



## FIRST SEMESTER M.TECH. (AEROSPACE ENGINEERING)

### END SEMESTER EXAMINATIONS, NOV/DEC 2016

#### SUBJECT: AEROSPACE SYSTEMS MODELLING [ICE 5101]

Time: 3 Hours

MAX. MARKS: 50

#### Instructions to Candidates:

- ❖ Answer **ALL** the questions.
- ❖ Missing data may be suitably assumed.

- 1A. Consider the simple mass-spring –damper system subjected to an input force  $f$ , as shown in Fig. Q1A. Obtain transfer function and state space model for this system. 5
- 1B. Write the differential equations governing the mechanical rotational system as shown in Fig. Q1B and obtain the transfer function model 3
- 1C. List the drawbacks in the conventional transfer function model. 2
- 2A. A pilot in an aerobatic aircraft performs a loop in 20s at a steady velocity of 100m/s. His seat is located 5m ahead of, and 1m above the CG. What total normal load factor does he experience at the top and at the bottom of the loop? 5
- 2B. Consider the situation when an aircraft is flying in a steady level coordinated turn at a speed of 250m/s at a bank angle of  $60^\circ$ . The force acting on the aircraft are shown in Fig. Q2B. Calculate the turn rate  $\dot{\psi}$ , the yaw rate  $\dot{r}$  and the pitch rate  $\dot{q}$ . 3
- 2C. Illustrate Euler angles and aircraft attitude with neat diagram 2
- 3A. Derive generalized force equations for a rigid body. 5
- 3B. Obtain generalized moment equations for an aircraft. 5
- 4A. Using Cramer's rule, obtain the elevator response transfer function models  $\left(\frac{u(s)}{\eta(s)}, \frac{w(s)}{\eta(s)} \text{ and } \frac{\theta(s)}{\eta(s)}\right)$  from the following equations of longitudinal symmetric motion for aircraft system 5

$$m\dot{u} - F_{x_u}^\circ u - F_{x_w}^\circ \dot{w} - F_{x_w}^\circ w - \left(F_{x_q}^\circ - mW_e\right)q + mg\theta \cos \theta_e = F_{x_\eta}^\circ \eta + F_{x_\tau}^\circ \tau$$

$$-F_{z_u}^\circ u + (m - F_{z_w}^\circ)\dot{w} - F_{z_w}^\circ w - \left(F_{z_q}^\circ + mU_e\right)q + mg\theta \sin \theta_e = F_{z_\eta}^\circ \eta + F_{z_\tau}^\circ \tau$$

$$-M_u^\circ u - M_w^\circ \dot{w} - M_w^\circ w + I_y \dot{q} - M_q^\circ q = M_\eta^\circ \eta + M_\tau^\circ \tau$$

$$\dot{\theta} = q$$

Notations are standard and provide specific meaning for aircraft system.
- 4B. Using Taylor series, deduce the aerodynamic force and moment terms in axial force equation and moment equation respectively for aircraft system. 3
- 4C. Write the expression of aerodynamic control derivatives due to elevator, aileron and rudder deflections. 2
- 5A. Derive the state space and transfer function models for 3 DOF helicopter system. 5

- 5B. Write Euler's equation of motion for the missile systems. Also, deduce the state space equations for the motion variables 3
- 5C. Illustrate control surface  $(\xi, \eta, \zeta)$  convention for the missile system using neat diagram. 2

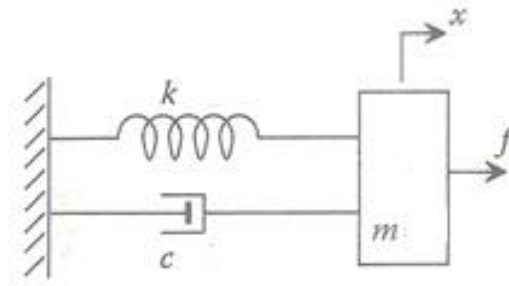


Fig. Q1A

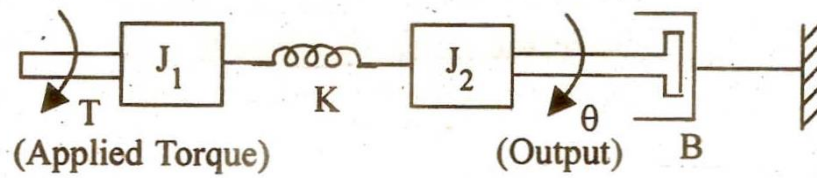


Fig. Q1B

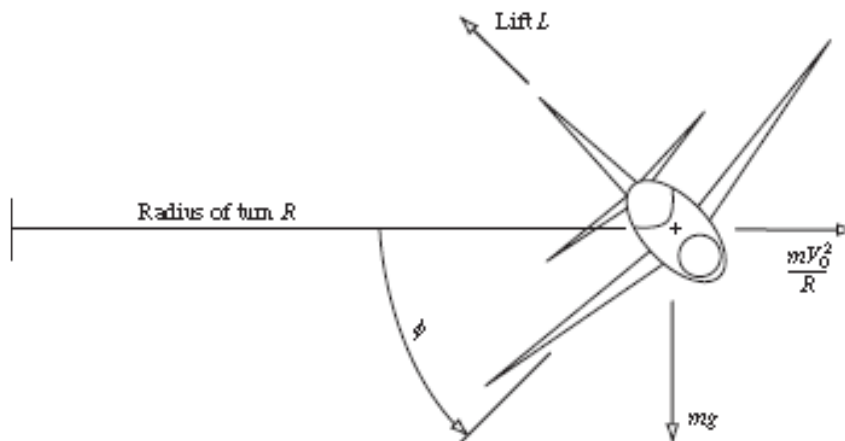


Fig. Q2B

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