



V SEMESTER B. TECH (MECHANICAL ENGG.) END SEMESTER ONLINE

EXAMINATIONS, JANUARY-FEBRUARY 2021

SUBJECT: FINITE ELEMENT METHOD [MME 3152]

REVISED CREDIT SYSTEM

Time: 3 Hours

MAX. MARKS: 50

Instructions to Candidates:

- ❖ Answer **ALL** the questions.
- ❖ Missing data (if any) may be suitably assumed.

- 1A.** The component shown in **figure 1A** is spinning at ω rad/sec. Assuming 1D structure, **05 M**
determine the finite element interpolation functions and obtain the expression for element stiffness matrices in terms of these interpolation functions. Use minimum number of finite elements.

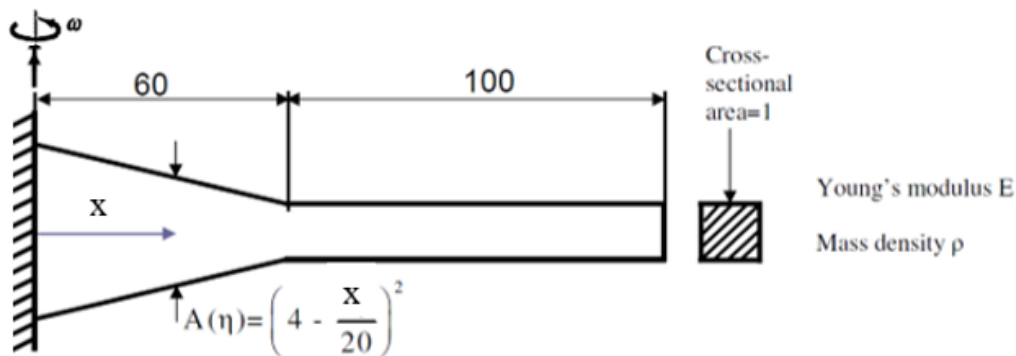


FIGURE 1A

- 1B.** A pipe line is laid to transport water at a velocity of 25 m/s to the top of a steep hill, **03 M**
whose inclination is assumed to be 45° . A small section of this pipeline system of length 1.5 m and 400 mm uniform diameter is required to be analyzed for pressure head distribution using FEM. The pressure at inlet and outlet are known as 29.43 N/cm² and 22.56 N/cm² respectively. Discretize the continuum into three equal length elements and determine unknown pressure heads. Use penalty approach for handling boundary conditions.
- 1C.** Solve the given integral function using two-point Gauss Quadrature rule. **02 M**

$$I = \int_1^3 x^6 - x^2 \sin(2x) dx$$

- 2A. Consider a simple bar fixed at one end ($x = 0$) and subjected to a concentrated force at the other end (at $x = 180$) as shown in **figure 2A**. 05 M

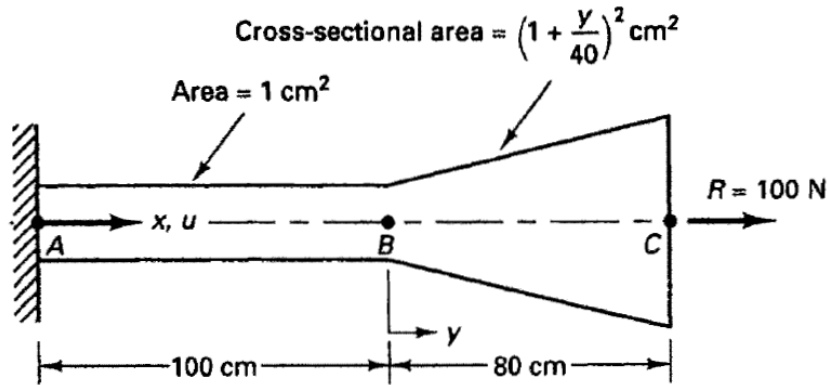


FIGURE 2A

Using the notations in the figure, the total potential energy of the structure is given by,

$$\Pi = \int_0^{180} \frac{1}{2} EA \left(\frac{du}{dx} \right)^2 dx - 100u|_{x=180} \quad \text{and } u_A = 0 \text{ at } x = 0.$$

Calculate the displacement and stress distributions in the structure using the Rayleigh-Ritz method with the following displacement assumptions:

$$u = \frac{xu_B}{100}; \quad 0 \leq x \leq 100$$

and,

$$u = \left(1 - \frac{x - 100}{80} \right) u_B + \left(\frac{x - 100}{80} \right) u_C; \quad 100 \leq x \leq 180$$

where, u_A , u_B and u_C are displacements at points A, B and C respectively and E is material constant.

