

## DEPARTMENT OF MECHATRONICS VI SEMESTER B. TECH (MECHATRONICS) End Semester Assessment– May 2022

# **Subject: Artificial Intelligence**

## Subject Code: MTE 4059

Time: 180 Minutes

## **Exam Time:**

#### MAX. MARKS: 50

#### **Instructions to Candidates:**

\* Answer ALL the questions.

✤ Missing data may be suitably assumed and justified.

								Μ	CO	PO	LO	BL
1A	For the multilayer feedforward network, perform single step error						5	2	1	1	3	
	back	backpropagation and find out the updated weight w <sub>212</sub> for the data given										
	belo	below. Z is the input vector, V and W are the weight matrices for hidden										
	and	d output layer respectively.										
	<i>Z</i> =	$Z = \begin{bmatrix} 1\\3\\-1 \end{bmatrix} \qquad V = \begin{bmatrix} 1 & 0 & 2\\2 & 3 & 1 \end{bmatrix} \qquad \qquad W = \begin{bmatrix} 1 & 1\\0 & 1 \end{bmatrix}$										
	Desi	Desired output is $= \begin{bmatrix} 1 & 0 \end{bmatrix}$										
	Consider the first layer to consist of unipolar sigmoid neurons and											
	seco	nd layer to	o consist o	f softmax	neurons.	Assume learnir	ng rate as 1 and					
	no b	ias inputs										
1B	Illus	trate an a	lgorithm	mentionin	g the step	os involved to	train a neural	3	3	2	2	4
	network with ADAM type of optimizer. Assume there are 'n' no. of											
	training vectors with 'm' no. of input features, use of sigmoid activation											
	function and squared error type of loss.											
1C	Explain two main advantages of a CNN over a fully connected DNN for						ected DNN for	2	4	1	1	2
	image classification											
2A	Classification of iris plants into three different species (iris-setosa, iris-						4	2,3	2	2	4	
	versicolor and iris-virginica) has to be done using multilayer feedforward											
	neural network, based on certain features. The classic iris dataset includes											
	three species with 50 samples of each (a total of 150 samples). First five											
	samples are shown below:											
		Sepal	Sepal	Petal	Petal							
		Length	Width	Length	Width							
	Id	(Cm)	(Cm)	(Cm)	(Cm)	Species						
	1	5.1	3.5	1.4	0.2	Iris-setosa						
	2	4.9	3	1.4	0.2	Iris-setosa					1	

