

VII SEMESTER B.TECH (AERONAUTICAL ENGINEERING)
END SEMESTER EXAMINATIONS, DEC 2015\ JAN 2016

SUBJECT: FINITE ELEMENT METHOD [AAE 405]

REVISED CREDIT SYSTEM

Time: 3 Hours

MAX. MARKS: 50

Instructions to Candidates:

- ❖ Answer **ANY FIVE FULL** the questions.
- ❖ Missing data may be suitable assumed.

- 1A.** For the beam shown in Figure 1, determine the displacements and the slopes (05)
 at the node2.

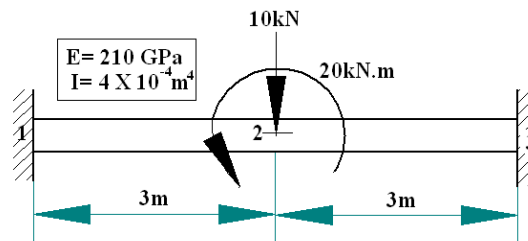


Figure 1

- 1B.** For the beams shown in Figure2, determine the displacements and the (05)
 slopes at the nodes.

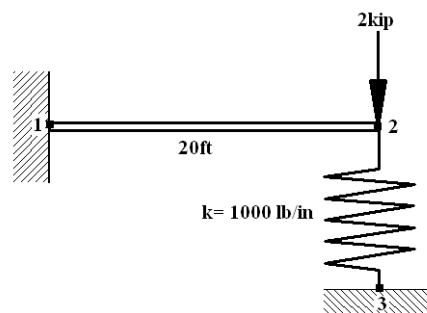


Figure 2

- 2A.** For the beams shown in Figure 3, determine the displacements and the (05)
 slopes at the nodes. Given: $E = 30 \times 10^6$ psi, $I = 100$ in⁴.

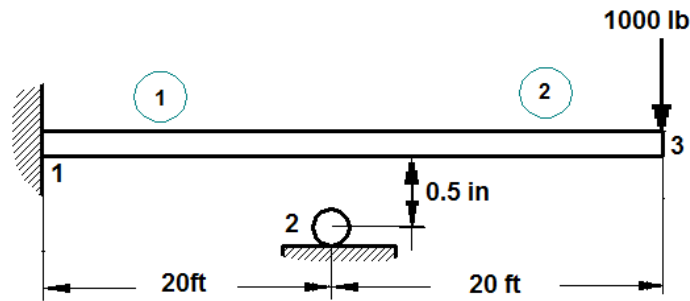


Figure 3

- 2B. Use the principle of minimum potential energy to solve the spring problems shown in Figure 4. Determine the nodal displacement. (05)

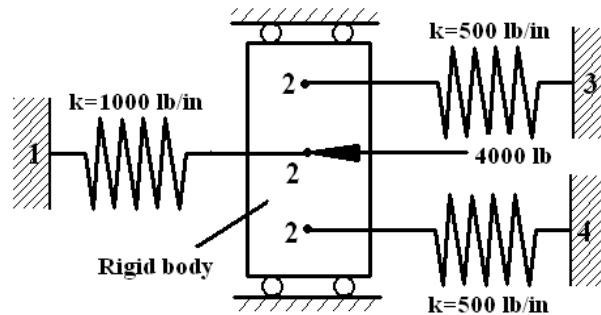


Figure 4

- 3A. For the truss shown in Figure 5, use symmetry to determine the displacements of the nodes and the stresses in each element. All elements have $E = 30 \times 10^6$ psi. Elements 1, 2, 4, and 5 have $A = 10$ in² and element 3 has $A = 20$ in². (07)

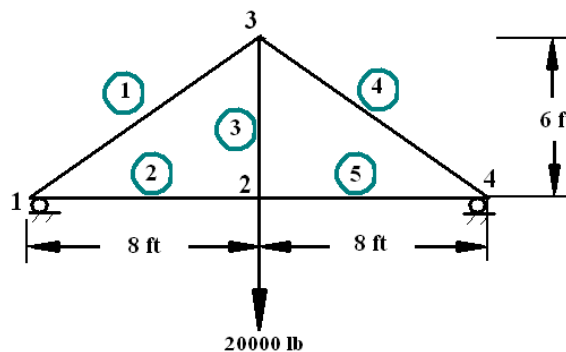


Figure 5

- 3B. Briefly explain Co-ordinate systems used in FEM. (03)

