Reg. No.

IANIPAL INSTITUTE OF TECHNOLOGY

MANIPAL (A constituent unit of MAHE, Manipal)

II SEMESTER M.TECH. (AUTOMOBILE ENGINEERING) END SEMESTER EXAMINATIONS, APR-MAY 2019

SUBJECT: COMPUTATIONAL FLUID DYNAMICS [AAE 5233]

REVISED CREDIT SYSTEM (04/05/2019)

Time: 3 Hours

MAX. MARKS: 50

Instructions to Candidates:

- ✤ Answer ALL the questions.
- Missing data may be suitable assumed.
- **1A.** For the one-dimensional heat conduction is given by

$$\frac{d}{dx}\left(k.\frac{dT}{dx}\right) + S = 0,$$

Where K = thermal conductivity and T is the temperature and S the heat generated, obtain the discretization equation by Finite Volume technique in the standard form, $a_pT_p = a_ET_E + a_wT_w + S_u$

- 1B. Derive the Navier-Stokes equation in non-conservative form for a 3-D fluid flow 06 subjected to normal and shear stresses as well as pressure forces
- 2A. Explain three the properties of numerical schemes in while using Control Volume 03 Approach.
- **2B.** Explain the difference between collocated and staggered grid arrangement **02**
- **2C.** With a neat flow diagram explain the SIMPLE algorithm of Patankar-Spalding **05**
- **3A.** Using finite difference numerical scheme and TDMA method to solve for the **06** distribution of ϕ with the data given below.

$$\frac{d^2T}{dx^2} + h'(T_a - T) = 0$$

 $\Delta x = 2.0, h' = 0.01$ boundary conditions: $T|_{x=0} = 200 \ ^{\circ}C \text{ and } T|_{x=10} = 100 \ ^{\circ}C$

- **3B.** With a neat sketch, explain the solution capsule for ADI method **02**
- **3C.** Explain the four basic rules of control volume formulations.
- 4. Use the simple implicit finite difference approximation to solve for the temperature 10AAE 5233 Page 1 of 2

04

02

distribution of a long thin rod with a length of 10cm after t = 0.2s and the following values: At t = 0 the temperature of the rod is zero and the boundary conditions are fixed for all the times at $T(0)=100^{\circ}$ C and $T(10)=50^{\circ}$ C.value of k = 0.835cm2/s. the governing equation is given as,

$$k \frac{\partial^2 T}{\partial x^2} = \frac{\partial T}{\partial t}$$
$$\Delta x = 2cm, \Delta t = 0.1s$$

5. A property ϕ is transported by means of convection and diffusion through the one 10 dimensional domain sketched below. The governing equation is

$$\frac{d\left(\rho u\phi\right)}{dx} = \frac{d}{dx} \left(\Gamma \frac{d\phi}{dx}\right)$$

The boundary conditions are

 $\phi_0 = 1.0$ at x = 0 and $\phi_L = 0$ at x = L.

Using five equally spaced cells and the UDS calculate the distribution of ϕ when u = 0.2 m/s. Consider $\rho = 1.5$, L = 0.5m, $\Gamma = 0.1$