Reg. No.



(A constituent unit of MAHE, Manipal)

FIRST SEMESTER M.TECH. (CONTROL SYSTEMS)

END SEMESTER DEGREE EXAMINATIONS, NOVEMBER - 2019

SUBJECT: ADVANCED CONTROL THEORY [ICE 5152]

TIME: 3 HOURS

MAX. MARKS: 50

Instructions to candidates : Answer ALL questions and missing data may be suitably assumed.

- 1A. Mention FOPDT model and with the help of graph elaborate each variable.
- Determine the type of the system, 1B.

 $G(s) = \frac{\kappa}{s^3 + 8s^2 + 17s}$ with the help of steady state error and its corresponding gains.

Design a lag compensator using time domain approach for the system, 1C.

 $G(s) = \frac{\pi}{s(s+1)}$ to satisfy the design specification of overshoot 10% and ramp error gain 10. Also plot the root locus after compensation.

(2+3+5)

2A. Find the solution of y(k+2)+3y(k+1)+2y(k) = r(k); r(k) is unit step function.

2B. Plot bode diagrams of

> $G(z) = \frac{10}{z(z-1)}$; with T=1 s. Also comment on closed loop stability of the system.

2C. Derive Pulse transfer function of the system shown in Fig. Q2C.



(2+3+5)

- 3A. Obtain the dominant pole locations of a second order discrete system if damping ratio is 0.5, settling time is 1 s and sampling period is 1 s.
- For the electrical system shown in Fig. Q3B, select minimal state variables and find the state model 3B. in physical variable form. Take $V_o(t)$ as the output.



3C. Diagonalize the system

 $\frac{Y(s)}{U(s)} = \frac{s+3}{s^3 + 9s^2 + 24s + 20}$

4A. Design state feedback control law by direct substitution method for the regulator system $\dot{x} = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix}$; $B = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$; $C = \begin{bmatrix} 1 & 0 \end{bmatrix}$;

The closed loop Eigen values to be placed at three times the open loop pole locations.

- 4B. Find the complete solution for the state equation for $\dot{x} = 8x + 2u$; y = x + u. with ramp input and initial state x(0) = 1.
- 4C. Derive the observable canonical form of $\frac{Y(s)}{U(s)} = \frac{s^3 + s^2 + 6s + 8}{s^3 + 9s^2 + 20s + 13}$

5A. Check the complete state observability of $x(k+1) = \begin{bmatrix} 1 & 0 \\ 0 & 0.5 \end{bmatrix} x(k) + \begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix} u(k)$; $y(k) = \begin{bmatrix} 1 & 1 \end{bmatrix} x(k)$.

- 5B. Obtain state model of the system by direct decomposition. Draw the state diagram. $G(z) = \frac{3}{(z+2)^3}$
- 5C. Given the continuous state model find the discrete state model of the system for T=1s. Also find its pulse transfer function.

 $\dot{x} = \begin{bmatrix} 1 & 1 \\ 0 & 2 \end{bmatrix} x + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u ; y = \begin{bmatrix} 0 & 1 \end{bmatrix} x + 0.5u$

(2+3+5)

(3+3+4)

(2+3+5)

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