


**IV SEMESTER B.TECH. (COMPUTER SCIENCE AND ENGINEERING)**
**END SEMESTER EXAMINATIONS, APRIL 2018**
**SUBJECT: FORMAL LANGUAGES AND AUTOMATA THEORY [CSE 2201]**
**REVISED CREDIT SYSTEM**

(17/04/2018)

Time: 3 Hours

MAX. MARKS: 50

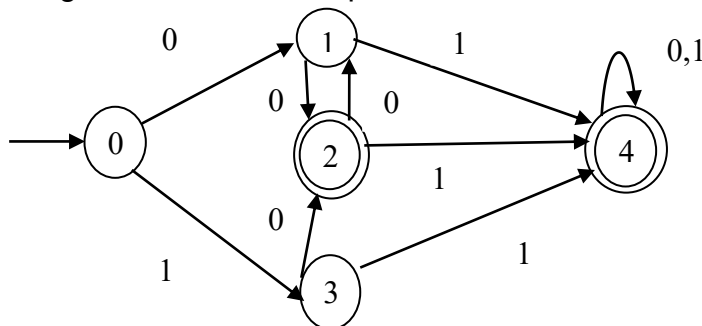
**Instructions to Candidates:**

- ❖ Answer **ALL** the questions.
- ❖ Missing data may be suitably assumed.

**1A.** Give a grammar that generates all real constants in **C++**. **3M**

**1B.** Let  $\Sigma = \{a, b\}$ , find a DFA with **3** states for accepting the language **3M**  
 $L = \{w : (n_a(w) + 2n_b(w)) \bmod 3 < 2\}$

**1C.** Using **mark** and **reduce** procedure, minimize the DFA in **Figure 1C**.


**Figure 1C**
**4M**

**2A.** Find a regular expression for the language **5M**  
 $L = \{w \in \{a, b\}^* : n_a(w) \text{ and } n_b(w) \text{ are both even}\}$  using **nfa-to-regex** procedure.

**2B.** Let  $L_1 = L(0^*10^*)$  and  $L_2 = (10^*1)$ . Design a DFA for  $L_1/L_2$  and then find  $L_1/L_2$ . **2M**

**2C.** Prove that  $L = \{w : w = w^R, w \in \{0, 1\}^*\}$  is not regular using Pumping lemma. **3M**

**3A.** Define ambiguity in context free grammar. Show that the grammar with the following productions:  $E \rightarrow E - E$ ,  $E \rightarrow 0 \mid 1$  is ambiguous. **4M**  
 Construct an equivalent unambiguous grammar.

**3B.** Remove all unit-productions, all useless productions and all  $\lambda$ -productions from the grammar:

$S \rightarrow aCb$   
 $B \rightarrow CD$   
 $C \rightarrow D \mid a \mid \lambda$   
 $D \rightarrow B \mid b \mid \lambda$

**4M**

- 3C.** Define Chomsky normal form and Greibach normal form with an example for each. **2M**
- 4A.** Construct an NPDA with **3** states for  $L = \{w \in \{a, b\}^* : n_a(w) = n_b(w) + 1\}$ . Give instantaneous description (ID) for the string **baaba**. **4M**
- 4B.** Let  $L_1 = \{a^n b^n : n \geq 0\}$  and  $L_2 = \{a^n b^{2n} : n \geq 0\}$  are deterministic context free languages. Design PDA for  $L = L_1 \cup L_2$ . Is  $L$  deterministic? Justify your answer. **3M**
- 4C.** Show that the following language is context-free.  
 $L = \{w \in \{a, b\}^* : n_a(w) = n_b(w), w \text{ does not contain the substring } \mathbf{aab}\}$  **3M**
- 5A.** For  $\Sigma = \{ (, ) \}$ , design a Turing machine with **4** states for the language  $L = \{w : w \text{ contains balanced parentheses}\}$ . For example  $(( ))( )$  and  $(( ))$  are balanced parentheses, but  $(( ))($  and  $(( )$  are not. Give ID for the string  $(( ))( )$ . **4M**
- 5B.** Design a linear bounded automata (LBA) with **7** states for the language  $L = \{a^n b^n c^n : n \geq 1\}$  **3M**
- 5C.** (a) Define decidable and undecidable problems. Give an example for each. **3M**  
 (b) Define recursive language. Give an example.

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