4. For the beams shown in Figure 6, determine the nodal displacements and slopes, the forces in each element, and the reactions. (10)

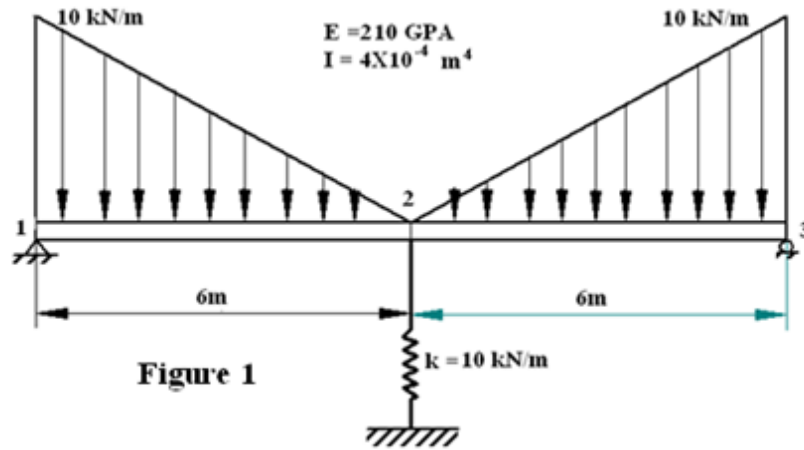


Figure 1

Figure 6

	f_{1y}	m_1	f_{2y}	m_2
	$-\frac{7wL}{20}$	$-\frac{wL^2}{20}$	$-\frac{3wL}{20}$	$\frac{wL^2}{30}$

5. For the plane trusses shown in Figure 7, determine the horizontal and vertical displacements of node 1 and the stresses in each element. All elements have $E = 210 \text{ GPa}$ and $A = 4 \times 10^{-4} \text{ m}^2$. (10)

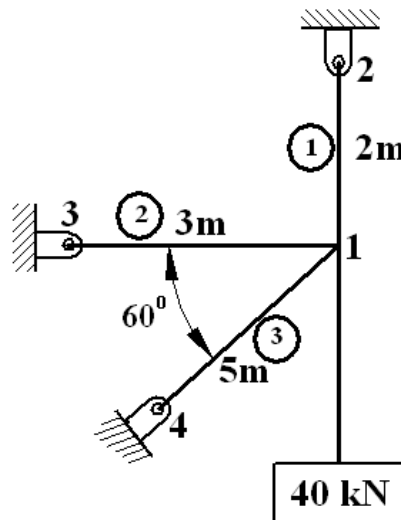


Figure 7

6. For the plane strain elements shown in Figure 8, the nodal displacements are given as (10)

$$u_1 = 0.001 \text{ in}; v_1 = 0.005 \text{ in}; u_2 = 0.001 \text{ in};$$

$$v_2 = 0.0025 \text{ in}; u_3 = 0.0 \text{ in}; v_3 = 0.0 \text{ in};$$

Determine the stiffness and element stresses $\sigma_x, \sigma_y, \tau_{xy}, \sigma_1$, and σ_2 and the principal angle θ_p . Let $E = 30 \times 10^6 \text{ psi}$ and $\theta = 0.25$, and use unit thickness for plane strain. All coordinates are in inches.

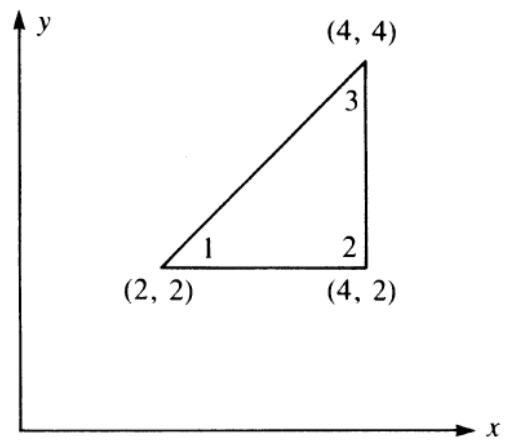


Figure 8