

Reg. No.



MANIPAL INSTITUTE OF TECHNOLOGY

MANIPAL

A Constituent Institution of Manipal University

I SEMESTER M.TECH. (CHEMICAL & BIOTECHNOLOGY)

END SEMESTER EXAMINATIONS, NOV/DEC 2017

**SUBJECT: MATHEMATICAL & NUMERICAL TECHNIQUES FOR
CHEMICAL AND BIOTECHNOLOGY ENGINEERING [MAT- 5102]**

REVISED CREDIT SYSTEM

Time: 3 Hours

MAX. MARKS: 50

Instructions to Candidates:

- ❖ Answer **ALL FIVE** questions.
- ❖ Missing data may be suitable assumed.

1A.	Using Jacobi's method, find all the eigen values and the corresponding eigen vectors of the matrix $A = \begin{bmatrix} 2 & \sqrt{2} & 4 \\ \sqrt{2} & 6 & \sqrt{2} \\ 4 & \sqrt{2} & 2 \end{bmatrix}$	4
1B.	Find a real root of the equation $xe^x - 1 = 0$ using Newton- Raphson method. Take $x_0 = 1$. Carryout four iterations.	3
1C.	Solve by Taylor series method, the equation $\frac{dy}{dx} = \log(xy)$ for $y(1.1)$ and $y(1.2)$, given $y(1) = 2$.	3
2A.	Consider the boundary value problem $y'' + (1+x^2)y = -1$, $y(\pm 1) = 0$. Determine the coefficients of the approximate solution $w(x) = a_1(1-x^2) + a_2x^2(1-x^2)$ by using Galerkin method.	4
2B.	Solve the following system of equations using Gauss-Seidel method. $4x + y - z = 3$, $2x + 7y + z = 19$, $x - 3y + 12z = 31$. Carryout three iterations.	3
2C.	Find the seventh term and general term of the series 3, 9, 20, 38, 65,... using interpolation.	3
3A.	Using Runge-Kutta method of order four find $y(0.3)$ and $z(0.3)$ from	4



	$\therefore \frac{dy}{dx}=1+xz, \frac{dz}{dx}=-xy$ with $y(0) = 0$ and $z(0) = 1..$													
3B.	Find the largest eigen value and the corresponding eigen vector of $A=\begin{bmatrix} 1 & 6 & 1 \\ 1 & 2 & 0 \\ 0 & 0 & 3 \end{bmatrix}$ by power method taking $X^{(0)}=[1 \ 0 \ 0]^T$. Carryout four iterations	3												
3C	Find the quadratic least square approximation to $f(x) = e^x, x \in [-1, 1]$ with respect to the weight function $w(x) = 1$.	3												
4A.	Solve $y''+(1+x)y'-y=0, y(0)=y'(0), y(1)+y'(1)=1, h=\frac{1}{2}$	4												
4B.	Prove that $\int_0^\infty e^{-x} L_n(x) L_m(x) dx = \begin{cases} 0, & m \neq n \\ 1, & m = n \end{cases}$	3												
4C.	Fit the exponential curve $y = ae^{bx}$ to the following data <table><tr><td>x</td><td>2</td><td>4</td><td>6</td><td>8</td><td>10</td></tr><tr><td>y</td><td>4.077</td><td>11.084</td><td>30.128</td><td>81.897</td><td>222.62</td></tr></table>	x	2	4	6	8	10	y	4.077	11.084	30.128	81.897	222.62	3
x	2	4	6	8	10									
y	4.077	11.084	30.128	81.897	222.62									
5A.	Find the Fourier transform of $f(x) = \begin{cases} a^2 - x^2, & x < a \\ 0, & x > a \end{cases}$ and hence deduce that $\int_0^\infty \left(\frac{\sin t - t \cos t}{t^3} \right) dt = \frac{\pi}{4}$.	4												
5B.	Solve: $2x+3y+z=9; x+2y+3z=6; 3x+y+2z=8$ by LU decomposition method.	3												
5C.	Solve: $\frac{\partial^2 u}{\partial t^2}=16\frac{\partial^2 u}{\partial x^2}, 0 < x < 5, t > 0. u(x,0) = x^2(5-x), \frac{\partial u(x,0)}{\partial t}=0, u(0, t) = 0 = u(5, t). h = 1$. Compute $u(x,t)$ for 4 time steps.	3												