



## Manipal Institute of Technology, Manipal

(A Constituent Institute of Manipal University)



(03)

## V SEMESTER B.TECH (AERONAUTICAL ENGINEERING) END SEMESTER EXAMINATIONS, DEC 2015/JAN 2016

SUBJECT: CONTROL SYSTEMS DESIGN [AAE-303]

## **REVISED CREDIT SYSTEM**

Time: 3 Hours

MAX. MARKS: 50

## Instructions to Candidates:

- ✤ Answer ANY FIVE FULL the questions.
- ✤ Missing data may be suitable assumed.
- 1A. An automobile driver uses a control system to maintain the speed of the car at (02) a prescribed level. Sketch a block diagram to illustrate this feedback system
- 1B. Derive the transfer function of DC Motor.
- 1C. Determine an internal controller  $G_c(s)$  for the system shown in figure below. It (05) is desired that the steady-state error to a ramp be zero and that settling time (2% criterion) of the ramp response be less than 8 seconds. Where, process is 1/(s+5)(s+7). Also find the suitable K.



- 2A. Sketch the signal  $x(t) = 5r(t)u(-t) + \sin(-t)u(-t+5)$ , r(t) ramp input. (02)
- 2B. Find the response of the circuit to the input x(t) = r(t) 2r(t-1) + r(t-2) (03)



2C. Design a root locus system and analyze the stability of a system as given (05) below



Where,  $G_C(s) = K_P + K_D s + K_I / s$  and G(s) = 1/(s+5)(s+6).

3A. Model the following system given below



(02)

3B. Sketch the signal flow graph of series RLC circuit and derive its transfer (03) function using Mason's gain formula.

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3C. Explain the bode plot of a system given as below:

$$G(j\omega) = \frac{K_b \prod_{i=1}^{M} (1 + j\omega\tau_i)}{(j\omega)^N \prod_{m=1}^{M} (1 + j\omega\tau_m) \prod_{k=1}^{R} [(1 + (2\varsigma_k / \omega_{nk}) / j\omega + (j\omega / \omega_{nk})^2)]}$$

- 4A. Derive the Laplace transform of integration of a system  $L[\int x(\tau)d\tau]$ . (02)
- 4B. In the circuit shown the switch is at position for a very long time and at t=0, the switch moved to position 2. Solve for current i(t), for  $t \ge 0$  using Laplace transform.



(05)

(03)

(05)

(03)

- 4C. Derive the transient response of mass-spring-damper system in underdamped (05) case and find the %Overshoot, settling time, rise time and peak time.
- 5A. Analyze stability of a system given below for non-negative values of K. (02)

$$\frac{d^{3}y(t)}{dt^{3}} + K\frac{d^{2}y(t)}{dt^{2}} + 5\frac{dy(t)}{dt} + 6y(t) = \frac{dx(t)}{dt} + 4x(t)$$

- 5B. Explain the frequency response of mass-spring-damper system. (03)
- 5C. State Space representation of a system is given below,

$$x = \begin{bmatrix} 0 & 1 & 0 \\ 0 & -2 & 1 \\ 0 & -8 & -5 \end{bmatrix} x + \begin{bmatrix} 0 \\ 0 \\ K \end{bmatrix} u$$
  
$$y = \begin{bmatrix} 1 & 0 & 0 \end{bmatrix} x + \begin{bmatrix} 0 \\ 0 \\ K \end{bmatrix} u$$

Design a state feedback controller which suits the following design parameters (i) Settling time (2% criterion) less than 5 sec and (ii) overshoot 12%.

6A. A hovering vehicle control systems is represented by following equation, (02)

$$\bar{x}_1 = 6x_2$$
 and  $\bar{x}_2 = -x_1 - 5x_2$ .

Find the state transition matrix and roots of characteristics equation.

6B. Consider the third-order system

$$\begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -10 & -8 & -5 \end{bmatrix} x + \begin{bmatrix} 0 \\ 0 \\ 2 \end{bmatrix} u$$
  
$$y = \begin{bmatrix} 3 & -5 & 0 \end{bmatrix} x + \begin{bmatrix} 0 \\ 0 \\ 2 \end{bmatrix} u$$

Verify that the system is observable. If so, determine the observer gain matrix required to place the observer poles at  $(-1 \pm j^2)$  and -5.

6C. An *RL* circuit is shown in Figure (a) Select the two stable variables and obtain the vector differential Equation, where the output is  $v_0(t)$ 

(b) Determine whether the state variables are observable when

 $R_1 / L_1 = R_2 / L_2$ 

(c) Find the conditions when the system has two equal roots.

