



**SIXTH SEMESTER B.TECH. (ELECTRONICS & INSTRUMENTATION ENGG.)**  
**ONLINE GRADE IMPROVEMENT/MAKE-UP EXAMINATIONS, AUGUST - 2021**

**SUBJECT: DIGITAL SIGNAL PROCESSING [ICE 3251]**

**TIME: 2 HOURS**

07-08-2021

**MAX.MARKS: 40**

**Instructions to candidates: Answer any *FOUR FULL* questions.**

**Missing data may be suitably assumed.**

- 1A. A system has an impulse response  $h[n] = a^n u[n]$ , determine its output for the following inputs.  
i)  $x[n] = n + 1; 0 \leq n \leq 2$ ; ii)  $x[n] = u[n]$
- 1B. State and prove i) up sampling; ii) right shifting properties of the Z-transform. (5+5)
- 2A. Determine the Z-transform for the following sequences  
i)  $x[n] = n \left(-\frac{1}{2}\right)^n u[n] * \left(\frac{1}{4}\right)^{-n} u[-n]$  ii)  $p[n] = -u[-n - 1] + \left(\frac{1}{2}\right)^n u[n]$
- 2B. Determine sequence  $x[n]$  for which  
$$X[z] = \frac{0.4}{1 - 0.7z^{-1}} + \frac{0.25}{1 - 5z^{-1}}$$
where the ROC includes the unit circle. Determine  $x(0)$ . (5+5)
- 3A. State and prove circular time shift and time reversal properties of DFT.
- 3B. Compute 8-point DFT of the discrete time signal,  $x(n) = \{1, 2, 1, 2, 1, 3, 1, 3\}$  and plot the magnitude spectrum. (5+5)
- 4A. Determine the response of the LTI system using radix-2 DIT FFT algorithm, given the input  $x(n) = \{2, 3, 4, 1\}$  and the impulse response  $h(n) = \{-2, -1\}$ .
- 4B. Define impulse invariance transformation? What for it is used? Obtain a relation between analog and digital frequency using impulse invariance transformation. (5+5)
- 5A. Determine the poles of a lowpass Butterworth filter for  $N = 3$ . Sketch the location of poles on s-plane and hence determine the analog normalized transfer function of lowpass filter.

- 5B. Obtain the digital filter  $H(Z)$  from given  $H(s)$

$$H(s) = \frac{2s}{s^2 + 0.2s + 1}.$$

Given the sampling period is 2 seconds. Use bilinear transformation technique.

(5+5)

- 6A. Given  $H(z) = \frac{0.44z^{-1} + 0.36z^{-2} + 0.02z^{-3}}{1 + 0.4z^{-1} + 0.18z^{-2} - 0.2z^{-3}}$  Obtain the direct form I and direct form II realization.

- 6B. Compare any five features of Butterworth and Chebyshev filter design methods.

(5+5)

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