORY [ELE 2104]

REVISED CREDIT SYSTEM

Time: 3 Hours

05 DECEMBER 2015

MAX. MARKS: 50

Instructions to Candidates:

- ❖ Answer **ALL** the questions.
- ❖ Missing data may be suitable assumed.
- ❖ Use of Steam Table is permitted

- 1A.** A circular disc of radius **R** carries a uniform charge ρ_s C/m² and is placed on the **x-y** plane with the axis same as z-axis. Derive the expression for electric field at (0, 0, h) from the center. **3**
- 1B.** Spherical surfaces at $r = 2, 4,$ and 6m carry uniform surface charge densities of $20\text{nC/m}^2, -4\text{nC/m}^2$ and ρ_{so} respectively. (a) Find **D** at $r = 1\text{m}$ and 3m . (b) Determine ρ_{so} such that **D** = 0 at $r = 7\text{m}$. **4**
- 1C.** Two parallel conducting planes in free space are at $y = 0$ and $y = 0.02\text{ m}$ with potential **0** and **V** volts respectively. If **D** = $253 \mathbf{a}_y$ nC/m² between the conductors, determine the conductor voltage. **3**
- 2A.** In the region of free space that includes the volume $2 < x, y, z < 3,$ **D** = $2xy \mathbf{a}_x + x^2 \mathbf{a}_y + 6z^3 \mathbf{a}_z$ C/m². Verify both sides of divergence theorem. **4**
- 2B.** A cylindrical capacitor has radii $a = 1\text{ cm}$ and $b = 2.5\text{ cm}$. If the space between the plates is filled with an inhomogeneous dielectric with $\epsilon_r = (10+p)/p$ where p is in centimeters, find the capacitance per unit length. **4**
- 2C.** An infinitely long filamentary wire carries a current of **2A** in the **+z** direction. Calculate
- I. **B** at $(-3, 4, 4)$
 - II. The flux through the square loop described by $2 \leq \rho \leq 6, 0 \leq z \leq 4, \phi = 90^\circ$. **2**
- 3A.** Determine the self-inductance of a co-axial cable per unit length of inner radius **a** and outer radius **b**. **4**
- 3B.** Region 1 described by $2x+5y \geq 10$ is free space while region 2 described by $2x+5y \leq 10$ is a magnetic material for which $\mu = 8\mu_0$. Assuming that boundary between the material and free space is current free, if **B**₁ = $0.2 \mathbf{a}_x + 0.4 \mathbf{a}_y + 0.1 \mathbf{a}_z$ Wb/m², find **B**₂, **H**₂ **4**

- 3C.** If $\mathbf{H} = (4z - y)\mathbf{a}_x + 6xz\mathbf{a}_y$, then find the current density and current passing through the plane $y = 2$, $-2 < x < 2$, $1 < z < 3$. **2**
- 4A.** A circular conducting loop of radius 20 cm and resistance 5Ω lies in $z = 0$ plane in a magnetic field $\mathbf{B} = 10\cos(377t) \mathbf{a}_z$ mWb/m². Calculate the current induced in the loop **2**
- 4B.** In a certain medium $\mathbf{E} = 16e^{-0.05x} \sin(2 \times 10^8 t - 2x)\mathbf{a}_z$ V/m. Find (a) The propagation constant (b) the wavelength (c) the speed of the wave (d) the skin depth. **3**
- 4C.** In a nonmagnetic medium ($\mu_r = 1$) $\mathbf{E} = 50\cos(10^9 t - 8x)\mathbf{a}_y + 40\sin(10^9 t - 8x)\mathbf{a}_z$ V/m. Find the dielectric constant ϵ_r , Direction of wave propagation and the corresponding \mathbf{H} Field. **4**
- 5A.** Derive pointing theorem and show that total power leaving the volume is equal to rate of decrease in energy stored in electric and magnetic fields minus power dissipated **4**
- 5B.** In free space, $\mathbf{E}(z, t) = 150\sin(\omega t - \beta z)\mathbf{a}_x$ V/m. Find the total power passing through the rectangular area, of sides 30 mm and 15 mm, in the $z = 0$ plane. **2**
- 5C.** An EM wave travels in free space with electric field component $\mathbf{E} = (10\mathbf{a}_y + 5\mathbf{a}_z) \cos(\omega t + 2y - 4z)$ in free space. (a) Calculate λ and ω (b) The angle of incidence (c) The reflected \mathbf{E} and \mathbf{H} field. **4**