

Reg. No.



# MANIPAL INSTITUTE OF TECHNOLOGY

MANIPAL

A Constituent Institution of Manipal University

## IV SEMESTER B.TECH. (EEE/ICE)

### END SEMESTER EXAMINATIONS, APR/MAY 2017

### SUBJECT: ENGINEERING MATHEMATICS [MAT 2208]

#### REVISED CREDIT SYSTEM

(12/06/2017)

Time: 3 Hours

MAX. MARKS: 50

#### Instructions to Candidates:

- ❖ Answer **ALL** the questions.
- ❖ Missing data may be suitable assumed.

1A.	Two coins $C_1$ and $C_2$ have the probabilities of falling heads $P_1$ and $P_2$ respectively. You win a bet if in three tosses you get at least 2 heads in succession. You toss the coin alternatively, starting with either coin. If $P_1 > P_2$ , what coin would you select to start the game?	4
1B.	Given $Z\{u_n\} = \frac{z}{z-1} + \frac{z}{z^2+1}$ , find $Z\{u_{n+2}\}$ .	3
1C.	If $\bar{X}$ is the mean of a random sample from a normal distribution with mean $\mu$ and variance 100, find "n" such that $P(\mu - 5 < \bar{X} < \mu + 5) = 0.954$ .	3
2A.	If the joint pdf of X and Y is given by $f(x, y) = \begin{cases} \frac{e^{- y }}{2}, & y >  x  \\ 0, & \text{elsewhere} \end{cases}$ . Find the co-relation co-efficient between X and Y.	4
2B.	Companies A, B, C produce 30%, 45% and 25% of cars respectively. It is known that 2%, 5% and 2% of cars produced by A, B and C are defective. If a car is purchased and found to be defective, what is the probability that this car is produced by company A?	3
2C.	Solve $y'' + xy = 0$ with $y(0) = 0$ , $y'(1) = 1$ , for $n=2$ .	3



<b>3A.</b>	<p>(i) The mean weight of 500 male students at a certain college is 151 lb and the standard deviation is 15 lb. Assuming that the weights are normally distributed find how many students weigh more than 185 lb?</p> <p>(ii) In a book of 520 pages, 390-typo graphical errors occur. Assuming Poisson law for the number of errors per page, find the probability that a random sample of 5 pages will contain no error.</p>	<b>4</b>
<b>3B.</b>	<p>A random variable X has <math>p(x) = \frac{c}{2^x}</math>, <math>x=1,2,3,\dots</math></p> <p>(i) Find c</p> <p>(ii) Find P(X is even)</p> <p>(iii) Calculate P(X is divisible by 3)</p>	<b>3</b>
<b>3C.</b>	Using Z transforms, solve $y_{n+2} - 5y_{n+1} + 6y_n = 1$ with $y_0 = 0, y_1 = 1$ .	<b>3</b>
<b>4A.</b>	<p>Solve Laplace equation with <math>h=1</math>, for <math>0 &lt; x &lt; 4</math>, <math>0 &lt; y &lt; 4</math>, <math>u(x,0) = x^2 + 2x</math>,  <math>u(x,4) = x^2 + 2x - 24</math>, <math>u(0,y) = -2y - y^2</math>, <math>u(4,y) = 24 - y^2 - 2y</math>.</p>	<b>4</b>
<b>4B.</b>	Suppose that the continuous two dimensional random variable (X, Y) is uniformly distributed over the square whose vertices are (1,0), (0,1), (-1,0) and (0,-1). Find the marginal pdf's of X and Y.	<b>3</b>
<b>4C.</b>	Find the mgf of Chi-square distribution and hence find the variance.	<b>3</b>
<b>5A.</b>	Solve $y_{n+2} - 2y_{n+1} + 2y_n = 2^n + \cos \frac{n\pi}{2}$	<b>4</b>
<b>5B.</b>	<p>Solve by Crank –Nicolson's scheme: <math>\frac{\partial u}{\partial t} = \frac{1}{16} \frac{\partial^2 u}{\partial x^2}</math>, <math>0 &lt; x &lt; 1</math>, <math>t \geq 0</math>, <math>u(x,0) = 0</math>,  <math>u(0,t) = 0</math>, <math>u(1,t) = 100t</math>. Compute u for one step with <math>h = \frac{1}{4}</math>.</p>	<b>3</b>
<b>5C.</b>	Suppose that X is uniformly distributed over (1, 3). Obtain the pdf of $Y=3X+4$ .	<b>3</b>

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