



MANIPAL INSTITUTE OF TECHNOLOGY
Manipal University
FIRST SEMESTER M. Tech. (DEAC) DEGREE END SEMESTER
EXAMINATION - NOV/DEC 2016
SUBJECT: DETECTION AND ESTIMATION THEORY (ECE -5104)

TIME: 3 HOURS

MAX. MARKS: 50

Instructions to candidates

- Answer **ALL** questions.
- Missing data may be suitably assumed.

- 1A. Derive the likelihood ratio test (LRT), under the criterion for a binary hypothesis problem.
- 1B. What is the Variance of the sum of Two Random Variables is $\text{Var}[X+Y]$ For two Independent Random Variables what is the Variance and Covariance. What is the correlation Coefficient?
- 1C. What is ML estimation Explain (5+3+2)
- 2A. With probability p a digital communication system transmits a 0. It transmits a 1 with probability $1-p$. The received signal is either $X = -v+N$ volts, if the transmitted bit is 0; or $v+N$ volts if the transmitted bit is 1. The voltage v is the received component of the signal and N is the Gaussian random variable for noise. Given the received signal X , what is the minimum probability of error rule for deciding whether 0 or 1 was transmitted.
- 2B. What is linear estimation of X given Y ? What is correlation between X and Y under different condition? Explain.
- 2C. Explain Kalman Filter with necessary diagram. (5+3+2)
- 3A. What is Maximum Likelihood Detection? With necessary equation? What is the difference between MAP and ML detection? Explain.
- 3B. Explain a Stochastic Process. What do you mean by stationary process? What is poisson process define its properties.
- 3C. Discuss difference between Markov and Chebyshev inequality. (5+3+2)
- 4A. Describe consistent estimator, unbiased Estimator, biased Estimator
- 4B. What is Type 1 error and Type II error in detection Explain with necessary equation
- 4C. Explain Wiener filter with necessary equation and block diagram. (5+3+2)

- 5A. Let X and Y be Gaussian Random Variables with $E[X]=E[Y]=0$ and $\text{Var}[X]=1$ and $\text{VAR}[Y]=4$
- a) Sketch pdfs $f_x(x)$ and $f_Y(y)$ on the same axes.
 - b) What is $P[-1 < X \leq 1]$
 - c) What is $P[Y > 3.5]$
 - d) What is $P[X > 3.5]$
 - e) What is $P[-1 < Y \leq 1]$
- 5B. Explain different application of estimation and detection in detail.
- 5C. What are the advantages of Blind estimation over other estimators?

(5+3+2)