MANIPAL INSTITUTE OF TECHNOLOGY

(A constituent unit of MAHE, Manipal)

## SIXTH SEMESTER B.TECH. (E & C) DEGREE END SEMESTER EXAMINATION APRIL/MAY 2019

## SUBJECT: DIGITAL COMMUNICATIONS (ECE - 3201)

## TIME: 3 HOURS

MAX. MARKS: 50

## **Instructions to candidates**

- Answer **ALL** questions.
- Missing data may be suitably assumed.
- 1A. A discrete memory-less source X has eight symbols x1, x2, x3, x4, x5, x6, x7 and x8 with probabilities  $P(x_1) = 0.01$ ,  $P(x_2) = 0.01$ ,  $P(x_3) = 0.15$ ,  $P(x_4) = 0.1$ ,  $P(x_5) = 0.05$ ,  $P(x_6) = 0.03$ ,  $P(x_7) = 0.4$ ,  $P(x_8) = 0.25$ . Perform source encoding using Shannon-Fanon and Huffman encoding techniques. Also, calculate and compare the efficiencies of both techniques.
- 1B. A convolutional encoder has a single stage (i.e., one flip-flop with constraint length K=2), one modulo-2 adder and an output multiplexer. The generator sequences of the encoder are:  $g^{(1)} = (1, 1), g^{(2)} = (1, 0)$ . Draw the block diagram of the encoder. Find the encoder output produced by the message sequence 10111.
- 1C. The PN sequence generator has 3 flip-flops with outputs  $x_1$ ,  $x_2$  and  $x_3$  respectively. The feedback has a modulo-2 adder with  $x_2$  and  $x_3$  inputs and the feedback is given to the input of first flip-flop. The initial state of flip-flop is 100. Obtain the PN sequence.

(4+3+3)

- 2A. Determine and plot the power spectral density of a Manchester data format. Assume statistically independent and equally likely message bits.
- 2B. With a neat diagram explain Generalized correlative coding. Construct a correlative coder which has tap weights  $w_0 = +1$ ,  $w_1 = 0$  and  $w_2 = -1$ . Encode the binary sequence 001011010 using the same coder.
- 2C. With a neat diagram of transmitter and the receiver, derive the expression for the probability of error of the coherent Binary Frequency Shift Keying.

(4+3+3)

- 3A. Derive the maximum likelihood detection rule for the detection of the known equiprobable M-ary signals in noise. Also obtain the expression for the probability of error for the same.
- 3B. Consider the functions  $s_1(t) = e^{-|t|}$  and  $s_2(t) = 1 Ae^{-2|t|}$ . Determine the constant, A, such that  $s_1(t)$  and  $s_2(t)$  are orthogonal over the interval  $(-\infty, \infty)$ .
- 3C. Derive the impulse response of a matched filter that gives maximum value of output SNR.

(4+3+3)

4A. Prove that a wide sense stationary message process X(t) that contains 'W' Hertz as highest frequency component can be reconstructed from its samples which are spaced at 1/2W secs apart with zero error power.

- 4B. Derive the expression for aliasing error while reconstructing the signal from its sampled version. Also mention its maximum value.
- 4C. Design a TDM PCM system that will accommodate four 300 bps (synchronous) digital inputs and one analog input that has a bandwidth of 500 Hz. Assume that the analog samples will be encoded into 4-bit PCM words.

(4+3+3)

- 5A. Determine the output SNR in a DM system for a 1 kHz sinusoid, sampled at 32 kHz without slope overload and followed by a 4 kHz post reconstruction filter.
- 5B. Determine the ratio of minimum to maximum step size in the case of A-law compander.
- 5C. A binary channel with a bit rate  $R_b = 36kbps$  is available for PCM voice transmission. Find appropriate values of the sampling rate, Number of quantization levels and the number of bits per sample if the maximum frequency component is  $f_m = 3.2$  kHz

(4+3+3)