

FIFTH SEMESTER B.TECH. (INSTRUMENTATION AND CONTROL ENGG.) END SEMESTER EXAMINATIONS, NOV - 2017

SUBJECT: MODERN CONTROL THEORY [ICE 3101]

Duration: 3 Hour

Instructions to Candidates:

- Answer ALL the questions.
- Missing data may be suitably assumed.
- **1A** State any two properties of state transition matrix.
- **1B** For the electrical system shown in Fig (Q1B) select minimal state variables and find the **3** state model in physical variable form. Take $V_o(t)$ as the output.



Fig (Q1B)

- **1C** Diagonalize the system matrix A given by,
 - $A = \begin{bmatrix} 2 & 0 & 2 \\ 1 & 3 & 1 \\ 1 & 0 & 2 \end{bmatrix}$
- 2A Derive an expression for transfer function from state models
- **2B** Derive the state models for the differential equation $\ddot{y}+6\ddot{y}+3\dot{y}+5y=\ddot{u}+2\dot{u}+7u$ in **3** observable canonical form.
- 2C Without interchanging the blocks, using cascade realization, obtain the state models from 5 the block diagram shown in Figure (Q2C).

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Max. Marks:50

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$$\begin{array}{c|c} \mathbf{R}(s) \\ \hline \\ \hline \\ s+5 \end{array} \end{array} \xrightarrow{\begin{array}{c} s+4 \\ s+3 \end{array}} \begin{array}{c} 5 \\ \hline \\ \hline \\ s+1 \end{array} \xrightarrow{\begin{array}{c} 5 \\ s+1 \end{array}} \begin{array}{c} Y(s) \\ \hline \\ \hline \end{array}$$

3A Find the Z transform of sin ωt

3B Find the inverse Z transform of G(s) =
$$\frac{s}{(s+1)^2(s+2)}$$
 3

- 3C Solve the state equation $\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u; \quad y = x_1 \text{ Also obtain the step response of the system.}$
- **4**A Check the sign definiteness of the following scalar functions

i)
$$V(x) = 2x_1^2 + 2x_2^2 + 2x_3^2 + 6x_1x_2 + 4x_2x_3 - 2x_3x_1$$
 ii) $V(x) = x_1^2 + 2x_2^2 + 2x_3^2 + 4x_2 - 2x_2x_3 + 4x_3x_1$

3 **4B** Consider the discrete time state equation described as $x(k+1) = \begin{bmatrix} 0 & 1 \\ -1 & -2 \end{bmatrix} x(k) + \begin{bmatrix} 0 \\ 1 \end{bmatrix} (-1)^k, \ y(k) = \begin{bmatrix} -1 & 1 \end{bmatrix} x(k) \text{ where } x(0) = \begin{bmatrix} 1 \\ 1 \end{bmatrix}.$ Find the closed form of solution for y(k) where $k \ge 1$.

- **4C** 5 Discretize the continuous time system $\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u; \text{ Take sampling time, T= 1sec.}$ 2
- State stability and instability in the sense of Lyapunov. 5A
- A linear autonomous system is described by the discrete state 5**B** model 3 $x(k+1) = \begin{bmatrix} 0.5 & 1 \\ -1 & -1 \end{bmatrix} x(k)$ Using Lyapunov direct method, determine the stability of the equilibrium state.
- 5C discrete regulator system has the plant 5 $x(k+1) = \begin{bmatrix} 1 & 0.1 \\ 0 & 1 \end{bmatrix} x(k) + \begin{bmatrix} 0.005 \\ 0.1 \end{bmatrix} u(k), \ y(k) = \begin{bmatrix} 1 & 0 \end{bmatrix} x(k)$ Design a state feedback control law such that the response of the closed loop system has the damping ratio= 0.6 and undamped natural frequency, $\omega_n = 8 \text{ rad/sec. Take T} = 1 \text{sec.}$

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