



SIXTH SEMESTER B.TECH. (ELECTRONICS & INSTRUMENTATION ENGG.)
ONLINE GRADE IMPROVEMENT/MAKE-UP EXAMINATIONS, AUGUST - 2021

SUBJECT: DIGITAL SIGNAL PROCESSING [ICE 3251]

TIME: 2 HOURS

07-08-2021

MAX.MARKS: 40

Instructions to candidates: Answer any *FOUR FULL* questions.

Missing data may be suitably assumed.

- 1A. A system has an impulse response $h[n] = a^n u[n]$, determine its output for the following inputs.
i) $x[n] = n + 1; 0 \leq n \leq 2$; ii) $x[n] = u[n]$
- 1B. State and prove i) up sampling; ii) right shifting properties of the Z-transform. (5+5)
- 2A. Determine the Z-transform for the following sequences
i) $x[n] = n \left(-\frac{1}{2}\right)^n u[n] * \left(\frac{1}{4}\right)^{-n} u[-n]$ ii) $p[n] = -u[-n - 1] + \left(\frac{1}{2}\right)^n u[n]$
- 2B. Determine sequence $x[n]$ for which
$$X[z] = \frac{0.4}{1 - 0.7z^{-1}} + \frac{0.25}{1 - 5z^{-1}}$$
where the ROC includes the unit circle. Determine $x(0)$. (5+5)
- 3A. State and prove circular time shift and time reversal properties of DFT.
- 3B. Compute 8-point DFT of the discrete time signal, $x(n) = \{1, 2, 1, 2, 1, 3, 1, 3\}$ and plot the magnitude spectrum. (5+5)
- 4A. Determine the response of the LTI system using radix-2 DIT FFT algorithm, given the input $x(n) = \{2, 3, 4, 1\}$ and the impulse response $h(n) = \{-2, -1\}$.
- 4B. Define impulse invariance transformation? What for it is used? Obtain a relation between analog and digital frequency using impulse invariance transformation. (5+5)
- 5A. Determine the poles of a lowpass Butterworth filter for $N = 3$. Sketch the location of poles on s-plane and hence determine the analog normalized transfer function of lowpass filter.

5B. Obtain the digital filter $H(Z)$ from given $H(s)$

$$H(s) = \frac{2s}{s^2 + 0.2s + 1}$$

Given the sampling period is 2 seconds. Use bilinear transformation technique.

6A. Given $H(z) = \frac{0.44z^{-1} + 0.36z^{-2} + 0.02z^{-3}}{1 + 0.4z^{-1} + 0.18z^{-2} - 0.2z^{-3}}$ Obtain the direct form I and direct form II realization. (5+5)

6B. Compare any five features of Butterworth and Chebyshev filter design methods.

(5+5)
