

MANIPAL INSTITUTE OF TECHNOLOGY

## FIRST SEMESTER M.TECH. (AEROSPACE AND CONTROL SYSTEMS) END SEMESTER EXAMINATIONS, NOV - 2017

ADVANCED CONTROL SYSTEMS [ICE 5102]

Duration: 3 Hour

Max. Marks:50

## Instructions to Candidates:

- Answer ALL the questions.
- Missing data may be suitably assumed.
- 1A Compare Lag and Lead compensators in terms of frequency response, pole-zero map and 4 performance.
- 1B The frequency response plot of an open loop system with steady state gain compensation is 6 shown in Fig. Q1C. It is desired to design a Lead compensator to meet the specification of phase margin of at least 60°. Design a cascade lead compensator and represent its transfer function.



Fig. Q1C

- **2A** How is the stability criteria of discrete time system be developed from that of continuous time 4 system.
- **2B** Use the root locus concept to design a cascade lag compensator for the system with plant 6 transfer function  $G(s) = \frac{K}{s(s+1)(s+4)}$ , to make the velocity error 0.2, overshoot < 20%.
- **3A** Give an account of selecting sampling time.

Consider the plant transfer function  $G_p(s) = \frac{e^{-2s}}{s+1}$  preceded by a ZOH. Obtain its pulse transfer

**3B** 

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function and discrete time unit step response. Consider the sampling time as 0.2.

**3C** Transform the following continuous time state equation to a discrete time system, for a 5 sampling time of 0.1 secs.

 $\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -3 & -4 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u; \quad y = \begin{bmatrix} 3 & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}.$  Hence determine the pulse transfer function and

the stability of discrete time system.

**4A** For the system shown in Fig. Q4A, obtain the closed loop pulse transfer function.



- **4B** For the pulse transfer function obtained in Q(3B), transform the transfer function to W-plane. In 3 which parameters the W-transformed transfer function and original s-domain transfer function are similar? What are the features of the W-transformation function used? Also mention the significance of W-transfer function.
  - **4C** For the following state equations, determine i) state transition matrix by both the methods 5 ii) Hence determine the time domain output of the system for a unit step input, with zero initial conditions.

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} -8 & 6 \\ -6 & 4 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 4 \\ -6 \end{bmatrix} u; \quad y = \begin{bmatrix} 1 & -1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$$

5A Obtain the state space representation of the following system in

Diagonal form

$$\frac{Y(s)}{U(s)} = \frac{2(s+3)}{(s+1)(s+2)}$$

**5B** 

For the matrix  $A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -24 & -26 & -9 \end{bmatrix}$  determine

- i) Eigen Values
- ii) Transformation matrix which transforms it into diagonal form
- iii) Obtain the diagonal form of A
- **5C** Define controllability and observability. Find a suitable transformation matrix which transforms 5 given system into controllable canonical form. Also determine the feedback gain matrix which places the closed loop poles of the system at  $s=-5\pm j5$ . Verify the result by Ackerman's formula.

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} 0 & 2 \\ -1 & -3 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u;$$

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