

## Manipal University, Manipal



## III SEMESTER M.Sc. (APPLIED MATHEMATICS AND COMPUTING) END SEMESTER EXAMINATIONS, NOV/DEC 2015

## SUBJECT: FORMAL LANGUAGE AND THEORY OF COMPUTATION [MAT 709.10]

Time: 3 Hours

MAX. MARKS: 50

|              | Instructions to Candidates:   |  |   |          |  |         |                       |         |         |  |
|--------------|---|--|---|----------|--|---------|-----------------------|---------|---------|--|
|              | Answer ANY FIVE FULL the questions.   |  |   |          |  |         |                       |         |         |  |
| 1A.          | Sketch the block diagram of a finite automaton and explain it's parts.  |  |   |          |  |         |                       |         | 4 Marks |  |
| 1 <b>B</b> . | Define ambiguous grammar.<br>Show that the grammar $S \rightarrow a \mid abSb \mid aAb, A \rightarrow bS \mid aAAb$ is ambiguous.               |  |   |          |  |         |                       | 3 Marks |         |  |
| 1C.          | Show that $\{abc,bca,cab\}$ can be generated by a regular grammar whose terminal set is $\{a,b,c\}$ .   |  |   |          |  |         |                       |         | ırks    |  |
| 2A.          | Define<br>Convert<br>given ta   | Mealy Mach<br>t the given<br>able:<br>State<br>$\rightarrow q_1$<br>$q_2$<br>$q_3$ | nine.<br>machine<br>Next Stat<br>i.p = 0<br>State<br>$q_3$<br>$q_1$<br>$q_2$<br>$\tilde{q}_2$ | in to ar | i.p a=1<br>State<br>q <sub>2</sub><br>q <sub>4</sub><br>q <sub>1</sub> | lent Mo | pore machine from the | 4 Ma    | ırks    |  |
| 2B.          | Find all strings of length 5 and write the regular set from the regular expression $a^* + (ab + a)^*$ .   |  |   |          |  |         |                       |         |         |  |
| 2C.          | Construct a minimum state automaton equivalent to the finite automaton given in figure $ \begin{array}{c}                                     $ |  |   |          |  |         |                       |         |         |  |





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|------------|--|---------|
| 3A.        | Prove that there exists a recursive set which is not a context sensitive language over $\{0,1\}$ .   | 4 Marks |
| 3B.        | Define push down automata. Represent this transition diagram in terms of PDA<br>$1 \xrightarrow{q_0} \xrightarrow{q_1} \xrightarrow{q_1} \xrightarrow{q_2} \xrightarrow{q_2} \xrightarrow{q_1} \xrightarrow{q_2} \xrightarrow{q_2} \xrightarrow{q_2} \xrightarrow{q_1} \xrightarrow{q_2} \xrightarrow{q_1} \xrightarrow{q_2} q_$ | 3 Marks |
| 3C.        | Show that $L=\{a^p/p \text{ is a prime}\}$ is not regular.   | 3 Marks |
| <b>4A.</b> | Find the regular expression corresponding to the figure using Arden's theorem.   | 4 Marks |
| <b>4B.</b> | State and prove pumping lemma for regular sets.  | 3 Marks |
| 4C.        | <ul> <li>Find regular expressions representing the following sets:</li> <li>i)the set of all strings over {0,1} having atmost one pair of 0's or atmost one pair of 1's.</li> <li>ii)the set of all strings over {0,1} ending with 11 and beginning with 00.</li> </ul>  | 3 Marks |
| 5A.        | Define a Greibach normal form. Convert the grammar $S \rightarrow AB, A \rightarrow BS/b, B \rightarrow SA/a$ , into GNF.  | 4 Marks |
| 5B.        | State and prove Kleen's theorem.   | 3 Marks |
| 5C.        | Show that there exists no finite automaton accepting all palindromes over $\{a,b\}$  | 3 Marks |
| 6A.        | Define a Greibach normal form. Convert the grammar $S \rightarrow AB, A \rightarrow BS/b, B \rightarrow S A/a$ , into GNF.   | 4 Marks |
| 6B.        | Show that $\{a^n b^n c^n   n \ge 1\}$ is not context free but context sensitive.   | 3 Marks |
| 6C.        | If L is regular then prove that $L^T$ is also regular.   | 3 Marks |