

FIRST SEMESTER M.TECH. (AEROSPACE ENGINEERING)

END SEMESTER EXAMINATIONS, DEC - 2017

SUBJECT: ADVANCED CONTROL SYSTEMS [ICE 5102]

Duration: 3 Hour

Max. Marks:50

3 7

4

Instructions to Candidates:

- ✤ Answer ALL the questions.
- Missing data may be suitably assumed.
- 1A Compare the properties of Lag compensator with that of Lead compensator
- **1B** Given the open loop transfer function of a continuous time system

 $G(s) = \frac{K}{s(s+3)(s+6)}$. Design a phase lead compensator using Root locus approach to achieve the

desired damping ratio of 0.4 and undamped natural frequency of 4r/s. Also the system should exhibit static velocity error constant of 5 /sec.

- 2A The frequency response of open loop transfer function with gain adjustment for steady state error 4 requirement is shown in Fig. (Q2A). Design a phase lag compensator to meet the desired phase margin of 45⁰.
- **2B** Explain with neat block diagram a typical digitally controlled system. Also mention the 3 advantages of discrete system analysis.
- **2C** Derive the expression for steady state error due to step, ramp and parabolic input for a unity 3 feedback discrete time system having forward path with a plant $G_p(s)$ preceded by a sampler and ZOH.
- **3A** Find the response y[k] for a system described by the difference equation

y[k+2]+y[k+1]+0.16y[k]=x[n+1]+0.32x[n], for the input $x(z)=\frac{z}{z+0.5}$, assuming all initial

conditions as zero.

3B A sampled data control system has its characteristic equation given by $F(z)=z^4-1.4z^3+0.4z^{2+}0.1z+0.002=0$. Determine stability of the system using Jury's stability test.

► Y(s)

 $G_2(s)$

δτ

Fig. Q3C

Derive the pulse transfer function $\frac{Y(Z)}{R(z)}$ for the discrete time system shown in Fig. Q3C.

 $G_1(s)$

H(s)

 δ_{T}

4A Consider the system $G(s) = \frac{s^2 - 4}{(s - 2)(2s^2 + 3s + 1)}$. Comment on its controllability and observability. Give reason. Obtain the minimal realization of the system in controllable canonical form.

4B Given the system description $\dot{x}(t) = \begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix} x(t)$. Determine the unforced system response for an 4

arbitrary initial condition of x(0). Derive the transfer function for

$$\dot{x}(t) = \begin{bmatrix} -6 & -1 \\ 5 & 0 \end{bmatrix} x + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u; \quad y = x_1$$
Consider the continuous time system described by

5A

 $\dot{x}(t) = \begin{bmatrix} -2 & 2 \\ 1 & -3 \end{bmatrix} x + \begin{bmatrix} -1 \\ 5 \end{bmatrix} u; \quad y = \begin{bmatrix} 2 & -4 \end{bmatrix} x + 6u(t).$ Obtain equivalent discrete time model, when the sampling time is T=0.2s

Consider the system $x(t) = \begin{bmatrix} 0 & 1 \\ 20.6 & 0 \end{bmatrix} x + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u$. Design a state feedback control law to place the **5B** closed loop poles at -1.8±j2.4. Verify the result by using Ackerman's formula.

10 Frequency (rad/sec) Fig. Q2A



4C

R(s)

3

5

3

5