Reg.No.					

प्रज्ञानं ब्रह्म Manipal MANIPAL INSTITUTE OF TECHNOLOGY

(A constituent institute of Manipal University)



## VII SEMESTER. B.Tech. (MECHANICAL ENGINEERING) END SEMESTER (MAKE UP) EXAMINATIONS, DEC 2015/JAN 2016

## SUBJECT: COMPUTATIONAL FLUID DYNAMICS (MME 441) (REVISED CREDIT SYSTEM)

Time: 3 Hours.

MAX.MARKS: 50

-02-

-04-

## Instructions to Candidates:

- Answer **ANY FIVE** full questions.
- ♦ Missing data may be suitably assumed.
- **Q.1A** State the **Basic Four Rules** for control volume formulation.
- **Q.1B** Derive the Energy Equation in the non-conservative form and reduce the same to **-08–** conservative form.
- **Q.2A** For the 2-D Fourier thermal diffusive flow equation given by

$$k_x \frac{d}{dx} \left[ \frac{dT}{dx} \right] + k_y \frac{d}{dy} \left[ \frac{dT}{dy} \right] + \dot{q}_g = 0$$

obtain the discretised equation using Finite Volume technique, in the form

$$a_P T_P = a_W T_W + a_E T_E + a_S T_S + a_N T_N + b$$

Q.2B Solve for steady state temperature distribution in a one dimensional bar having conductivity as 1000 w/m.K and a cross sectional area of 10X 10<sup>-3</sup> m, as given below: Use TDMA for computation of grid temperatures.



- **Q.3A** Enumerate the challenges and the respective strategies to overcome the same in **-06**the case of convection dominated diffusion flows. Deduce the velocity correction equation and hence derive the **Pressure Correction Equation** for Convection dominated Diffusion flow.
- **Q.3B** Derive the scale-free (non-dimensional) form of the Continuity Equation for a **-04**-differential control volume fixed in space.
- Q.4A Explain the SIMPLE algorithm of Patankar and Spalding with a neat flow diagram -04-

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- Q.4B Solve for steady state temperature distribution in a one dimensional pin fin exposed to -06-350°C and the other end having an insulated free end. The fin is exposed to convective ambience having a convective heat transfer coefficient of 10 W/m<sup>2</sup>.K and ambient temperature of 35 °C. The thermal conductivity of the fin material is 100 w/m.K and a cross sectional area of 0.0025m<sup>2</sup>. The fin is 0.25m long. Discretize the domain into 5 control volumes and use TDMA for computation of grid temperatures.
- **Q.5A** Explain the characteristic advantages and limitations of solving a transient **-03**unsteady heat transfer problem by,
  - (i) Euler's Explicit Method
    - (ii) Crank-Nicholson Semi-Implicit Method
  - (iii)Pure Implicit Method
- Q.5B Determine the steady state temperature distribution for the one dimensional composite -07wall given below. Use Control Volume Method. Use atleast three CVs. -



**Q.6A** Deduce the finite difference expression for second order accurate mixed derivative **-06**-given by,

$$\left(\frac{\partial^2 u}{\partial x \,\partial y}\right)_{i,j} = \frac{u_{i+1,j+1} - u_{i+1,j-1} - u_{i-1,j+1} + u_{i-1,j-1}}{4\Delta x \,\Delta y} + \mathcal{O}[(\Delta x)^2, (\Delta y)^2]$$

- **Q.6B** With regard to finite difference discretization schemes of CDS and UDS, compare **-04**-(a) Consistency
  - (b) Boundedness
  - (c) Transportiveness
  - (d) Accuracy