	3	4.7	3.2	1.3	0.2	Iris-setosa						
	4	4.6	3.1	1.5	0.2	Iris-setosa						
	5	5	3.6	1.4	0.2	Iris-setosa						
	Sup	Supposing that you have designed a network with an input layer of 20										
	neur	neurons, hidden layer of 10 neurons, followed by the output layer, answer										
	the following questions:											
	i.	i. What is the shape (matrix dimension) of the input training data										
		consid	ering 90%	of the sar	nples are u	used for trainir	ng?					
	ii.	ii. What is the shape of the network output matrix?										
	iii.	iii. What is the shape of the weight matrix connecting the hidden layer										
		to the output layer?										
	iv.	iv. Identify suitable activation functions for the neurons of the three										
		layers.										
	v.	You fi	nd that the	network e	exhibits a	high bias and a	a low variance.					
		Descri	be what ca	an be done	to solve t	he problem.						
2B	Perf	orm singl	e step He	bbian lear	ming of a	single neuror	n network and	3	2	1	1	3
	calc	ulate the u	pdated we	eight. Cons	sider input	t vector as						
	X=[	1 -1] <sup>t</sup> , init	ial weight	vector as	$[2 - 1]^t$ , le	arning rate as	1 and sigmoid					
	activ	vation fund	ction.									
2C	Expl	ain the RE	SNET mod	el of convo	olutional ne	ural network. H	ighlight the key	3	4	1	1	2
	impr	ovements i	n this netw	ork to the p	previous on	les.						
3A	Consider a CNN composed of three convolutional layers, each with $3 \times 3$						ich with $3 \times 3$	4	4	1	1	3
	kernels, a stride of 2, and zero padding. The lowest layer outputs 100 feature						buts 100 feature					
	maps, the middle one outputs 200, and the top one outputs 400. The input images are RGB images of $200 \times 300$ pixels. What are the total number of trainable parameters in the CNN? Bias inputs can be neglected.											
3B	Justify the correctness or otherwise of the statement:							3	3	2	2	4
	While training a multilayer feedforward neural network with						network with	_	_			
	backpropagation training algorithm, it is okay to initialize all the weights											
	to 'one'.											
3C	Cons	sider fuzzy	sets A and	B defined	in the unive	erse of discours	e U and V:	3	5	1	1	3
		-										
				$A = \frac{1}{2}$	$+\frac{0.5}{0.5}+\frac{0.5}{0.5}$	1						
		$A = \frac{1}{0} + \frac{1}{1} + \frac{1}{2}$										
				0 1	04 0	13						
				$B = \frac{0.1}{1}$	$\frac{1}{2} + \frac{0.1}{2} + \frac{0}{2}$	3						
				1	-	0						
	Perfe	orm <b>Diene</b> s	s-Rescher i	implication	n to interp	ret 'if A then B	,					
	Forn	Formula:										
	$\mu_{Q_I}$	$_{\scriptscriptstyle D}(x,y) =$	max[1 - ]	$\mu_{FP_1}(x), \mu$	$u_{FP_2}(y)]$							
4A	Cons	sider a two	o-input-one	-output fu	zzv system	that is constr	ucted from the	5	5	1	1	3
	follo	wing two r	ules:			15 001151		-	-	-	-	-
		C										

