

END SEMESTER EXAMINATIONS (DECEMBER 2021/JANUARY 2022) - QUESTION PAPER - PART A

COURSE CODE : ICE 3153
COURSE NAME : Modern Control Theory
SEMESTER : V
DATE OF EXAM : 21/12/2021
DURATION : 45 + 5 minutes

Instructions for Students:

- (1) ANSWER ALL THE QUESTIONS.
(2) EACH QUESTION CARRIES 1 MARK.
(3) YOU ARE INSTRUCTED TO INFORM THE INVIGILATOR AFTER SUBMISSION OF THIS FORM IN THE CHAT SECTION.

* Required

* This form will record your name, please fill your name.

1

STUDENT NAME: *

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REGISTRATION NUMBER: *

3

The system matrix of the given differential equation in controllable canonical form is (1 Point)

$$\ddot{y} + 6\dot{y} + 3y = u + 2$$

- ☐ [0 1 0; 0 0 1; -6 -3 -5]
- ☐ [0 1 0; 0 0 1; -5 -3 -6]
- ☐ [-7 1 0; -2 0 1; -1 0 0]
- ☐ [1 0 0; 0 1 0; -1 -2 -7]

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The system matrix in the diagonal canonical form of the given system is
(1 Point)

$$\frac{Y(s)}{R(s)} = \frac{10}{(s-1)(s+2)}$$

- ☐ [-1 0; 0 -2]
- ☐ [0 -1; -2 0]
- ☐ [0 1; 2 0]
- ☐ [1 0; 0 2]

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The input matrix of the given transfer function in observable canonical form is (1 Point)

$$\frac{Y(s)}{R(s)} = \frac{s^2 + 7s + 26}{s^3 + 9s^2 + 26}$$

- ☐ [2; 7; 1]
- ☐ [1 7 2]
- ☐ [1; 7; 2]
- ☐ [1 7 2]

6

The output matrix of the given transfer function in diagonal canonical form is (1 Point)

$$\frac{Y(s)}{R(s)} = \frac{10}{(s-1)(s+2)}$$

- ☐ [-10 10]
- ☐ [-10 ; 10]
- ☐ [10 ; -10]
- ☐ [1 ; 1]

7

The input matrix of the given transfer function in controllable canonical form is (1 Point)

$$\frac{Y(s)}{R(s)} = \frac{s^2 + 7s + 26}{s^3 + 9s^2 + 26s + 26}$$

- ☐ [1; 0; 0]
- ☐ [1 0 0]
- ☐ [0 0 1]
- ☐ [0; 0 ; 1]

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The Input matrix in diagonal canonical form of given transfer function is (1 Point)

$$\frac{Y(s)}{R(s)} = \frac{10}{(s-1)(s+2)}$$

- ☐ [1 1]
- ☐ [0 1]
- ☐ [1 ; 1]
- ☐ [1; 0]

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Given the system the controllability matrix using Kalman test is (1 Point)

$$\dot{x}(t) = \begin{bmatrix} -1 & 3 \\ 0 & -2 \end{bmatrix} x(t) + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u(t); y(t) =$$

- ☐ [0 -2; 1 3]
- ☐ [0 3; 1 -2]
- ☐ [0 1; 3 -2]
- ☐ [1 -2; 0 3]

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The system given is (1 Point)

$$\dot{x}(t) = \begin{bmatrix} -1 & 3 \\ 0 & -2 \end{bmatrix} x(t) + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u(t); y(t) :$$

- ☐ Not completely state controllable
- ☐ One state is not controllable
- ☐ Completely state controllable
- ☐ Two states are not controllable

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The dimension of state feedback controller gain matrix for the given system is (1 Point)

$$\dot{x}(t) = \begin{bmatrix} -1 & 3 \\ 0 & -2 \end{bmatrix} x(t) + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u(t); y(t) :$$

- ☐ 2X1
- ☐ 2X2
- ☐ 1X1
- ☐ 1X2

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For the given system, the state transition matrix using Sylvester's interpolation formula is (1 Point)

$$\dot{x}(t) = \begin{bmatrix} 0 & 2 \\ 0 & -3 \end{bmatrix} x(t) + \begin{bmatrix} 1 \\ 0 \end{bmatrix} u(t)$$

- ☐ [1 0; -0.67(e^{-3t}+1) 0]
- ☐ [0 e^{-3t}; 1 -0.67(e^{-3t}+1)]
- ☐ [1 -0.67(e^{-3t}+1); 0 e^{-3t}]
- ☐ [0 1; 1 -0.67(e^{-3t}+1)]

