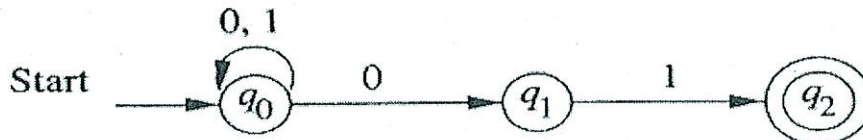


Instructions to candidates

- Answer any FIVE FULL questions.
- Missing data, if any, may be suitably assumed.

1A. Convert the following NFA to DFA.



1B. Give formal definition of a DFA. Find a DFA for accepting all strings over  $\{a,b\}$  such that there is no substring bbb.

1C. Construct an NFA for the following regular expression.  
 $(0+1)^*11+0^*$

[5+3+2]

2A. Give the proof for the theorem "If  $L=L(A)$  for some DFA A, then there is a regular expression R such that  $L=L(R)$ ".

2B. Prove that the following language is not regular using Pumping lemma.  
 $L=\{a^n b^n : n \geq 1\}$

2C. List any four closure properties of regular languages and explain.

[5+3+2]

3A. Design an NPDA for the following language.  
 $L= \{ ww^r : w \text{ is in } (a+b)^* \}$

3B. Convert following grammar to PDA.  
 $S \rightarrow AB \quad A \rightarrow aAb|ab \quad B \rightarrow cBd|cd$

3C. What are parse trees? Give an example for a parse tree.

[5+3+2]

4A. Convert the following grammar to GNF.  
 $S \rightarrow AA|0 \quad A \rightarrow SS|1$

4B. Prove that "If L is CFL and R is regular language, then  $L \cap R$  is a CFL".

4C. List any four undecidable problems about Context Free Language.

[5+3+2]

5A. Design a Turing Machine to accept all strings with balanced parentheses.

5B. Discuss Storage in the state construction technique for Turing machines with a suitable example.

5C. Show that the class of Turing Machines with Semi-infinite tapes are equivalent to the standard Turing Machines.

[5+3+2]

6A. List and give proof for any five closure properties of recursive languages.

6B. Prove that if there is a reduction from P1 to P2 then

- If P1 is undecidable then so is P2
- If P1 is not recursively enumerable so is P2

6C. Give two examples for NP complete problems.

[5+3+2]