Reg. No.

MANIPAL INSTITUTE OF TECHNOLOGY

LIFE A Constituent Institution of Manipal University

FIFTH SEMESTER B.Tech. (E & C) DEGREE END SEMESTER EXAMINATION NOV/DEC 2017

SUBJECT: LINEAR AND DIGITAL CONTROL SYSTEMS (ECE - 3101)

TIME: 3 HOURS

MAX. MARKS: 50

Instructions to candidates

- Answer **ALL** questions.
- Missing data may be suitably assumed.
- Centimeter and semilog graph sheets will be supplied
- The closed loop transfer function of a system is $\frac{C(s)}{R(s)} = \frac{100}{s^6 + 3s^5 + 8s^4 + 18s^3 + 20s^2 + 24s + 16}$. 1A. Determine the number of poles on right hand side, left hand side and on the j ω axis. Comment on the stability of the system. Explain the time domain specifications of a second order system with suitable sketches. 1B. 1C. A negative unity feedback system has open-loop transfer function $G(s) = \frac{4}{s(s+4)}$. The nature of the step response is -----a) Underdamped b) Over damped c) critically damped d) oscillatory. (5+3+2)Obtain the differential equation governing the motion of the mechanical system and write the state 2A. equations for a mechanical system shown in figure (2A). Derive the expression for resonant frequency and magnitude of a second order system. 2B. 2C. A unity feedback system has forward- path transfer function $G(s) = \frac{25}{s(s+6)}$. The resonant peak of the closed loop frequency response is -----a) 1.012 b) 1.122 c) 1.032 d) 1.042. (5+3+2)
- ^{3A.} A closed loop sampled data system whose open lop transfer function $\frac{5}{s(s+2)}$ is sampled at the error signal with sampling period of 0.4 sec. Find the characteristic polynomial in the z-domain and

ascertain its stability through Bilinear transformation.

- 3B. For a lag-lead controller obtain the expression for the transfer function.
- 3C. The transfer function Y(s)/X(s) for a system with a signal flow graph as shown in figure (3C) is ----

a)
$$\frac{s+2}{s(s+1)}$$
 b) $\frac{s+2}{s-1}$ c) $\frac{s+2}{s(s-1)}$ d) $\frac{s+2}{s+1}$
(5+3+2)

4A. If $A = \begin{bmatrix} -2 & 0 \\ 0 & -3 \end{bmatrix}$, find state transition matrix using e^{At} (power series method). Verify the result by

Laplace transform method and also find the inverse state transition matrix.

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- 4B. Discuss why transportation lag is important in control systems. How it is modelled mathematically?
- 4C. The pulse transfer function for a process with zero order hold is given by $GH(z) = \frac{Z^{-2}(0.6 + 0.5Z^{-1})}{4 - 3Z^{-1}}$ Write the difference equation for implementing DDC using Kalman's

method.

(5+3+2)

- 5A. The open loop transfer function of the uncompensated system is $G(s) = \frac{K}{s(s+2)}$. Design a suitable phase lag compensator for the system so that the static velocity error constant is 20 sec⁻¹ and phase margin is at least 55⁰.
- 5B. Derive an expression for a controller D(z) that will achieve dead beat control of a process of transfer function G(s).
- 5C. State and prove the properties of state transition matrix.

(5+3+2)



Figure (3C)