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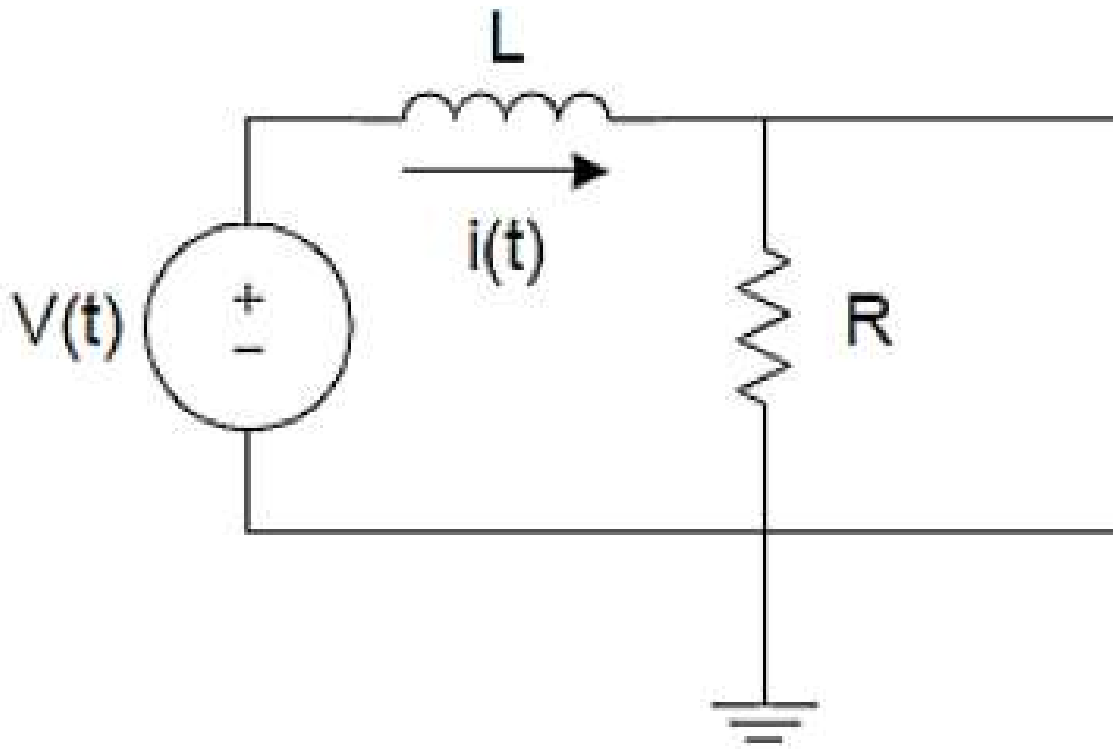
The given LTI system is (1 Point)

$$\dot{x}(t) = \begin{bmatrix} 0 & 2 \\ 0 & -3 \end{bmatrix} x(t) + \begin{bmatrix} 1 \\ 0 \end{bmatrix} u(t)$$

- ☐ Unstable
- ☐ Stable
- ☐ Marginally Stable
- ☐ Can not determine

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If $V_R(t)$ is the output of the of the RL circuit, the state equation of the circuit is (1 Point)



- ☐ $\dot{x} = V - (R/L)x$
- ☐ $\dot{x} = V/L - (R/L)x$
- ☐ $\dot{x} = Rx$
- ☐ $\dot{x} = Rx + V$

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$$\dot{x} = -2x + 1u; y = 2x + 2u$$

The transfer function of the given state model is

(1 Point)

- ☐ $(2s+6)/(s+2)$
- ☐ $(s+2)/(2s+6)$
- ☐ $1/(s+2)$
- ☐ $1/(2s+6)$

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The direct transmission matrix in the given transfer function is (1 Point)

$$\frac{Y(s)}{U(s)} = \frac{2s}{s+4}$$

- ☐ 0
- ☐ 1
- ☐ 2
- ☐ 3

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Given the system matrix A , the Vandermonde matrix is given as (1 Point)

