

# Question Paper

Exam Date & Time: 14-Jan-2021 (02:00 PM - 05:00 PM)



**MANIPAL INSTITUTE OF TECHNOLOGY**  
MANIPAL  
(A constituent unit of MAHE, Manipal)

FOURTH SEMESTER B.TECH ELECTRONICS AND INSTRUMENTATION END SEMESTER EXAMINATIONS, JAN 2021

**LINEAR CONTROL THEORY [ICE 2253]**

**Marks: 50**

**Duration: 180 mins.**

## Part A

**Answer all the questions.**

Instructions to Candidates: Missing data may be suitably assumed

- 1) Obtain the transfer function  $\frac{X_o(s)}{X_i(s)}$  of the mechanical system shown in figure 1(a). Also obtain the (5)
- A)

transfer function  $\frac{E_o(s)}{E_i(s)}$  of the electrical system shown in figure 1(b). Show that these transfer functions of the two systems are of identical form and thus they are analogous systems.

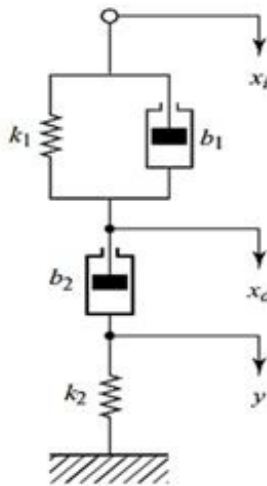


Figure 1(a)

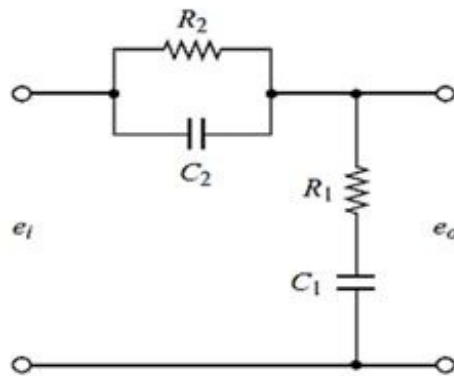


Figure 1(b)

- B) Distinguish between open loop and closed loop system. What are the characteristics of negative feedback? (3)
- C) What pole locations characterize (i) the under damped system (ii) over damped system (iii) critically damped system (iv) undamped system. (2)
- 2) Using Mason's rule find the transfer function,  $T(s) = \frac{C(s)}{R(s)}$ , for the system described by signal (5)
- A)
- flow graph as shown in figure 2.

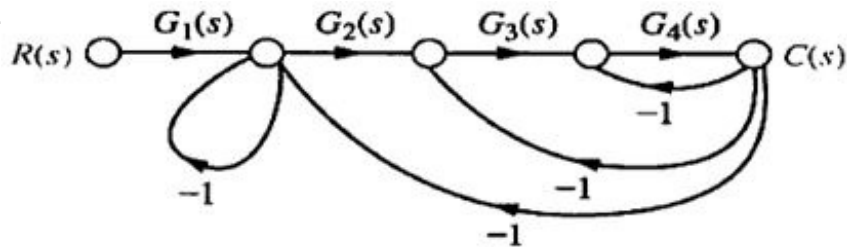


Figure 2

- B) Consider a unity feedback system with a closed loop transfer function  $\frac{C(s)}{R(s)} = \frac{Ks + b}{s^2 + as + b}$ . (3)

Determine the open loop transfer function  $G(s)$ . Also obtain the steady state error for the system with unit ramp input.

- C) Define corner frequency. What are the advantages of Bode plot? (2)

- 3) For the system shown in figure 3, (i) Find  $K_p$ ,  $K_v$ , and  $K_a$  (ii) Find the steady state error for an input of  $50u(t)$ ,  $50tu(t)$ , and  $50t^2u(t)$  (iii) State the system type. (5)

A)

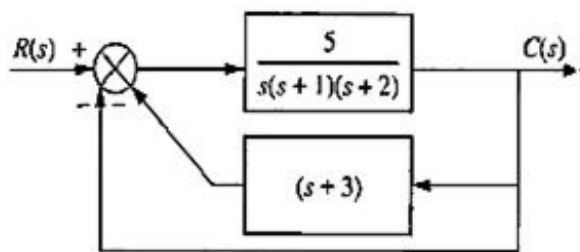


Figure 3

- B) What is Nyquist stability criterion? For the loop transfer function  $G(s)H(s) = \frac{K}{s(s+2)(s+10)}$ , based on the following statements comment on the closed loop stability of the system (Case I and Case II), justify the answer. What is the range of  $K$  for the stability? (5)

loop stability of the system (Case I and Case II), justify the answer. What is the range of  $K$  for the stability?

**Case I:** When  $K$  is less than 240, the contour crosses real axis at a point between 0 and -1. On travelling through Nyquist plot in clockwise direction it is found that the point  $-1+j0$  is not encircled.

**Case II:** When  $K$  is greater than 240, the contour crosses real axis at a point between -1 and  $-\infty$ . On travelling through Nyquist plot in clockwise direction it is found that the point  $-1+j0$  is encircled two times.

- 4) Construct the Routh array and determine the stability of the system represented by the characteristic equation,  $s^6 + 2s^5 + 8s^4 + 12s^3 + 20s^2 + 16s + 16 = 0$ . Also (5)

- A) determine the number of roots lying on right half  $s$  - plane, left half  $s$  - plane and on imaginary axis.

- B) Sketch the root locus for the unity feedback system whose open loop transfer function is  $G(s)H(s) = \frac{K(s+1.5)}{s(s+1)(s+5)}$  (5)

- 5) A unity feedback system has an open loop transfer function,  $G(s) = \frac{K}{s(1+2s)}$ . Design a (7)

- A) suitable lag compensator so that phase margin is  $40^\circ$  and steady state error for ramp input is  $\leq 0.2$

- B) What is meant by compensation in control systems? Write the transfer function of lead compensator and draw its pole - zero plot. (3)

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