MANIPAL INSTITUTE OF TECHNOLOGY

(A constituent unit of MAHE, Manipal)

THIRD SEMESTER B.TECH. (E & C) DEGREE END SEMESTER EXAMINATION DECEMBER 2018/JANUARY 2019 SUBJECT: SIGNALS AND SYSTEMS (ECE - 2104)

TIME: 3 HOURS

MAX. MARKS: 50

Instructions to candidates

- Answer **ALL** questions.
- Missing data may be suitably assumed.
- 1A. Express the signal x(t) shown in **Figure 1A** in terms of step and ramp functions. Also determine and plot Odd and Even parts of x(t)
- 1B. (i) Given $v(t) = \sin(t)u(t)$, state whether the signal x(t) = v(t) + v(-t) is periodic. Justify your statement. Determine period if signal is periodic.
 - (ii) State with justification whether the discrete time system defined by $y[n] = (-2)^n x[|n|]$ is stable, linear, memoryless, causal, invertible

(5+5)

- 2A. Derive the condition for the system that has impulse response h(t) to be (a) memoryless, (b) causal, and (c) stable. Hence State whether the system h(t) = (1/4)(u(t) u(t 4)) is stable, causal and memoryless.
- ^{2B.} (i) Find the step response of a system defined by impulse response $h(t) = e^{-3|t|}$
 - (ii) Draw DF I and DF II for the system defined by differential equation

$$\frac{d^{3}y(t)}{dt^{3}} + 5\frac{d^{3}y(t)}{dt} + 6y(t) = \frac{d^{2}x(t)}{dt^{2}} + \frac{d^{3}x(t)}{dt}$$
(5+5)

- 3A. Determine appropriate Fourier representation of signal $x[n] = 2 + \cos(\frac{\pi}{3}n)$ and plot magnitude and phase function. Compute energy and power as applicable.
- 3B. Using Fourier analysis, determine the output of the LTI system with impulse response: $h(t) = 2\cos(2\pi t)\frac{\sin(\pi t)}{\pi t}$ to the input x (t) = 0.5 + cos(1.5\pi t) + cos (6\pi t)

(5+5)

- 4A. Explain the process of sampling analog signal. Derive the expression for Fourier transform of the sampled signal and hence illustrate sampling theorem through suitable spectral plots.
- 4B. Determine the bilateral Laplace transform of the signal $x(t) = e^{-3t} u(t) + e^{-t} \cos(2t) u(t)$. Plot the poles and zeroes and indicate ROC.

(5+5)

- 5A. State and prove linearity and convolution properties of Z-transform. Discuss the effect on ROC with example.
- 5B. Consider the z-transform $X(z) = \frac{\left(3 \frac{5}{6}z^{-1}\right)}{\left(1 \frac{1}{4}z^{-1}\right)\left(1 \frac{1}{3}z^{-1}\right)}$ Determine the three time domain signals corresponding to this z-transform.

(5+5)

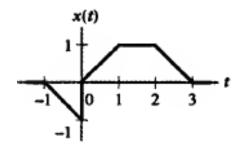


Figure. 1A