

V SEMESTER B.TECH (ELECTRICAL & ELECTRONICS ENGINEERING)

MAKE UP EXAMINATIONS, DEC 2015 / JAN 2016

SUBJECT: DIGITAL SIGNAL PROCESSING [ELE 303]

REVISED CREDIT SYSTEM

Time: 3 Hours

31 December 2015

MAX. MARKS: 50

Instructions to Candidates:

- ❖ Answer **ANY FIVE FULL** questions.
- ❖ Missing data may be suitably assumed.
- ❖ DSP Quick reference table may be used.

- 1A.** Using overlap-add method perform the convolution of $x(n)$ with $h(n)$. Take sub frame length of 6.

$$x(n)=[1, 2, 0, -3, 4, 2, -1, 1, -2, 3, 2, 1] \text{ and } h(n)=[1, 1, 1]$$

(05)

- 1B.** Design an FIR-Linear phase digital filter approximating the ideal frequency response

$$H_d(\omega) = \begin{cases} 1, & \text{for } 0 \leq |\omega| \leq \frac{3\pi}{4} \\ 0, & \text{for } \frac{3\pi}{4} < |\omega| \leq \pi \end{cases}$$

Determine the filter co-efficient of a 7-tap filter based on window method with a Hamming window.

(05)

- 2A.** Consider a causal IIR system with system function

$$H(z) = \frac{1 + 2z^{-1} + 3z^{-2} + 2z^{-3}}{1 + 0.9z^{-1} - 0.8z^{-2} + 0.5z^{-3}}$$

- a) Determine the equivalent lattice-ladder structure.
- b) Check if the system is stable.

(08)

- 2B.** An analog electrocardiogram (ECG) signal contains useful frequencies up to 100Hz.

- a) What is the Nyquist rate of the signal?
- b) Suppose that we sample this signal at a rate of 250 samples/s what is the highest frequency can be represented uniquely at this sampling rate?

(02)

- 3A.** Consider the sequence $x(n) = 4\delta(n) + 3\delta(n-1) + 2\delta(n-2) + \delta(n-3)$. If $X(k)$ be the 6 point DFT of $x(n)$, find the finite length sequence $y(n)$ that has a 6 point DFT $Y(k) = W_6^{4k} X(k)$.

(03)

- 3B.** Determine the coefficients $h(n)$ of a linear-phase FIR filter of length $M=15$ which has a symmetric unit sample response and a frequency response that satisfies the condition

$$H_r\left(\frac{2\pi k}{15}\right) = \begin{cases} 1, & k = 0,1,2,3 \\ 0, & k = 4,5,6,7 \end{cases} \quad (07)$$

- 4A.** An IIR filter digital low pass filter is required to meet the following specifications

Passband ripple $\leq 0.8\text{dB}$

Passband edge: 1KHz

Stopband edge: 5KHz

Stopband attenuation: $\geq 40\text{dB}$

The filter is to be designed using impulse invariant transformation on an analog system function. Use Chebyshev approximation.

(05)

- 4B.** Find the 4 point circular convolution of $x_1(n)$ and $x_2(n)$ using DFT –IDFT method.

$$x_1(n)=[1, 2, 3, 1] \text{ and } x_2(n)=[4, 3, 2, 2]$$

(05)

- 5A.** Compute the 8 point DFT of the sequence $x(n)$ using radix-2 DIT-FFT algorithm.

$$x(n)=[2, 1, -1, -3, 0, 1, 2, 1]$$

(06)

- 5B.** Consider the causal linear shift invariant filter with system function $H(z)$. Draw the cascade structure for the system.

$$H(z) = \frac{1 + 0.875z^{-1}}{(1 + 0.2z^{-1} + 0.9z^{-2})(1 - 0.7z^{-1})} \quad (04)$$

- 6A.** A digital notch filter is required to remove an undesirable 60Hz hum associated with a power supply in an ECG recording application. The sampling frequency used is $F_s = 260$ samples/s.

a) Design a second order FIR notch filter. b) Design a second order pole-zero notch filter. For both the cases choose b_0 so that $|H(\omega)| = 1$ for $\omega = 0$.

(05)

- 6B.** An IIR Butterworth digital low pass filter is required to meet the following specifications

Passband ripple $\leq 0.5\text{dB}$

Passband edge: 1KHz

Stopband edge: 2KHz

Stopband attenuation: $\geq 40\text{dB}$

Sample rate: 8KHz

Use Bilinear transformation.

(05)