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Manipal University, Manipal
First Semester M.Sc.(Physics)
End Semester Examination, December 2015
Subject: Quantum Mechanics I (PHY-605)
(Credit System)

Time: 3 hours

Marks: 50

Answer any five full questions.

1. For the Gaussian wavepacket given by

$$\psi(x, 0) = \frac{1}{(\pi\sigma_0^2)^{\frac{1}{4}}} \exp\left(-\frac{x^2}{2\sigma_0^2} + \frac{i}{\hbar}p_0x\right)$$

evaluate $\langle x \rangle$, $\langle x^2 \rangle$, $\langle p \rangle$, $\langle p^2 \rangle$, and show that $\Delta x \Delta p = \frac{1}{2}\hbar$. [10]

2. (i) Show that eigenfunctions of a Hermitian operator belonging to different eigenvalues are orthogonal. [5]

(ii) Briefly discuss about the Dirac's bra-ket notations. [5]

3. Show that for a finite deep square potential well only finite number of energy levels are possible. [10]

4. (i) The time-independent wave function of a particle of mass m moving in a potential $V(x) = \alpha^2 x^2$ is

$$\psi(x) = \exp\left(-\sqrt{\frac{m\alpha^2}{2\hbar^2}}x^2\right)$$

where α being a constant. Find the energy of the system. [5]

(ii) A rigid rotator is constrained to rotate about a fixed axis. Find the eigenvalues and eigenfunctions. [5]

5. A particle of mass m is confined to the interior of a hollow spherical cavity of radius R with impenetrable walls. Find the pressure exerted on the walls of the cavity by the particle in its ground state. [10]

6. (i) Explain the meaning of:

(a) identical particle,

(b) distinguishable particles,

(c) indistinguishable particles. [5]

(ii) Write short notes on symmetric and anti-symmetric wave-functions. [5]

Useful formulae:

$$\int_0^\infty \exp(-ax^2) dx = \frac{1}{2} \sqrt{\left(\frac{\pi}{a}\right)}$$

$$\int_0^\infty x^2 \exp(-ax^2) dx = \frac{\sqrt{\pi}}{4} \frac{1}{a^{3/2}}$$

$$\int_0^\infty x^4 \exp(-ax^2) dx = \frac{3\sqrt{\pi}}{8} \frac{1}{a^{5/2}}$$

$$\nabla^2 t = \frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 \frac{\partial t}{\partial r} \right) + \frac{1}{r^2 \sin \theta} \frac{\partial}{\partial \theta} \left(\sin \theta \frac{\partial t}{\partial \theta} \right) + \frac{1}{r^2 \sin^2 \theta} \frac{\partial^2 t}{\partial \phi^2}$$