



SEVENTH SEMESTER B.TECH. (INSTRUMENTATION AND CONTROL ENGG.)

END SEMESTER EXAMINATIONS, DEC - 2017

SUBJECT: DIGITAL CONTROL SYSTEMS [ICE 4102]

Duration: 3 Hour

Max. Marks:50

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Instructions to Candidates:

- ✤ Answer ALL the questions.
- ✤ Missing data may be suitably assumed.
- 1A State Sampling theorem. With necessary frequency responses, illustrate sampling theorem.
- **1B** Obtain the expression for Y(z) for the system shown in Fig. Q1B considering the input as unit step function.



Fig. Q1B

- 2A Explain the transformation necessary to use the Routh stability test for determining stability of discrete time systems.
- **2B** Given the characteristic equation of a discrete time system $F(z)=z^4+0.6z^3-0.25z^2-0.2z-0.05=0.$

Determine its stability using Jury's stability test.

2C Show that steady state error of a unity feed back discrete time system depends on reference input signal R(z) as well as the forward path transfer function $G(z)=G_{ho}G_{p}(z)$, where G_{ho} represents the

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ZOH. Hence find i) Steady state error due to step input

ii)Steady state error due to Ramp input

iii) Steady state error due to Parabolic input.

- 3A Obtain the pulse transfer function and response of the system described by the difference 3 equation y[n]-0.6y[n-1]-0.16y[n-2]=5x[n], with y(-1)=y(-2)=0 and with $x[n]=\delta[n]$.
- **3B** Realise the following pulse transfer function in ladder form

$$G(z) = \frac{z^2 + 2z + 1}{z^2 + 8z - 1}$$
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- **3**C Obtain the pulse transfer function of a digital PID controller in positional form.
- **4**A Explain the procedure for designing a discrete time PD controller using root locus approach.
- **4B** Consider a unity feedback discrete time system having forward path with a ZOH and a continuous plant $G_p(s) = \frac{1}{s(s+1)}$. Design a digital lead compensator D(z) for the system to meet the following specifications:

- The velocity error constant $K_v = 7.5/sec$. i)
- ii) The peak overshoot M_p to step input is $\leq 15\%$
- Settling time $T_s(2\%$ tolerance band) ≤ 5 sec iii)

Use Root locus method. Consider the sampling time as T=1sec

- 5A Consider the forward path of a unity feedback discrete time system having a ZOH and a continuous plant $G_p(s) = \frac{1}{s(s+1)}$. Determine its W-transfer function. Compare it with continuous 3 plant transfer function and comment on observations. Let the sampling time be T=1s.
- **5B** Bode plot of W transformed function with steady state gain adjustment is shown in Fig. Q5B vs. fictitious frequency γ . From the plot design a phase lag compensator to achieve a desired phase margin of 40°. Hence derive the pulse transfer function of the controller and represent it in the difference equation form. Assume a sampling time of T=1sec. 7

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Fig. Q5B