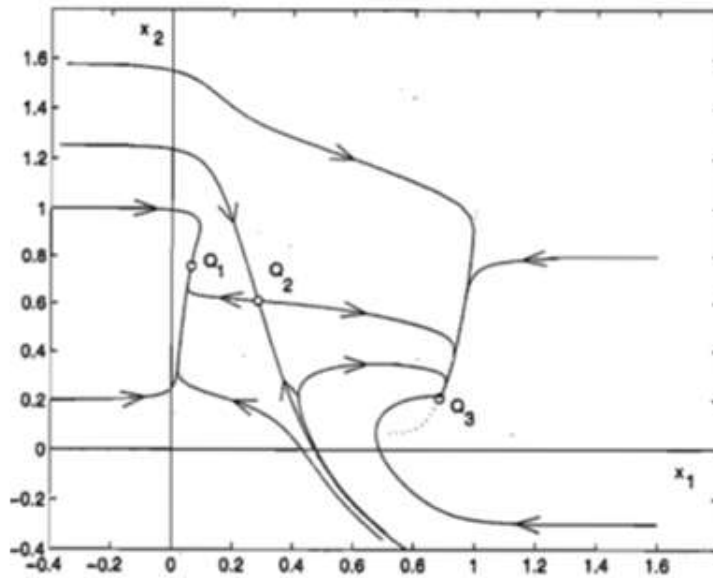
$$A = \begin{bmatrix} -1 & 0 \\ 0 & -2 \\ 0 & 0 \end{bmatrix}$$

- ☐ $P = [0 \ 0 \ 1; -1 \ -2 \ -3; 1 \ 0 \ 0]$
- ☐ $P = [0 \ 1 \ 0; 0 \ 0 \ 1; -1 \ -2 \ -3]$
- ☐ $[1 \ 1 \ 1; -1 \ -2 \ -3; 1 \ 4 \ 9]$
- ☐ $[1 \ 1 \ 1; 1 \ 4 \ 9; -1 \ -2 \ -3]$

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The phase portrait of a tunnel diode is shown in the below figure, where the equilibrium points are marked as Q1, Q2, Q3. The equilibrium point Q2 is a _____.

(1 Point)

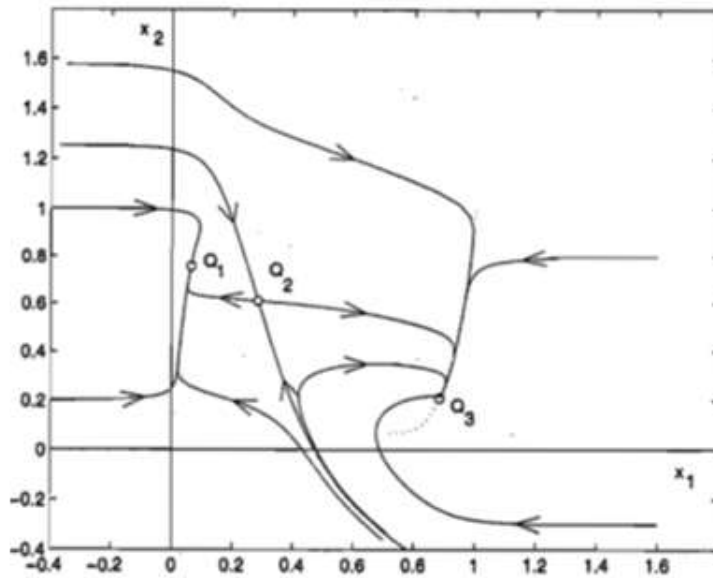


- ☐ Stable focus
- ☐ Unstable focus
- ☐ Saddle point
- ☐ Stable Node

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The phase portrait of a tunnel diode is shown in the below figure, where the equilibrium points are marked as Q1, Q2, Q3. The type of the equilibrium point Q3 is _____.

(1 Point)



- ☐ Stable focus
- ☐ Unstable Node
- ☐ Saddle point
- ☐ Stable Node

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For the nonlinear system represented by the state equation given below, the number of equilibrium points are ____.

(1 Point)

$$\dot{x}_1 = x_1 + x_1x_2, \quad \dot{x}_2 = -x_2 + x_2^2 + x_1x_2 - x_1^3$$

- ☐ 2
- ☐ 4
- ☐ 3
- ☐ None of the above

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For the nonlinear system represented by the state equation given below, the type of the equilibrium point (1, -1) is _____. (1 Point)

$$\dot{x}_1 = x_1 + x_1x_2, \quad \dot{x}_2 = -x_2 + x_2^2 + x_1x_2 - x_1^3$$

- ☐ Stable focus
- ☐ Unstable focus
- ☐ Stable node
- ☐ Unstable node

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Which of the following is not a properties of nonlinear dynamic systems?
(1 Point)

- ☐ Finite escape time
- ☐ Commutativity does not apply
- ☐ Isolated closed curves
- ☐ Unique equilibrium point

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There is _____ exist for the following nonlinear system.

