



## FOURTH SEMESTER BTECH. (E & C) DEGREE END SEMESTER EXAMINATION

JUNE 2022

SUBJECT: ELECTROMAGNETIC WAVES (ECE -2252 )

TIME: 3 HOURS

MAX. MARKS: 50

### Instructions to candidates

- Answer **ALL** questions.
- Missing data may be suitably assumed.

Q. No.	Questions	M*	C*	A*	B*
1A.	Derive an expression for divergence using Gauss's Law. Show all intermediate steps.	4	1	1,2 ,3, 4,1 8	3
1B.	The spherical region, $0 < r < 10$ cm, contains a uniform volume charge density of $4\mu\text{C}/\text{m}^3$ . (i) Find $Q_{\text{tot}}$ , $0 < r < 10$ cm (ii) Find $D_r$ , $0 < r < 10$ cm (iii) The uniform volume charge density, $\rho_v = -3/(r^3 + 0.001)$ nC/m <sup>3</sup> , exists for $10 \text{ cm} < r < r_0$ . Find $r_0$ so that the total charge in the region $0 < r < r_0$ is zero	3	1	1,2 ,3, 4,1 8	4
1C.	If $\vec{G} = 5 r \sin^2 \theta \cos^2 \phi \vec{a}_r$ , evaluate both sides of the divergence theorem for the region $r \leq 2$ . Show all intermediate steps.	3	1	1,2 ,3, 4,1 8	4
2A.	Two extensive homogeneous isotropic dielectrics meet on plane $z = 0$ . For $z > 0$ , $\epsilon_{r1} = 4$ and for $z < 0$ , $\epsilon_{r2} = 3$ . A uniform electric field $\vec{E}_1 = 5\vec{a}_x - 2\vec{a}_y + 3\vec{a}_z$ kV/m exists for $z \geq 0$ . Find (i) $\vec{E}_2$ for $z \leq 0$ (ii) The angles $E_1$ and $E_2$ make with the interface (iii) The energy densities (in J/m <sup>3</sup> ) in both dielectrics (iv) The energy within a cube of side 2 m centered at (3, 4, -5)	4	1	1,2 ,3, 4,1 8	4
2B.	Given the electrical potential $V = \frac{10}{r^2} \sin \theta \cos \phi$ , (i) Find the electric flux density $\vec{D}$ at (2, $\pi/2$ , 0). (ii) Calculate the work done in moving a 10 $\mu\text{C}$ charge from point A(1, 30°, 120°) to B(4, 90°, 60°).	3	1	1,2 ,3, 4,1 8	4

2C.	Sketch the magnitudes of voltage and current for two wavelengths, on a dissipation less two wire transmission line when: (i) Load impedance is equal to zero (ii) Load impedance is equal to infinity (iii) load impedance is equal to characteristic impedance	3	4	1,2 ,3, 4,1 8	3
3A.	Write the mathematical expression equating left hand side and right hand side of Stoke's theorem and explain each sides.	2	1	1,2 ,3, 4,1 8	2
3B.	State and prove Vector Poynting theorem	3	2	1,2 ,4, 18	2
3C.	A 9375 MHz uniform plane wave is propagating in polystyrene. If electric field intensity is 20 V/m and material is assumed to be lossless, find  (a) Phase constant $\beta$ (b) Wavelength $\lambda$ (c) Wave phase velocity (velocity of propagation) $v_p$ (d) Intrinsic impedance $\eta$ (e) Propagation constant $k$ (f) Magnetic field intensity $H$  For polystyrene relative permittivity is 2.56 and relative permeability is 1.	5	2	1,2 ,4, 18	4
4A.	Find the amplitude of displacement current density in metallic conductor at 60Hz if $\epsilon = \epsilon_0$ , $\mu = \mu_0$ , $\sigma = 5.8 \times 10^7$ S/m and $J = \sin(377t - 117.1z)10^6 \mathbf{a}_x$ A/m <sup>2</sup> .	2	2	1,2 ,4, 18	4
4B.	Obtain the Maxwell's equations from Faraday's law of electromagnetic induction.	3	2	1,2 ,4, 18	3
4C.	From fundamentals derive complete expressions for voltage and current at any point on a dissipation less two wire transmission line in trigonometric form.	5	4	1,2 ,3, 4,1 8	3
5A.	At a frequency of 1GHz the characteristic impedance and propagation constant of a two wire transmission line are $(179.44 + j26.5)\Omega$ and $(0.051 + j0.273)/m$ respectively. Determine the primary parameters of the transmission line.	2	4	1,2 ,3, 4,1 8	4
5B.	A 50 Ohm lossless line connects a signal of 100KHz to a load of $100\Omega$ . The load power is 100 mW. Calculate the (i) Voltage reflection coefficient (ii) VSWR (iii) Position of first $V_{min}$ and $V_{max}$ . (iv) Impedance at $V_{min}$ and $V_{max}$ and the values of $V_{min}$ and $V_{max}$ .	4	4	1,2 ,3, 4,1 8	4

5C.	A load impedance of $(73-j80)\Omega$ is required to be matched to a $50\Omega$ coaxial line having lossless dielectric with $\epsilon_r = 4$ , using a $50\Omega$ short circuit shunt stub at 500 MHz. Determine the length and position of the inductive stub using Smith chart.	4	4	1,2 ,3, 4,1 8	4

**M\*--Marks, C\*--CLO, A\*--AHEP LO, B\* Blooms Taxonomy Level**