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## INTERNATIONAL CENTRE FOR APPLIED SCIENCES

(MAHE)

III-SEMESTER B.Sc. (Applied Sciences) DEGREE EXAMINATION – NOV/DEC 2021

SUBJECT: MATHEMATICS-III (IMA 231)

(BRANCH: CHEMICAL/CS)

Time: 3 Hours

17 November 2021

Max. Marks: 100

- ✓ Answer ANY FIVE FULL Questions.
- ✓ Missing data, if any, may be suitably assumed

1.

a. Solve  $y(1+x^2)^{\frac{1}{2}} dy + x\sqrt{1+y^2} dx = 0$

b. Solve  $\frac{dy}{dx} - \frac{y}{x} + \operatorname{cosec} \frac{y}{x} = 0$ ,  $y(1) = 0$

c. Solve  $(4r^2s - 6)dr + r^3ds = 0$  (7+6+7)

2.

a. Solve  $(D^3 - 3D^2 + 4D - 2)y = e^x + \cos x$

b. Solve  $(ye^{xy} + 4y^3)dx + (xe^{xy} + 12xy^2 - 2y)dy = 0$ ,  $y(0) = 2$

c. Solve  $(D^2 + 1)y = \operatorname{cosec} x$  by method of variation of parameters. (7+6+7)

3.

a. Applying Taylor's series method, find the value of  $y(1.1)$  correct to four decimal places given that  $\frac{dy}{dx} = xy^{\frac{1}{3}}$ ,  $y(1) = 1$

b. Solve by the method of indicated transform  $u_{xx} + u_{xy} - 2u_{yy} = 0$  by using the transformation  $v = x + y$  and  $z = 2x - y$ .

c. Solve D.E by Laplace Transform  $y'' + 4y' + 8y = 1$   
 $y(0) = 0$ ,  $y'(0) = 1$ . (6+7+7)

4.

a. Solve by Partial fraction  $F(S) = \frac{s^3 - 3s^2 + 6s - 4}{(s^2 - 2s + 2)^2}$

b. Find the Laplace transform of a periodic function  $f(t) = \begin{cases} \frac{t}{a}, & 0 < t < a \\ \frac{1}{a}(2a - t), & a < t < 2a \end{cases}$

with  $f(t) = f(t+2a)$  and sketch the graph.

- c. Solve by the method separation of variables  $4\frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} = 3u$  given  $u(0, y) = 2e^{5y}$ . (7+6+7)

5.

- a. Find Laplace transform of saw-toothed wave of period  $T$  given  $f(t) = \frac{K}{T}t$ .

- b. Find  $L^{-1}\left\{\frac{2s-5}{4s^2+25} + \frac{4s-18}{9-s^2}\right\}$

- c. Solve  $(D^2 + 1)x = t \cos 2t$  given  $x = 0, \frac{dx}{dt} = 0$  at  $t = 0$ . (6+7+7)

6.

- a. Show that  $f(z) = \cosh z$  is analytic and hence find  $f'(z)$ .
- b. Show that the following function is harmonic also determine the corresponding analytic function  $f(z)$  and find its conjugate

$$u = \sin x \cosh y + 2 \cos x \sinh y + x^2 - y^2 + 4xy.$$

- c. Evaluate  $\int_{1-i}^{2+i} (2x + iy + 1)dz$  along  $x = t + 1$  and  $y = 2t^2 - 1$ . (6+7+7)

7.

- a. Find all the Taylor's and Laurent's series of  $f(z) = \frac{3-2z}{z^2-3z+2}$  at  $z = 0$

- b. Evaluate by Residue  $\oint \frac{z+2}{z(z-1)}dz$  where i).  $c : |z| = \frac{1}{2}$

ii).  $c : |z| = 2$       iii).  $c : |z+1| = \frac{1}{2}$

- c. Solve the linear differential Equation  $y''(x) + 2y'(x) + y(x) = x$ ,  $y(0) = -3$ ,  $y'(0) = 0$  (6+7+7)

8.

- a. Solve  $\frac{dy}{dx} + y = y^2(\cos x - \sin x)$

- b. Solve by Convolution Theorem  $F(S) = \frac{1}{(s^2+4)(s+1)^2}$

- c. State and prove Cauchy's integral formula. (6+7+7)