if $x_1$ is $A_1$ and $x_{2 is} A_2$ , then y is $A_1$					
if $x_1$ is $A_2$ and $x_2$ is $A_1$ , then y is $A_2$					
Where, A1 and A2 are fuzzy sets with membership functions:					
$\left( 1 - \left  \frac{u}{2} \right  if - 2 \le u \le 2 \right)$					
$\mu_{A_1(u)} = \begin{cases} 1 &  u  \\ 1 &  u  \\ 2 &  u  \\ 1 &  u  \\ 2 &  u  \\ 1 &  u  \\$					
Suppose that the input to the fuzzy system is $(x_1^*, x_2^*) = (0.8, 1.4)$ and we use the singleton fuzzifier, Determine the output y* in the following situation: Mamdani Minimum inference engine with mean max membership defuzzifier					
The set of input training vectors to a perceptron is as follows:	3	3	1	1	2
$X_1 = \begin{bmatrix} 1 \\ -1.5 \end{bmatrix}  X_2 = \begin{bmatrix} 0.5 \\ 2 \end{bmatrix}$					
The initial weight vector W1 is assumed to be: $W_1 = \begin{bmatrix} 1.5\\ -1 \end{bmatrix}$					
The learning constant is assumed to be 0.1. The desired response for X1 is $d1=$ -1, $d2=$ -1 respectively. Update the weights according to perceptron learning algorithm using the signum activation function.					
Describe in which case would you want to use the following activation functions: leaky ReLU and softmax.	2	5	1	1	3
You are asked to develop a controller to regulate the temperature of a room. Knowledge of the system allows you to construct a simple rule of thumb: when the temperature is HOT then cool room down by turning the fan at the fast speed, or, expressed in rule form, IF temperature is HOT, THEN fan should turn FAST. Fuzzy sets for hot temperature and fast fan speed can be developed: for example $H = hot = \left\{ \frac{0}{60} + \frac{0.1}{70} + \frac{0.7}{80} + \frac{0.9}{90} + \frac{1}{100} \right\}$ represents universe X in °F, and $F = fast = \left\{ \frac{0}{0} + \frac{0.2}{1} + \frac{0.5}{2} + \frac{0.9}{3} + \frac{1}{4} \right\}$ represents universe Y in 1000 rpm. (a) From these two fuzzy sets construct a relation for the rule using classical implication. (b) Suppose a new rule uses a slightly different temperature, say "moderately hot." and is	4	5	2	1	4
	$\begin{aligned} & \text{if } x_1 \text{ is } A_1 \text{ and } x_2 \text{ is } A_2, \text{ then } y \text{ is } A_1 \\ & \text{if } x_1 \text{ is } A_2 \text{ and } x_2 \text{ is } A_1, \text{ then } y \text{ is } A_2 \end{aligned}$ Where, A1 and A2 are fuzzy sets with membership functions: $\begin{aligned} & \mu_{A_1(u)} = \begin{cases} 1 - \left  \frac{u}{2} \right  \text{ if } -2 \leq u \leq 2 \\ 1 - \left  \frac{u}{2} - 1 \right  \text{ if } 0 \leq u \leq 4 \end{aligned}$ Suppose that the input to the fuzzy system is $(x_1^*, x_2^*) = (0.8, 1.4)$ and we use the singleton fuzzifier. Determine the output y* in the following situation: Mamdani Minimum inference engine with mean max membership defuzzifier The set of input training vectors to a perceptron is as follows: $\begin{aligned} & X_1 = \begin{bmatrix} 1 \\ -1.5 \end{bmatrix}  X_2 = \begin{bmatrix} 0.5 \\ 2 \end{bmatrix} \end{aligned}$ The initial weight vector W1 is assumed to be: $\begin{aligned} & W_1 = \begin{bmatrix} 1.5 \\ -1 \end{bmatrix} \end{aligned}$ The learning constant is assumed to be 0.1. The desired response for X1 is d1= -1, d2= -1 respectively. Update the weights according to perceptron learning algorithm using the signum activation functions: leaky ReLU and softmax. You are asked to develop a controller to regulate the temperature of a room. Knowledge of the system allows you to construct a simple rule of thumb: when the temperature is HOT then cool room down by turning the fan at the fast speed, or, expressed in rule form, IF temperature and fast fan speed can be developed: for example $\begin{aligned} H = hot = \left\{ \frac{0}{60} + \frac{0.1}{70} + \frac{0.7}{80} + \frac{0.9}{90} + \frac{1}{100} \right\} \text{ represents universe X in °F, and} \\ F = fast = \left\{ \frac{0}{0} + \frac{0.2}{1} + \frac{0.5}{2} + \frac{0.9}{3} + \frac{1}{4} \right\} \text{ represents universe Y in 1000 rpm.