(1 Point)

$$\dot{x}_1 = -x_1 + 2x_1x_2^2 + g(x_2) ; \dot{x}_2 = x_2 + 2x_1^2x_2 + h(x_2)$$

- ☐ no chaos
- ☐ no jump response
- ☐ no limit cycle
- ☐ no singular point

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A nonlinear system produces an output, **W** as the cube of its input **X**. Assume the input to be a sinusoidal signal and nonlinear output has an odd function characteristic. The term a_1 in the output **W** is _____. (1 Point)

- ☐ 0
- ☐ $3A^{3/4}$
- ☐ $3A^{2/4}$
- ☐ 1

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A nonlinear system produces an output, **W** as the cube of its input **X**. Assume the input to be a sinusoidal signal and nonlinear output has an odd function characteristic. The term b_1 in the output **W** is _____. (1 Point)

- ☐ 2
- ☐ $3A^{3/4}$
- ☐ $3A^{2/4}$
- ☐ $3A^2$

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A nonlinear system produces an output, **W** as the cube of its input **X**. Assume the input to be a sinusoidal signal and nonlinear output has an odd function characteristic. The describing function for the nonlinear component can be obtained as _____. (1 Point)

- ☐ $3A^{3/4}$
- ☐ $3A^{2/4}$
- ☐ $4A^{3/3}$
- ☐ $4A^{2/3}$

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For nonlinearities which are characterized as single valued function, N is _____ and therefore the plot of $-1/N$ will always lies on the real axis. (1 Point)

- ☐ Imaginary
- ☐ Real
- ☐ Odd
- ☐ Symmetric

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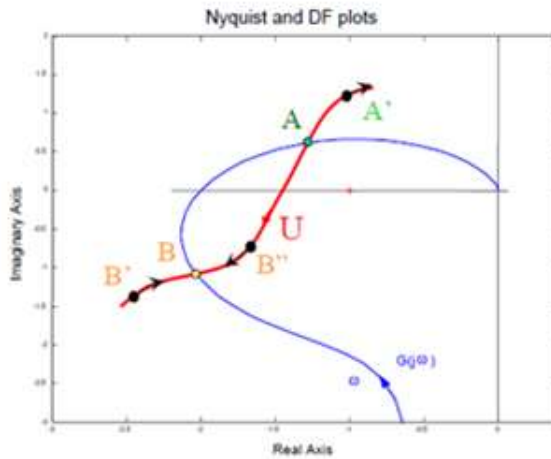
Which of the following parameters of the limit cycle cannot be used to discriminate between acceptable and dangerous oscillations? (1 Point)

- ☐ Oscillation frequency
- ☐ Phase shift in oscillation
- ☐ Oscillation magnitude
- ☐ Stability

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Analyze the given figure and select the TRUE statement for the given scenario.

(1 Point)



- ☐ Point B is not a limit cycle
- ☐ Point A and B are stable limit cycle
- ☐ Point B'' is unstable system
- ☐ Point A' is unstable system

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For the following dynamical system, what is the value of the constant **a** such that the equilibrium point is globally asymptotically stable. (1 Point)

$$\begin{aligned}\dot{x}_1 &= -x_1 + 4x_2 \\ \dot{x}_2 &= -x_1 - x_2^3.\end{aligned} \quad V = x_1^2 + ax_2^2.$$

- ☐ 3
- ☐ -5
- ☐ 4
- ☐ 5

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Which of the following statement is not correct if the linearized system is marginally stable? (1 Point)

- ☐ Linearization could not conclude about the stability
- ☐ Equilibrium point may be asymptotically stable for the nonlinear system
- ☐ All the equilibrium point may be marginally stable for the nonlinear system
- ☐ Equilibrium point may be unstable for the nonlinear system

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The sign definiteness of the Lyapunov function given below is _____.
(1 Point)

$$V(x) = x_1^2 + x_2^2 + x_3^3 - x_1x_2 + x_2x_3 - x_1x_3$$

- ☐ Negative definite
- ☐ Positive definite
- ☐ Positive semi definite
- ☐ Negative semi definite

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