

Reg. No.

**MANIPAL INSTITUTE OF TECHNOLOGY****MANIPAL***(A constituent unit of MAHE, Manipal)***I SEMESTER M.TECH. (STRUCTURAL ENGINEERING)****END SEMESTER EXAMINATIONS****FEBRUARY-2021****SUBJECT: FINITE ELEMENT METHOD****[CIE 5173]**

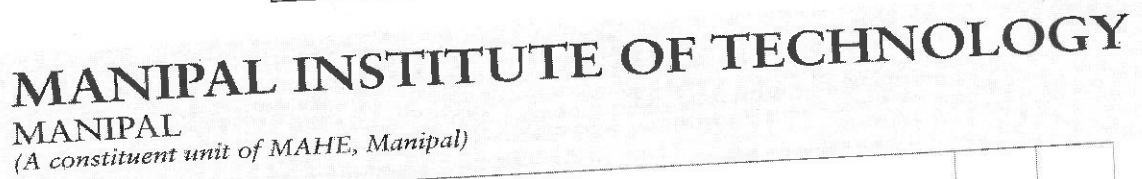
Date of Exam: 24-02-2021

Time of Exam: 3 Hours

Instructions to Candidates:

- ❖ Answer **ALL** the questions.
- ❖ Missing data may be suitably assumed

| Q. No | | MARKS | CO |
|-------|---|-------|-----|
| 1A. | List the various steps of finite element method of analysis and obtain the equation of equilibrium relating the stiffness matrix, displacement vector and load vector using principle of minimum potential energy | 04 | CO1 |
| 1B. | Obtain the shape functions for three noded triangular element | 03 | CO1 |
| 1C. | Calculate the equivalent nodal load vector for three noded bar element of length 1.0 m due to the varying load defined by the equation $q = 10x$ kN/m | 03 | CO1 |
| 2A. | <p>Analyse the axially loaded structure shown in figure Fig Q 2A. Take modulus of elasticity as 2×10^7 kN/m²</p> <p style="text-align: center;">Fig. Q. 2 A</p> | 05 | CO2 |
| 2B | Two noded beam element of length 3m is subjected to i) uniformly distributed load of 5 kN/m and a point load of 10 kN acting at a distance of 1 m from node 2. If the displacements at the nodes 1 and 2 are as follows, calculate forces in the element Take $EI = 1200$ kNm ² | 05 | CO3 |



| Node no | v (m) | Θ (rad) |
|---------|----------|----------------|
| 1 | 0 m | 0.001 |
| 2 | 0.0016 m | 0.0 |

Analyse the structure with fixed support at one end and supported by a spring as shown in figure **Fig. Q. 3A**. Take $EI = 6400 \text{ kNm}^2$ for the horizontal member and $AE = 1000 \text{ kN}$ for the spring

Fig Q 3A

| Question | Answer | CO |
|----------|---|----|
| 3A | | 07 |
| 3B. | using the stiffness matrix of two noded bar element obtain the stiffness matrix for two noded space truss element | 03 |
| 4 A | Obtain the shape functions N_1 and N_2 for three noded bar element in natural coordinate system using the shape functions in cartesian coordinate system | 02 |
| 4B | Obtain the expression to calculate stiffness matrix for three noded triangular element | 03 |
| 4C. | Obtain the matrix B at the centre for six noded triangular element with coordinates (0,0) at node 1, (1,0) at node 2 and (0,2) at node 3 | 05 |
| 5A. | Explain Gaussian Quadrature rule for area integration | 02 |
| 5B | Explain the procedure to obtain stiffness matrix for four noded isoparametric element | 04 |
| 5C | Calculate the equivalent nodal load vector for four noded element with coordinates (0,0) at node 1, (1.2, 0) at node 2, (1.2,1.2) at node 3 and (0,1.2) at node 4 due to the load varying from 5 kN/m at node 1 to 10 kN/m at node 2 acting along y-direction | 04 |