- 2B. For the truss configuration shown in **figure 2B**, setup global $\{F\} = [K] \{Q\}$ relationship 03 M and apply all boundary conditions.

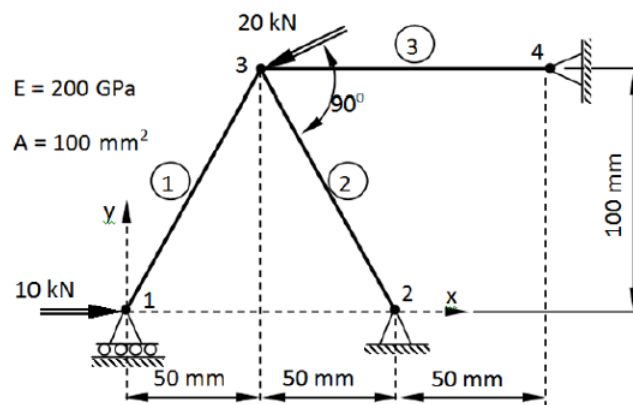


FIGURE 2B

2C. "A simple 4 noded 2D plane element is a complete element". Justify. 02 M

3A. A disc with a centerline hole of radius 20 mm is shown in **figure 3A**, spinning at a rotational velocity of ω radians/ second. Idealize the structure as an assembly of 2 noded minimum number of finite elements and determine: 05 M

i) Interpolation functions.

ii) Strain-displacement relationship matrix.

iii) Stiffness matrix in integral form.

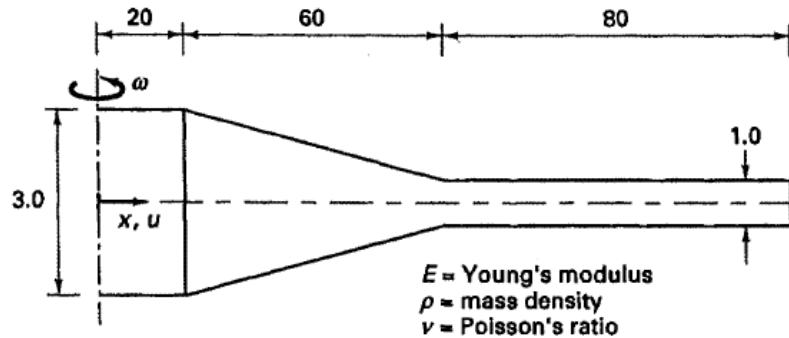


FIGURE 3A

3B. For the bar element with varying cross-section shown in **figure 3B**, derive the element stiffness matrix. Assume Elastic modulus (E) as constant and Area (A) varies linearly. 03 M

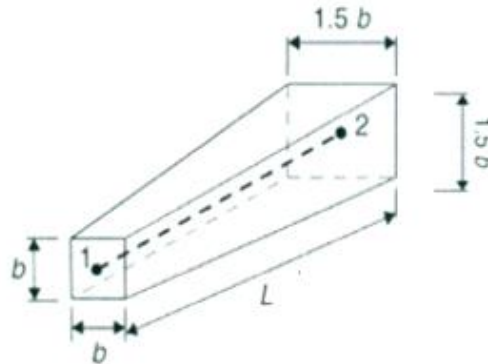


FIGURE 3B

3C. Write the displacement functions using polynomials for simplest 3D element and mention how the number of equations and number of terms in the equations are decided? 02 M

4A. The structure shown in **figure 4A**, need to be analyzed using 3 noded 2D elements. Discretize the domain using minimum no elements and sketch discretized representation. Also, obtain the global $\{F\} = [K] \{Q\}$ relationship and apply boundary conditions. Take elastic modulus as $20 \times 10^6 \text{ N/cm}^2$, ratio of lateral strain to longitudinal strain as 0.3 and thickness of the plate as 1 cm. 05 M