} \\ (a) Suppose a new rule uses a slightly different temperature, say "moderately hot," and is \begin{aligned} & W_1 = W_1 = W_2 + W_2$	$\begin{aligned} & \text{if } x_1 \text{ is } A_1 \text{ and } x_2 \text{ is } A_2, \text{ then } y \text{ is } A_1 \\ & \text{if } x_1 \text{ is } A_2 \text{ and } x_{2 \text{ is }} A_1, \text{ then } y \text{ is } A_2 \end{aligned}$ Where, A1 and A2 are fuzzy sets with membership functions: $\begin{aligned} & \mu_{A_1(u)} = \begin{cases} 1 - \left  \frac{u}{2} \right  \text{ if } -2 \leq u \leq 2 \\ 1 - \left  \frac{u}{2} -1 \right  \text{ if } 0 \leq u \leq 4 \end{aligned}$ Suppose that the input to the fuzzy system is $(x_1^*, x_2^*) = (0.8, 1.4)$ and we use the singleton fuzzifier, Determine the output y* in the following situation: Mandani Minimum inference engine with mean max membership defuzzifier The set of input training vectors to a perceptron is as follows: $\begin{aligned} & X_1 = \begin{bmatrix} 1 \\ -1, 5 \end{bmatrix}  X_2 = \begin{bmatrix} 0.5 \\ 2 \end{bmatrix} \end{aligned}$ The initial weight vector W1 is assumed to be: $\begin{aligned} & W_1 = \begin{bmatrix} 1.5 \\ -1 \end{bmatrix} \end{aligned}$ The learning constant is assumed to be 0.1. The desired response for X1 is d1= -1, d2= -1 respectively. Update the weights according to perceptron learning algorithm using the signum activation function. Describe in which case would you want to use the following activation functions: leaky ReLU and softmax. You are asked to develop a controller to regulate the temperature of a room. Knowledge of the system allows you to construct a simple rule of thumb: when the temperature is HOT then cool room down by turning the fan at the fast speed, or, expressed in rule form, IF temperature and fast fan speed can be developed: for example. $\begin{aligned} H = hot = \left\{ \frac{0}{0} + \frac{0.2}{11} + \frac{0.2}{20} + \frac{0.9}{3} + \frac{1}{100} \right\} \\ \text{represents universe X in GF, and} \\ F = fast = \left\{ \frac{0}{0} + \frac{0.2}{11} + \frac{0.5}{20} + \frac{0.9}{3} + \frac{1}{4} \right\} \\ \text{represents universe Y in 1000 rpm.} \\ (a) From these two fuzzy sets construct a relation for the rule using classical implication.         $	$\begin{aligned} & \text{if } x_1 \text{ is } A_1 \text{ and } x_{2 \text{ is }} A_2, \text{ then } y \text{ is } A_1 \\ & \text{if } x_1 \text{ is } A_2 \text{ and } x_{2 \text{ is }} A_1, \text{ then } y \text{ is } A_2 \end{aligned}$ $\begin{aligned} & \text{Where, A1 and A2 are fuzzy sets with membership functions:} \\ & \mu_{A_1(w)} = \begin{cases} 1 - \left  \frac{w}{2} \right  \text{ if } -2 \le u \le 2 \\ 1 - \left  \frac{w}{2} -1 \right  \text{ if } 0 \le u \le 4 \end{aligned}$ $\begin{aligned} & \text{Suppose that the input to the fuzzy system is (x_1^*, x_2^*) = (0.8, 1.4) \text{ and we use the singleton fuzzifier,} \\ & \text{Determine the output y* in the following situation:} \\ & \text{Mandani Minimum inference engine with mean max membership defuzzifier} \end{aligned}$ $\begin{aligned} & \text{The set of input training vectors to a perceptron is as follows:} \qquad 3 \qquad 3 \end{aligned}$ $\begin{aligned} & X_1 = \begin{bmatrix} 1 \\ -1.5 \end{bmatrix}  X_2 = \begin{bmatrix} 0.5 \\ 2 \end{bmatrix} \end{aligned}$ $\begin{aligned} & \text{The initial weight vector W1 is assumed to be:} \\ & W_1 = \begin{bmatrix} 1.5 \\ -1 \end{bmatrix} \end{aligned}$ $\begin{aligned} & \text{The learning constant is assumed to be to be 0.1. The desired response for X1 is d1= -1, d2= -1 