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MANIPAL INSTITUTE OF TECHNOLOGY Manipal University



## FIFTH SEMESTER B.TECH (E & C) DEGREE END SEMESTER EXAMINATION - NOV/DEC 2016 SUBJECT: DIGITAL SIGNAL PROCESSING (ECE - 303)

## TIME: 3 HOURS Instructions to candidates

MAX. MARKS: 50

- Answer **ANY FIVE** full questions.
  - Missing data may be suitably assumed.
- 1A. Define unilateral z-transform. Using unilateral z-transform, compute y(n) for  $n \ge 0$  for y(n) y(n-1) y(n-2) = 0; y(-1) = 0 and y(-2) = 1
- 1B. Impulse response of certain causal LTI system is  $h[n] = \{1, 1\}$ . Determine the response of the system

for the periodic input  $x[n] = 5 - 2\cos(\frac{\pi}{2}n) + 10\sin(\frac{3\pi}{2}n)$ .

1C. Draw the magnitude response and z-domain pole-zero plot for the system  $h(n) = 2\delta(n+1) + \delta(n) + 2\delta(n-1)$ 

(5+3+2)

- 2A. Derive radix-2 DIT FFT algorithm. Illustrate with signal flow diagram.
- 2B. For a given real sequence x (n) = $\delta$  (n+1) + $2\delta$  (n) + $\delta$  (n-1). Compute the sequence y (n) if Y (K) = X<sup>2</sup>(K), where X(K) is the 4 point DFT of x(n).
- 2C. State periodicity and circular convolution property of DFT.

(5+3+2)

- 3A. With relevant mathematical analysis, describe overlap-add method of linear filtering through DFT-IDFT calculations.
- 3B. Deduce second order Goertzel filter for the computation of N-point DFT.
- 3C. Define group delay. What is the group delay for N-length linear phase FIR filter?

(5+3+2)

- 4A. Using bilinear transformation method, design third order digital Butterworth Low pass filter. The filter has 3-dB frequency of 500 Hz at sampling frequency of 5000 Hz.
- 4B. Explain impulse invariant method of digitising analog filter.
- 4C. Suggest the location of zeros of system function H(z) for a notch filter to suppress 100Hz signal. Assume sampling frequency of 1kHz.

(5+3+2)

- 5A. Compute the coefficients of 11-length digital linear phase FIR high-pass filter with cut-off frequency of 1kHz at sampling frequency of 5kHz. Use causal Hamming window.
- 5B. For N-length FIR filter having impulse response h[n], prove that the system function  $H(k) = \int_{N} \sum_{k=1}^{N-1} H[k]/N$

$$H(z) = (1 - z^{-N}) \sum_{k=0}^{N} \frac{H(K)/N}{1 - e^{j\frac{2\pi k}{N}} z^{-1}} \text{ where } H(K) \text{ are the DFT coefficients of } h(n).$$

5C. Mention the basic building blocks for implementing digital filter system function.

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6A. Realise the following IIR filter using direct forms 1 and 2 and cascade structures.

$$H(z) = \frac{(1+2z^{-1})}{(1-0.25z^{-1})(1-2z^{-1}+3z^{-2})}$$

- 6B. Describe Welch method of PSD estimation.
- 6C. Bring out two major differences between parametric and non- parametric methods of PSD estimation.

(5+3+2)

(5+3+2)