

**DEPARTMENT OF SCIENCES,
III SEMESTER M.Sc (Applied Mathematics and Computing)
END SEMESTER EXAMINATIONS, MARCH 2021**

SUBJECT: Formal Language and Theory of computation [MAT 5001]

(REVISED CREDIT SYSTEM-2017)

Time: 3 Hours

Date: 24.03.2021

MAX. MARKS: 50

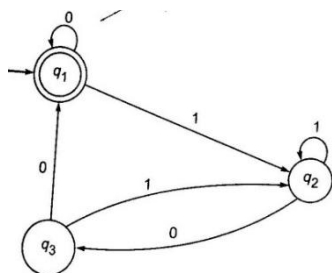
Note : All questions carry equal marks (3 + 3 + 4)

- 1A. Sketch and Describe the block diagram of a Finite automaton
- 1B. Prove that if L is regular then L^T is also regular. Give an example.
- 1C. Design FA which checks whether a given decimal number is divisible by four.
Verify the same for the number 456789 and write a corresponding path.
- 2A. Define Mealy machines.
With suitable explanation, construct an equivalent Machine for the given Machine and draw its transition diagram.

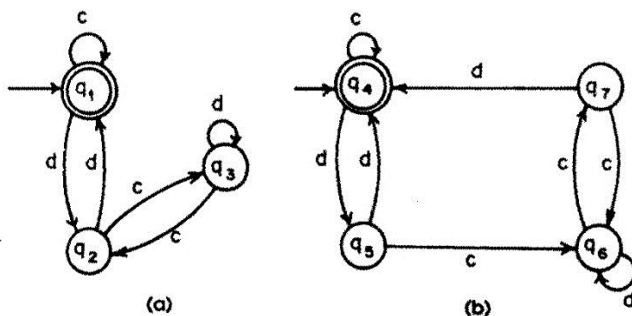
State	i.p. a=0		i.p. a=1	
	state	o.p.	state	o.p.
$\rightarrow q_1$	q_3	0	q_2	0
q_2	q_1	1	q_4	0
q_3	q_2	1	q_1	1
q_4	q_4	1	q_3	1

- 2B. Is \Rightarrow_G an equivalence relation on $(V_N \cup V_T)^*$?
- 2C. Show that the set $L = \{a^p \mid p \text{ is a prime}\}$ is not regular.
- 3A. Let L be the set of all palindromes over $\{a, b\}$. Construct a grammar G generating L .

- 3B. State and prove Arden's theorem..
- 3C. Construct a regular grammar G generating the regular set represented by $a^*b(a+b)^*$.
- 4A. Construct a reduced grammar equivalent to the grammar G whose productions are $S \rightarrow AB|CA$, $B \rightarrow BC|AB$, $A \rightarrow a$, $C \rightarrow aB|b$
- 4B. Construct a regular expression corresponding to the following FA shown in figure using algebraic method.



- 4C. Define comparison method. Determine whether the given two machines are equivalent.



- 5A. Define Greibach normal form of a language.
Convert the grammar $S \rightarrow AB$, $A \rightarrow BS|b$, $B \rightarrow SA|a$ into GNF.
- 5B. Show that the grammar $S \rightarrow aB|ab$, $A \rightarrow aAB|a$, $B \rightarrow ABb|b$ is ambiguous
- 5C. Obtain an equivalent automaton without ϵ moves with proper explanation to the figure below.

