

Reg. No.



# MANIPAL INSTITUTE OF TECHNOLOGY

MANIPAL  
(A constituent unit of MAHE, Manipal)

I SEMESTER M.TECH. (CEM) END SEMESTER EXAMINATIONS  
FEBRUARY 2021

SUBJECT: OPERATIONS RESEARCH AND DECISION THEORY  
[CIE 5158]

Date of Exam: 24/02/2021 Time of Exam: 2:00 PM to 5:00 PM Max. Marks: 50

## Instructions to Candidates:

- ❖ Answer ALL the questions & missing data may be suitably assumed

1A.	Discuss decision trees in detail with a suitable example	03	CO1																																					
1B.	<p>Solve the following game using graphical method indicating the optimal strategies and game value. The below given pay-off matrix is for Player A</p> <table><tr><td></td><td>B<sub>1</sub></td><td>B<sub>2</sub></td><td>B<sub>3</sub></td><td>B<sub>4</sub></td></tr><tr><td>A<sub>1</sub></td><td>2</td><td>2</td><td>3</td><td>-2</td></tr><tr><td>A<sub>2</sub></td><td>4</td><td>3</td><td>2</td><td>6</td></tr></table>		B <sub>1</sub>	B <sub>2</sub>	B <sub>3</sub>	B <sub>4</sub>	A <sub>1</sub>	2	2	3	-2	A <sub>2</sub>	4	3	2	6	07	CO1																						
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2A.	Discuss Artificial variables in detail in connection with LPP	02	CO2																																					
2B.	<p>Obtain the optimal solution to the following LPP using Big M method.</p> <p>Maximize <math>Z = 3x_1 - x_2</math> Subject to <math>2x_1 + x_2 \geq 2</math> <math>x_1 + 3x_2 \leq 3</math> <math>x_2 \leq 4</math> And <math>x_1, x_2 \geq 0</math></p>	08	CO2																																					
3A.	Discuss in brief, the unbalanced transportation problems with examples	02	CO3																																					
3B.	<p>Solve the following transportation problem using MODI (u-v) method. The table gives the transportation cost in thousands of Indian Rupees. Initial Basic Feasible Solution is indicated in bold numerals in the north west corner of the cells</p> <table><tr><td colspan="2" rowspan="2"></td><td colspan="4">Destination</td><td rowspan="2">Supply(units)</td></tr><tr><td>D<sub>1</sub></td><td>D<sub>2</sub></td><td>D<sub>3</sub></td><td>D<sub>4</sub></td></tr><tr><td rowspan="3">Warehouses</td><td>S<sub>1</sub></td><td>25 8</td><td>2 10</td><td>7</td><td>23 6</td><td>50</td></tr><tr><td>S<sub>2</sub></td><td>12</td><td>9</td><td>40 4</td><td>7</td><td>40</td></tr><tr><td>S<sub>3</sub></td><td>9</td><td>30 11</td><td>10</td><td>8</td><td>30</td></tr><tr><td colspan="2">Demand(units)</td><td>25</td><td>32</td><td>40</td><td>23</td><td></td></tr></table>			Destination				Supply(units)	D <sub>1</sub>	D <sub>2</sub>	D <sub>3</sub>	D <sub>4</sub>	Warehouses	S <sub>1</sub>	25 8	2 10	7	23 6	50	S <sub>2</sub>	12	9	40 4	7	40	S <sub>3</sub>	9	30 11	10	8	30	Demand(units)		25	32	40	23		08	CO3
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4A.	<p>Obtain an IBFS to the following transportation problem using VAM. The cost of transportation shown in table are in thousands of Indian Rupees</p> <table><tr><td></td><td>D<sub>1</sub></td><td>D<sub>2</sub></td><td>D<sub>3</sub></td><td>D<sub>4</sub></td><td>SUPPLY(units)</td></tr><tr><td>S<sub>1</sub></td><td>2</td><td>3</td><td>11</td><td>7</td><td>6</td></tr><tr><td>S<sub>2</sub></td><td>1</td><td>5</td><td>6</td><td>1</td><td>4</td></tr><tr><td>S<sub>3</sub></td><td>5</td><td>8</td><td>15</td><td>9</td><td>10</td></tr><tr><td>DEMAND(units)</td><td>8</td><td>6</td><td>3</td><td>3</td><td></td></tr></table>		D <sub>1</sub>	D <sub>2</sub>	D <sub>3</sub>	D <sub>4</sub>	SUPPLY(units)	S <sub>1</sub>	2	3	11	7	6	S <sub>2</sub>	1	5	6	1	4	S <sub>3</sub>	5	8	15	9	10	DEMAND(units)	8	6	3	3		03	CO3
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4B.	<p>Three buildings B<sub>1</sub>, B<sub>2</sub>, B<sub>3</sub> are to be done by four contractors C<sub>1</sub>, C<sub>2</sub>, C<sub>3</sub> and C<sub>4</sub>. Each building can be assigned to one and only one contractor. The cost of construction of each building by each of the contractors is given in the following matrix in Lakhs of Indian Rupees. What are the building assignments which will minimize the cost of construction?</p> <table><tr><td></td><td>C<sub>1</sub></td><td>C<sub>2</sub></td><td>C<sub>3</sub></td><td>C<sub>4</sub></td></tr><tr><td>B<sub>1</sub></td><td>18</td><td>24</td><td>28</td><td>32</td></tr><tr><td>B<sub>2</sub></td><td>8</td><td>13</td><td>17</td><td>19</td></tr><tr><td>B<sub>3</sub></td><td>10</td><td>15</td><td>19</td><td>22</td></tr></table>		C <sub>1</sub>	C <sub>2</sub>	C <sub>3</sub>	C <sub>4</sub>	B <sub>1</sub>	18	24	28	32	B <sub>2</sub>	8	13	17	19	B <sub>3</sub>	10	15	19	22	07	CO4										
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5A.	<p>In a store with one server,9 customers arrive on an average of 5 minutes. Service is done for 10 customers in 5 minutes. Find</p> <p>(i) The average no. of customers in the system</p> <p>(ii) The average queue length</p> <p>(iii) The average time a customer spends in the store</p>	03	CO4																														
5B.	<p>Solve the following LPP using Dynamic Programming</p> <p>Maximize <math>Z=5x_1+2x_2</math></p> <p>Subject to</p> $x_1+2x_2 \leq 43$ $x_1 \leq 23$ <p>And <math>x_1, x_2 \geq 0</math></p>	05	CO5																														
5C.	<p>Distinguish between Minimum – Span problems and Shortest- Route problems in connection with Network analysis</p>	02	CO5																														