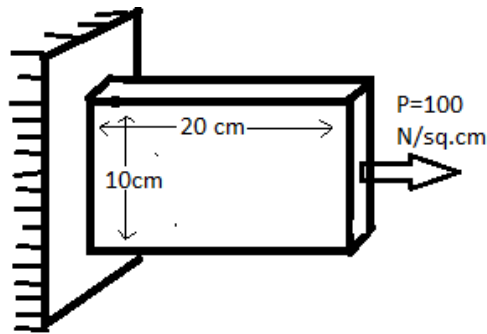


FIGURE 4A

- 4B.** For the structural configuration shown in **figure 4B**, obtain the displacement and slope **03 M**
using FEM. Take the flexural rigidity constant as EI and spring constant as,

$$K = \frac{76EI}{L^3}.$$

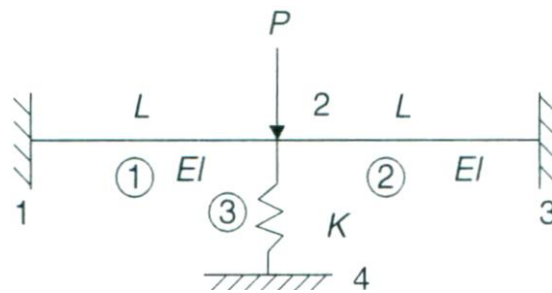


FIGURE 4B

- 4C.** Illustrate the limitations of minimum potential energy method with suitable example. **02 M**
- 5A.** A transverse load carrying member having uniform circular cross section of 100 mm **04 M**
diameter is loaded with uniformly distributed load as shown in **figure 5A**. Using
minimum no of finite elements determine the deflection at the midpoint of the
distributed load region. Take material constant $E = 200 \text{ GPa}$.

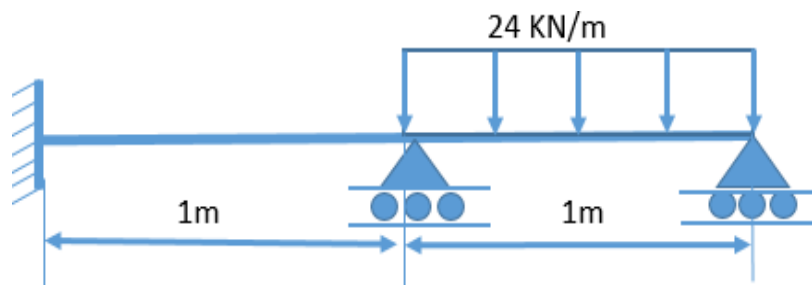


FIGURE 5A

- 5B.** Using principle of minimum potential energy, setup the global $\{F\} = [K]\{Q\}$ **04 M**
relationship for the spring assemblages shown in **figure 5B** and determine unknown
displacements.

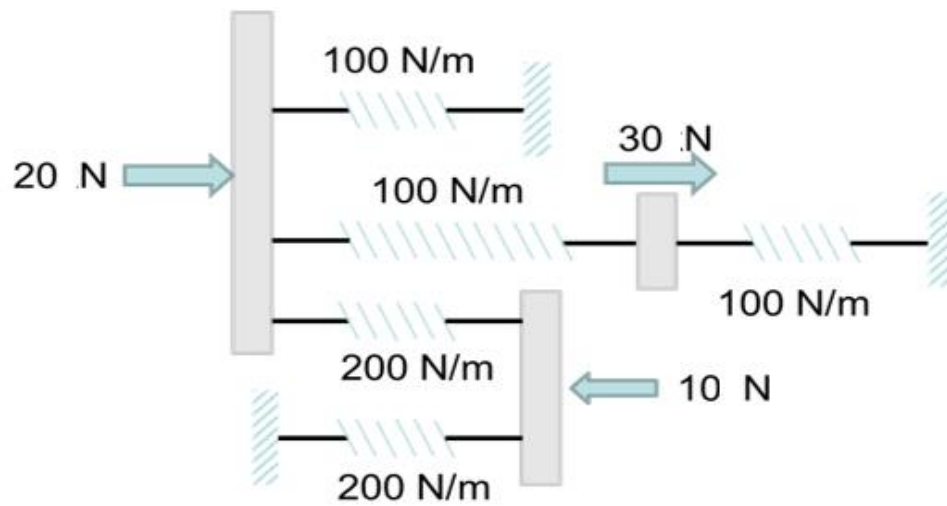


FIGURE 5B

- 5C. With an example illustrate the term “spacial isotropy” of an element in finite element method. **02 M**