

## MANIPAL INSTITUTE OF TECHNOLOGY

**I SEMESTER M.TECH. (CIVIL ENGINEERING)** 

## END SEMESTER EXAMINATIONS, NOV/DEC 2016

SUBJECT: ADVANCED MECHANICS OF SOLIDS [CIE 5151]

## REVISED CREDIT SYSTEM ( /11/2016)

Time: 3 Hours

MAX. MARKS: 50

## Instructions to Candidates:

- ✤ Answer ALL the questions.
- ✤ Missing data may be suitable assumed.

|              | The general displacement fields in a body in Cartesian coordinate system is given by   | 5  |
|--------------|--|----|
| 1A.          | $u = 3x^2y + y^2$ ; $v = 3yz + xy$ ; $w = 4xz^2 + 5xy^2$ . Find strain tensor and the linear strain  |    |
|              | at the point (1, -3, 2) in the direction (0.6, 0.53, -0.6).  |    |
| 1 <b>B</b> . | Derive the stress compatibility conditions for plane stress condition (2D).  | 5  |
| 2.           | State of stress at a point in a strained body is given: $\sigma = \begin{bmatrix} 30 & -45 & -65 \\ -45 & 45 & 30 \\ -65 & 30 & -25 \end{bmatrix} MPa$   | 10 |
|              | Determine the three principal stresses and associated principal planes.  |    |
| 3A.          | Analyze for stress in a cantilever beam of span 'L', unit width and depth '2C', subjected to point load at free end, considering Airy's stress function $\phi = Bxy + Dxy^3$ . Take origin at fixed end. | 5  |
| <b>3B.</b>   | Derive the strain displacement relations in 2D polar co-ordinate system.   | 5  |
| 4A.          | For a thin rectangular plate subjected to uniformly distributed load, obtain the expressions for Kirchhoff's shear forces in terms of vertical displacement 'w'.   | 5  |
| 4 <b>B</b> . | For a simply supported plate subjected to uniform constant lateral load ' $q_o$ ' using Navier's solution, obtain the expressions for deflection and moments.  | 5  |
| 5A.          | Obtain the expressions for deflection and moment of an annular plate simply supported at outer edges, and loaded by edge moments $M_1$ at the inner edge (r = b) & $M_2$ at outer edge (r = a).          | 5  |
| 5B.          | With usual notations for a shell element, obtain the stress resultants in terms of strains and curvature.  | 5  |