Exam Date & Time: 28-Nov-2019 (02:00 PM - 05:00 PM)



MANIPAL ACADEMY OF HIGHER EDUCATION

INTERNATIONAL CENTRE FOR APPLIED SCIENCES END SEMESTER THEORY EXAMINATION - NOVEMBER/ DECEMBER 2019 IV SEMESTER B.Sc.(Applied Sciences)in Engg.

Dynamics Of Systems [ME 244]

Marks: 100

Duration: 180 mins.

Answer any FIVE full Questions. Missing data, if any, may be suitably assumed

¹⁾ Define corner frequency with respect to frequency domain analysis. Determine the magnitude and phase using bode plot analysis for the open loop transfer function ⁽¹⁰⁾

A)

$$G(s) = \frac{e^{-0.2s}}{s(s+2)(s+8)}$$

- ^{B)} With the help of a neat diagram, derive the transfer function for an armature controlled ⁽¹⁰⁾ DC servo motor.
- 2) Sketch the Nyquist plot for an open loop transfer function of a system which is defined (12) as:
 A)

$$G(s)H(s) = \frac{K(4s+1)}{s(s-1)}$$

Also compute the range of K for which the system is stable.

^{B)} For a system which is subjected to a step of 1 volt, the open loop transfer function is ⁽⁸⁾ given by

$$G(s) = \frac{2}{s(s+2)}$$

Find a) Time to first maximum b) Time to first minimum c) Time to second maximum d) Time to second minimum

³⁾ Describe any four disadvantages of the classical LTI approaches which are overcome ⁽¹²⁾ by the use of state space approach. Obtain the state space model for the following transfer function using phase variables.

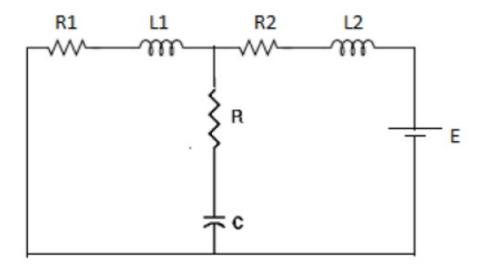
$$\frac{Y(s)}{U(s)} = \frac{s^2 + 3s + 4}{s^3 + 2s^2 + 3s + 2}$$

B)

Derive the expression for the response of an over damped second order system for a ⁽⁸⁾

unit step input and draw its response.

- With mathematical expressions, describe the behavior of four test signals used in time ⁽⁴⁾ domain analysis.
- ^{B)} What is damping ratio with respect to a second order system? Describe the effect of damping ratio on the performance of a second order system by considering the characteristic equation.
- ^{C)} For the electrical system shown in fig. 4(c),
 - i) Write down the differential equations describing the electrical system.
 - ii) Draw the equivalent mechanical analogous system and rotational analogous system.
 - iii) Write the differential equations for mechanical translational and rotational system.



Define Controllability and Observability. Evaluate both for the following parameters of (10) the state space model:

A)

5)

4)

0	1	0]	[8]			
A = 0	0	1	$\mathbf{B} = \begin{bmatrix} 8\\4\\0 \end{bmatrix}$	C = [3	4	1]
Lo	$^{-2}$	-3	Lol			

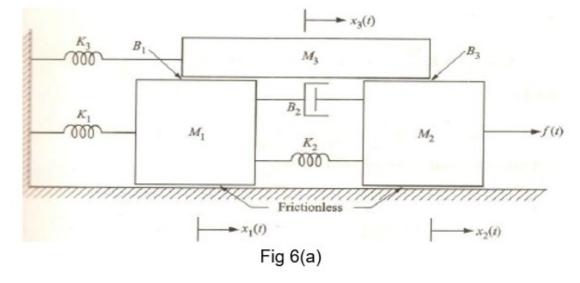
^{B)} Write the conditions for Bounded Input Bounded Output (BIBO) stability. For the characteristic equation given below, calculate the number of roots lying on the right hand side of the s-plane and comment on the stability of the system using the R-H stability criterion.

$$s^7 + 9s^6 + 24s^5 + 24s^4 + 24s^3 + 24s^2 + 23s + 15 = 0$$

 ⁶⁾ For the mechanical rotational system shown in fig. 6(a), Draw equivalent mechanical network and with free body diagrams, write down the differential
 ^{A)} equations describing the system. Draw analogous electrical network based on force current analogy and write down the analogous electrical equations.

(12)

(10)



^{B)} Define steady state error and write its mathematical expression. Consider a unity (8) feedback system with a closed loop transfer function

$$M(s) = C(s) / R(s) = \frac{Ks+b}{s^2+as+b}$$

Determine open loop transfer function G(s). Show that the steady state error for a unit ramp input is given by (a - K)/b.

Consider a system defined by X = Ax + Bu, where,

A)

7)

8)

 $\mathbf{A} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -1 & -5 & -6 \end{bmatrix} \qquad \mathbf{B} = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$

By using the state-feedback control $\mathbf{u} = -\mathbf{K}\mathbf{x}$, it is desired to have closed loop poles at - 2-4j,-2+4j and -10 respectively. Determine the state-feedback gain matrix K. Verify the result by using Ackerman's formula.

- ^{B)} Differentiate between open loop system and closed loop system with an example. ⁽⁴⁾
- What is the need of controller in control systems? With neat sketches, explain
 proportional plus integral (PI), proportional plus derivative (PD) and proportional integral derivative (PID) controllers
- B) Sketch the root locus for the open loop transfer function of a unity feedback system (12) given by:

$$G(s) = \frac{K}{s(s+2)(s+4)}$$

Also, determine K for damping ratio of 0.5 from the root locus.

(16)