ANIPAL INSTITUTE OF TECHNOLOGY

(A constituent unit of MAHE, Manipal)

## SEVENTH SEMESTER B.TECH. (INSTRUMENTATION AND CONTROL ENGG.) END SEMESTER DEGREE EXAMINATIONS, DECEMBER - 2019

SUBJECT: ROBOTIC SYSTEMS AND CONTROL [ICE 4030]

## TIME: 3 HOURS

## MAX. MARKS: 50

## Instructions to candidates : Answer ALL questions and missing data may be suitably assumed.

- 1A. A rigid body is translated by 2 units along the X-Axis, then rotated about the -Z axis by  $30^{0}$  and finally translated by a distance of 4 units along the Y axis. Determine the homogeneous transformation matrix.
- 1B. Calculate the degrees of freedom for the mechanism shown in Fig. Q1B.
- 1C. Given the homogenous transformation matrices  ${}^{a}T_{b}$  and  ${}^{c}T_{b}$ , find the transformation matrix  ${}^{a}T_{c}$ .

$${}^{a}T_{b} = \begin{bmatrix} 0.867 & -0.5 & 0 & 11 \\ 0.5 & 0.867 & 0 & -1 \\ 0 & 0 & 1 & 8 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad {}^{c}T_{b} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0.867 & 0.5 & 10 \\ 0 & -0.5 & 0.867 & -20 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

1D. List the basic elements of a robot. Also, determine the orientation matrix {R} w.r.t RPY angles  $q = \begin{bmatrix} 30^{\circ} & -45^{\circ} & 60^{\circ} \end{bmatrix}$ 

(2+2+4+2)

- 2A. Explain why D-H representation does not give unique frame assignment for any given manipulator.
- 2B. Define manipulator workspace. How does reachable workspace differ from dextrous workspace?
- 2C. With a relevant example, differentiate between constrained and unconstrained kinematic motions.
- 2D. Obtain the end-effector coordinates for the manipulator shown in Figure Q2B. Given that the coordinates of the base frame  $\{0\}$  is  $[0\ 0\ 0]^T$ . Assume: L<sub>1</sub>=10, L<sub>2</sub>=4, L<sub>3</sub>=2, d<sub>1</sub>=0.5 (all units in cm) (2+2+2+4)
- 3A. For Q2D, determine all possible joint configuration(s) corresponding to kinematic singularity for the manipulator.
- 3B. Given that the homogeneous transformation matrix ( ${}^{0}T_{E}$ ) (i.e. end-effector w.r.t. base frame) for a 3DoF manipulator is as given below. Determine the joint space  $q = [\theta_1 \quad \theta_2 \quad d_3]^T$

$${}^{0}T_{E} = \begin{bmatrix} C_{1}C_{2} & -S_{1} & -C_{1}S_{2} & -d_{3}C_{1}S_{2} \\ S_{1}C_{2} & C_{1} & -S_{1}S_{2} & -d_{3}S_{1}S_{2} \\ S_{2} & 0 & C_{2} & d_{3}C_{2} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

- 3C. Explain how Skew symmetric matrix (S) is related to the angular velocity of a link for an N-dof arm. (5+3+2)
- 4A. Differentiate between:

- (i) Path and trajectory
- (ii) Joint Space Trajectory and Cartesian Space Trajectory
- 4B. A rotary joint moves from  $-15^{\circ}$  to  $+45^{\circ}$  in 3 seconds. Determine a fifth order polynomial for a smooth joint trajectory. Also plot the position, velocity and acceleration of the joint as a function of time (t). Assume both velocity and acceleration to be zero at t=0s and t=3s.
- 4C. In Cartesian straight-line path planning, *linear-trajectory-with-parabolic-blends* is more appropriate. Why?

(3+5+2)

- 5A. List the various types of proprioceptive and exteroceptive sensors used in robots.
- 5B. Draw and explain the block-diagram for a partitioned PD controller for the trajectory control of a 1-dof rotary joint.
- 5C. (i) Number of rows in the Jacobian matrix corresponds to \_\_\_\_\_ (taskspace dimension / dof).
   (ii) State TURE or FALSE: "The inertia-matrix M(q) is symmetric and uniformly positive definite for all q ∈ ℝ<sup>n</sup>."
- 5D. For the hand-frame of a 5-dof (RRPRR) robot, the instantaneous values of its forward-kinematic transformation and Jacobian matrices are given as follows. Determine the new location of the hand-frame after the given differential motions (dq).

$$J = \begin{bmatrix} 3 & 0 & 0 & 0 & 0 \\ -2 & 0 & 1 & 0 & 0 \\ 0 & 4 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 & 0 \\ -1 & 0 & 0 & 0 & 1 \end{bmatrix} {}^{0}T_{5} = \begin{bmatrix} 1 & 0 & 0.1 & 5 \\ 0 & 0 & -1 & 3 \\ 0 & 1 & 0 & 2 \\ 0 & 0 & 0 & 1 \end{bmatrix} dq = \begin{bmatrix} 0.1^{0} & -0.1^{0} & 0.05cm & 0.1^{0} & 0^{0} \end{bmatrix}$$

$$(2+2+2+4)$$





Figure Q1B

Figure Q2B

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