



**MANIPAL INSTITUTE OF TECHNOLOGY**  
**MANIPAL**  
(A constituent unit of MAHE, Manipal)

**1<sup>st</sup> SEMESTER M.TECH. (COMPUTER SCIENCE & INFORMATION SECURITY)**

**END SEMISTER EXAMINATIONS, NOV 2018**

**SUBJECT: NUMBER THEORY AND CRYPTOGRAPHY [CSE 5121]**

**REVISED CREDIT SYSTEM**

**(27/11/2018)**

Time: 3 Hours

MAX. MARKS: 50

**Instructions to Candidates:**

- ❖ Answer **ALL** the questions.
- ❖ Missing data may be suitably assumed.

- 1A.** State and prove Euler's theorem. **4M**
- 1B.** State Chinese remainder theorem and find the value of  $x$  for the following example: **3M**
- $x \equiv 5 \pmod{6}$   
 $x \equiv 4 \pmod{11}$   
 $x \equiv 3 \pmod{17}$
- Ensure the validation of the value of  $x$ .
- 1C.** Given the message "additionalsheet" use a Rail Fence of key 3 to encrypt and decrypt this message. Show all the steps in detail. Make suitable assumptions if required. **3M**
- 2A.** The vigenere key stream does not depend on the plaintext characters; it depends only on the position of the character in the plaintext. Write the procedure of encryption and decryption. Also, encrypt the message "She is listening" using the 6-character keyword "PASCAL". **3M**
- 2B.** What is the Data Encryption Standard (DES)? Write the block diagram of the Data Encryption Standard system. Write encryption and decryption algorithms of DES system. **4M**
- 2C.** Write the general design of AES encryption cipher. Distinguish between AES and DES crypto systems. **3M**
- 3A.** Using Diffie Helman, prove  $K_A = K_B$  where  $K_A$  and  $K_B$  are shared secret keys. Consider a Diffie-Hellman scheme with a common prime number  $q=11$  and primitive root  $\alpha=7$ . Alice chooses a secret integer  $X_A=3$ . Bob chooses a secret integer  $X_B=6$ . Find the public keys and a shared key of Alice and Bob. **3M**
- 3B.** Describe the RC4 algorithm for key- stream generation. Write encryption and decryption process of RC4 cryptosystem. **3M**

- 3C.** Write Blum-Blum-Shub Pseudorandom Bit Generator and find linear congruential generator output, when  $m=16$ ,  $a=3$ , and  $b=1$ ,  $a$ ,  $b$  are relatively prime numbers,  $m$  is modulus and  $x_0$  is initial seed value. Write the procedure to find points on the elliptic curve. **4M**
- 4A.** Explain the key generation, encryption, and decryption of Rabin cryptosystem. Why it is called a variant of RSA? Clearly discuss the decryption process of Rabin cryptosystem by using Chinese remainder theorem. **3M**
- 4B.** What is hashing function? Explain the general operation of a cryptographic hash function. Briefly explain the four message authentication techniques with the relevant diagrams. **4M**
- 4C.** With the help of a diagram explain overview and step by step procedure of SHA-512. **3M**
- 5A.** Why we need message authentication? write three types of functions that are used to produce an authenticator. With the help of a diagram briefly explain HMAC structure. **4M**
- 5B.** Mention the key generation steps of Elliptic curve digital signature scheme. Write the block diagram representations of the following digital signature schemes. **3M**
- (i) RSA digital signature scheme.
  - (ii) The RSA signature on the message digest.
- 5C.** Briefly explain the model authentication system. What is zero-knowledge proof statements? write any two properties of zero-knowledge proof statements. **3M**