Reg. No.

MANIPAL INSTITUTE OF TECHNOLOGY

## THIRD SEMESTER B.TECH. (E & C) DEGREE END SEMESTER EXAMINATION NOVEMBER 2018

## SUBJECT: ELECTROMAGNETIC WAVES (ECE - 2102)

## **TIME: 3 HOURS**

MAX. MARKS: 50

- Instructions to candidatesAnswer ALL questions.
  - Missing data may be suitably assumed.

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- 1A. In a nonmagnetic medium ( $\mu_r = 1$ ) the electric field component is  $\vec{E} = 4 \sin(2\pi \times 10^7 t 0.8x)\vec{a_z}$  V/m, Determine the total power crossing the surface of area 20 cm<sup>2</sup> in the  $\vec{a_x}$  direction.
- 1B. A uniform plane wave propagating through the medium with loss tangent 0.53,  $\varepsilon_r = 8$ ,  $\mu_r = 2$  has  $\vec{E} = 0.5e^{-z/3} \sin(10^8 t \beta z) \vec{a}_x$  V/m, determine  $\beta$  and  $\vec{H}$ .
- 1C. For a good conducting medium having  $\sigma = 58 MS/m$ ,  $\mu_r = 1$  and  $\varepsilon_r = 1$  at a frequency of 100 MHz, calculate the intrinsic impedance ( $\eta$ ), propagation constant ( $\gamma$ ) and skin depth ( $\delta$ ).

(4+3+3)

- 2A. Given  $\vec{E} = E_0 \sin(10^6 t \beta z) \overrightarrow{a_x} V/m$  in free space. Determine wavelength, expressions for  $\vec{D}, \vec{B}$  and  $\vec{H}$  at t = 1µS.
- 2B. (i) Find the distance between two points A (10,  $30^0$ ,  $50^0$ ) and B (7,  $45^0$ ,  $90^0$ ).
  - (ii) The magnetic flux density is given as  $\vec{B} = \frac{4}{\rho} \vec{a_{\phi}}$  T in cylindrical coordinates. Determine the magnetic flux crossing the plane surface defined by  $1m < \rho < 2.5m$ , 0 < z < 2m and  $\phi = \pi/4$ .
- 2C. Derive the modified amperes circuit law for a time varying field.

(4+3+3)

- 3A. Write the expressions for incident wave  $(\overrightarrow{E_{ls}}, \overrightarrow{H_{ls}})$ , reflected wave  $(\overrightarrow{E_{rs}}, \overrightarrow{H_{rs}})$ , and transmitted wave  $(\overrightarrow{E_{ts}}, \overrightarrow{H_{ts}})$ , for a uniform plane wave propagating along positive z direction and incident normally at the boundary z = 0 between two perfect dielectrics. Assume that  $\overrightarrow{E_{ls}}$ ,  $\overrightarrow{E_{rs}}$  and  $\overrightarrow{E_{ts}}$  have polarized along  $\overrightarrow{a_x}$  direction and medium 1 (z < 0), medium 2 (z > 0) are characterised by  $(\varepsilon_1, \mu_0)$  and  $(\varepsilon_2, \mu_0)$  respectively.
- 3B. Use Ampere's circuital law to find the magnetic field intensity  $\vec{H}$  at  $\rho < a$  and at  $a < \rho < b$  for a coaxial cable of length *l* consisting of two concentric cylinders of radius *a* and *b* separated by free space. Assume current I is flowing in  $\vec{a_z}$  direction in inner conductor and  $-\vec{a_z}$  direction in outer conductor.

3C. Derive the expression for total internal reflection.

(4+3+3)

- 4A. The magnetic flux density in free space is given as  $\vec{B} = 0.4 \vec{a_x} + 0.2 \vec{a_y} 0.3 \vec{a_z}$  T. A rectangular loop carrying current of 20 mA in counter clock direction lies in z = 0 plane and is bounded by x=1m, x=3m, y=2m and y=5m. Find the force acting on each segment and hence the total torque acting on the loop.
- <sup>4</sup>B. If magnetic vector potential is  $\vec{A} = -\left(\frac{\rho^2}{4}\right)\vec{a_z}$  A/m, determine the total flux crossing the surface  $\varphi = \pi/2$ ,  $1m \le \rho \le 2m$ ,  $0 \le z \le 5m$ .
- 4C. A circular disk of radius *d* is uniformly charged with surface charge density of  $\rho_s C/m^2$ . The disk lies on the z = 0 plane with its axis along the *z* axis. Determine the expression for electric field intensity  $\vec{E}$  at point (0, 0, h).

(4+3+3)

- 5A. Derive the expression for reflection and transmission coefficient for a uniform plane wave at oblique incidence with  $\vec{E}$  parallel to the plane of incidence.
- 5B. Given that  $\vec{H}_1 = -2\vec{a}_x + 6\vec{a}_y + 4\vec{a}_z A/m$  in region 1 (z > 0) where  $\mu_1 = 5\mu_0$ . If the interface carries current  $\vec{K} = 80 \overrightarrow{a_x} A/m$  on the surface z = 0. Determine  $\vec{H}_2$  and  $\vec{B}_2$  in region 2 (z < 0) filled with  $\mu_2 = 3\mu_0$ .
- 5C. Light is incident from air to glass at Brewster angle. Refractive index of glass is 1.45. Determine the incident and transmitted angles.

$$(4+3+3)$$