Reg. No.



# MANIPAL INSTITUTE OF TECHNOLOGY

A Constituent Institution of Manipal University

## SECOND SEMESTER M.TECH. (AEROSPACE ENGINEERING)

### END SEMESTER EXAMINATIONS, MAY/JUNE 2017

## SUBJECT: FLIGHT MECHANICS [ICE 5202]

Time: 3 Hours

#### MAX. MARKS: 50

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#### **Instructions to Candidates:**

- ✤ Answer ALL the questions.
- ✤ Missing data may be suitably assumed.
- 1A. Derive the moment equations for aircraft motion in the body axis system.
- 1B. Express all forces (namely weight, aerodynamic and thrust forces) acting on aircraft in its most convenient axis system. Consider the aircraft model T-37 at the following Euler angles:

$$\psi = 90 \ deg, \qquad \theta = 10 \ deg, \qquad \phi = 10 \ deg$$

Describe the aircraft attitude and transform the weight force through these angles to the body axis system. The gross weight is **6600 lbf**.

- Illustrate the axis transformation for a vector in the stability axis system into the body 2 axis system.
- 2A. Derive Breguet range equation. A T-37 aircraft model at 20000 ft. has a drag polar 5  $C_D = 0.02 + 0.057C_L^2$  and  $S = 184 ft^2$ . The aircraft has an initial weight of 6000 lb. and 500 lb. of usable fuel. If the TSFC at sea level is 0.9/h, determine the max range for the T-37 at 20000 ft. using constant altitude cruise and a cruise climb.
- 2B. Find the expression for turn rate and turn radius in the pull-ups case for the aircraft level flight. An F-22 is performing a 5-g pull-up at 10000 ft. and 500 kn. true airspeed. What is the turn rate and turn radius?
- 2C. Sketch a thrust required curve and a power required curve, and show where  $\left(\frac{L}{D}\right)_{max}$  2 occurs on each curve.
- 3A. Using the average acceleration method, find the max power takeoff ground roll with no wind and a zero-runway slope for a 12000 lb. T-38 at sea level and 6000 ft. given the following conditions:

 $S = 170 ft^2$ ,  $C_{L_{max}} = 0.88$ ,  $\mu_r = 0.025$ ,  $C_{D_0} = 0.02$ , K = 0.2,  $\rho = 0.00238$ ,  $a_{SL} = 1116.4$ ,  $T_{avg} = 6000 lb$ .

- 3B. Derive the expression to estimate the landing ground roll during the period of wheel 3 braking.
- **3C.** A **T-37** aircraft model has a drag polar  $C_D = 0.02 + 0.057C_L^2$ . Find its max glide 2 ratio and max glide range from 20000 ft. to sea level.
- 4A. Find the expression for aircraft aerodynamic center. Consider the aircraft model A-10 5 with the followings parameters:  $S = 506 ft^2$ ,  $S_h = 120 ft^2$ ,  $\eta_h \approx 0.9$ , AR = 6.54,  $AR_h = 3$ ,  $\frac{d\epsilon}{da} \approx 0.1$ ,  $\bar{c} = 8.8 ft$ ,  $x_{AC_h} = 26.25 ft$ ,  $\bar{x}_{AC_{wf}} \approx 0.25$ ,  $C_{l_{\alpha}} =$

**0.11**,  $\overline{x}_{cg} = 0.5$ . Determine the static margin  $C_{m_{\alpha}}$  and  $C_{m_{c_{1}}}$ . Is the aircraft statically stable in pitch?

- Determine the aileron and rudder deflections required for an F-15 aircraft model to **4B**. 3 maintain a +1 degree wings level sideslip at 0.9 Mach and 20000 ft. Also determine the value of the side-force coefficient under these conditions. Applicable derivatives are as follow:  $C_{y_0} = 0$ ,  $C_{y_\beta} = -0.\frac{9056}{rad}$ ,  $C_{y_{\delta_\alpha}} = -0.\frac{0047}{rad}$ ,  $C_{y_{\delta_r}} = 0.1492/rad$ ,  $C_{l_0} = 0$ ,  $C_{l_\beta} = -0.0732/rad$ ,  $C_{l_{\delta_\alpha}} = 0.0226/rad$ ,  $C_{l_{\delta_r}} = 0.0029/rad$ ,  $C_{n_0} = 0$ ,  $C_{n_\beta} = 0.1638/rad$ ,  $C_{n_{\delta_\alpha}} = 0.0026/rad$ ,  $C_{n_{\delta_r}} = -0.0712/rad$ rad.
- What are the two requirements for the longitudinal static stability? **4C.**
- 5A. The transfer function for an aircraft model T-37 at 30000 ft. and 0.46 Mach is given 5 by

$$\frac{\alpha}{\delta_e} = -0.0924 \frac{(s+336.1)(s^2+0.0105s+0.0097)}{(s^2+4.58s+21.6)(s^2+0.0098s+0.0087)}$$

Find the natural frequency, damping ratio, damped frequency and time constant for the short period and phugoid modes.

Find the transfer function  $\frac{\phi(s)}{\delta_a(s)}$  for the following simplified differential equation **5B.** 3 defining roll response of the aircraft.

$$\ddot{\phi} + 0.704 \, \dot{\phi} = 0.037 \delta_a$$

Assume zero initial conditions. Also obtain time response  $\phi(t)$ .

Write a note on short period mode and phugoid mode. 5C.

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