

# Question Paper

Exam Date & Time: 28-Apr-2018 (09:30 AM - 12:30 PM)



**MANIPAL ACADEMY OF HIGHER EDUCATION**  
**INTERNATIONAL CENTRE FOR APPLIED SCIENCES**  
**IV SEMESTER B.S.(ENGG.)**  
**END - SEMESTER THEORY EXAMINATIONS APRIL-2018**

**DATE : 28.04.2018**  
**TIME : 9:30AM - 12:30PM**  
**Signal Processing [EC 244A]**

**Marks: 100**

**Duration: 180 mins.**

**Answer 5 out of 8 questions.**

- 1) (10)  
A) The system given below have input  $x[n]$  and output  $y[n]$ , respectively. Determine whether each of them is memory less, stable, causal, linear and time in-variant

i.  $y[n] = \log_{10}(|x[n]|)$

ii.  $y[n] = x[n] \sum_{k=-\infty}^{\infty} \delta[n-2k]$

- B) (10)  
Determine the even and odd component of the signal  $x(t)$  as shown in Fig. 1B

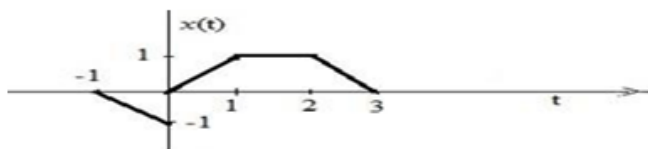


Fig. 1B

- 2) (10)  
A) Let input to the LTI system with impulse response  $h[n] = \alpha^n \{u[n-2] - u[n-13]\}$  be  $x[n] = 2\{u[n+2] - u[n-12]\}$ . Compute the output  $y[n]$  using convolution.

- B) (10)  
State and explain the following properties for the Fourier transform representation.  
i. Time and Frequency shifting  
ii. Convolution and Modulation

- 3) (10)  
A)

Certain LTI system has input  $x[n] = \left(\frac{1}{2}\right)^n u[n] - \left(\frac{1}{2}\right)^{n-1} u[n-1]$  and has the response  $y[n] = \left(\frac{1}{2}\right)^n u[n]$ .

Obtain the frequency response and the impulse response of the system. Also write the difference equation representation of the system.

- B) (10)

Determine whether the following systems are causal and stable

i.  $H(z) = \frac{2z+3}{z^2+z-\frac{5}{16}}$

ii.  $y[n] - 2y[n-2] = x[n] - \frac{1}{2}x[n-1]$

- 4) An LTI system has impulse response  $h(t) = 2 \cos(6\pi t) \frac{\sin(\pi t)}{\pi t}$ . Using Fourier transform, (10)

A) determine the output if the input is  $x(t) = 5 + \sin(\pi t) + \cos(6\pi t)$ .

- B) Suppose the input  $x(t)$  and the impulse response  $h(t)$  of a LTI system is given (10)  
by  $x(t) = u(t+2) - u(t-2)$  and  $h(t) = u(t-3) - u(t-10)$ . Use convolution integral to evaluate the output  $y(t)$  of the LTI system. Sketch the output  $y(t)$

- 5) Sketch the waveform for the following signal (10)

A) i.  $x(t) = r(t+1) - r(t) + r(t-2)$

ii.  $x(t) = -u(t+3) + 2u(t+1) - 2u(t-1) + u(t-3)$

Where  $r(t)$  is the unit ramp and  $u(t)$  is the unit step function.

- B) Draw the frequency response of the following ideal digital filters (10)

i. Low-pass

ii. High - pass

iii. Band - pass

- 6) Determine the transfer function and difference equation representation of the system (10)  
with the following impulse response

A)  $h[n] = \left(\frac{1}{3}\right)^n u[n] + \left(\frac{1}{2}\right)^{n-2} u[n-1]$

- B) (10)

A LTI system is described  $\frac{d^2 y(t)}{dt^2} + 3 \frac{dy(t)}{dt} + 2y(t) = 2 \frac{dx(t)}{dt} + x(t)$ . Determine

i. Frequency response

ii. Impulse response of the system

iii. Output of the system for the input  $x(t) = e^{-3t} u(t)$

- 7) Draw the DF-1 and DF-II structures for an LTI system represented by the following (10)  
differential/difference equation.

A)

i.  $y[n] + 1.2y[n-1] - \frac{1}{8}y[n-2] = 2x[n] + x[n-1]$

ii.  $3y(t) + 6 \frac{dy(t)}{dt} + \frac{d^3 y(t)}{dt^3} = 2x(t) + 3 \frac{dx(t)}{dt}$

- B) Compare IIR and FIR filters. (10)

- 8) (10)

A)

Consider the LTI system described by the difference equation

- B)  $7y[n] = x[n] + x[n-1] + x[n-2] + x[n-3] + x[n-4]$  Compute the 8 point DFT of sequence  $x[n] = \{1 \ 1 \ 1 \ 1 \ 0 \ 0 \ 0 \ 0\}$ . (10)

Determine the system function and the impulse response. Draw the pole zero plot and hence comment on the stability and causality of the system.

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