respectively. Update the weights according to perceptron learning algorithm using the signum activation function. \end{aligned}$ $\begin{aligned} & \text{You are asked to develop a controller to regulate the temperature of a room. Knowledge of the system allows you to construct a simple rule of thumb: when the temperature is HOT then cool room down by turning the fan at the fast speed, or, expressed in rule form, IF temperature and fast fan speed can be developed: for example \\ & H = hot = \left\{ \frac{0}{60} + \frac{0.2}{1} + \frac{0.5}{20} + \frac{0.9}{3} + \frac{1}{4} \right\} \end{aligned}$ represents universe X in *F, and $F = faast = \left\{ \frac{0}{0} + \frac{0.2}{1} + \frac{0.5}{2} + \frac{0.9}{3} + \frac{1}{4} \right\}$ represents universe Y in 1000 rpm. $\end{aligned}$ (a) From these two fuzzy sets construct a relation for the rule using classical implication. \end{aligned}	$\begin{aligned} & \text{if } x_1 \text{ is } A_1 \text{ and } x_2 \text{ is } A_2 \text{ then } \text{y is } A_2 \\ & \text{if } x_1 \text{ is } A_2 \text{ and } x_2 \text{ is } A_1 \text{ then } \text{y is } A_2 \end{aligned}$ Where, A1 and A2 are fuzzy sets with membership functions: $\begin{aligned} & \mu_{A_1(u)} = \begin{cases} 1 - \left  \frac{u}{2} \right  \text{ if } -2 \le u \le 2 \\ 1 - \left  \frac{u}{2} - 1 \right  \text{ if } 0 \le u \le 4 \end{aligned}$ Suppose that the input to the fuzzy system is $(x_1^*, x_2^*) = (0.8, 1.4)$ and we use the singleton fuzzifier, Determine the output $y^*$ in the following situation: Mandani Minimum inference engine with mean max membership defuzzifier The set of input training vectors to a perceptron is as follows: $\begin{aligned} & 3 & 3 & 1 \\ X_1 = \begin{bmatrix} -1 \\ -1.5 \end{bmatrix}  X_2 = \begin{bmatrix} 0.5 \\ 2 \end{bmatrix} \end{aligned}$ The initial weight vector W1 is assumed to be: $\begin{aligned} & W_1 = \begin{bmatrix} 1.5 \\ -1 \end{bmatrix} \end{aligned}$ The learning constant is assumed to be 0.1. The desired response for X1 is d1= -1, d2= -1 respectively. Update the weights according to perceptron learning algorithm using the signum activation function. Describe in which case would you want to use the following activation functions: leaky ReLU and softmax. $\begin{aligned} & 2 & 5 & 1 \\ \text{You are asked to develop a controller to regulate the temperature of a room. Knowledge of the system allows you to construct a simple rule of thumb: when the temperature is HOT then cord room down by turning the fan at the fast speed, or, expressed in rule form. IF temperature is HOT, THEN fan should turn FAST. Fuzzy sets for hot temperature and fast fan speed can be developed: for example \\ H = hot = \left\{ \frac{0}{60} + \frac{0.2}{1} + \frac{0.5}{2} + \frac{0.9}{3} + \frac{1}{10} \right\}$ represents universe X in sF, and $F = fast = \left\{ \frac{0}{0} + \frac{0.2}{1} + \frac{0.5}{2} + \frac{0.9}{3} + \frac{1}{4} \right\}$ represents universe Y in 1000 rpm. (a) From these two fuzzy sets construct a relation for the rule using classical implication. (b) Suppose a new rule uses a slightly different temperature, say	$\begin{aligned} & \text{if } x_1 \text{ is } A_1 \text{ and } x_{216} A_2, \text{ then } y \text{ is } A_1 \\ & \text{if } x_1 \text{ is } A_2 \text{ and } x_{216} A_1, \text{ then } y \text{ is } A_2 \end{aligned}$ $\text{Where, A1 and A2 are fuzzy sets with membership functions:} \\ & \mu_{A_1(u)} = \begin{cases} 1 - \left  \frac{u}{2} \right  \text{ if } -2 \le u \le 2 \\ 1 - \left  \frac{u}{2} -1 \right  \text{ if } 0 \le u \le 4 \end{aligned}$ $\text{Suppose that the input to the fuzzy system is } (x_i^*, x_i^*) = (0.8, 1.4) \text{ and we use the singleton fuzzifier.} \end{aligned}$ $\text{The set of input training vectors to a perceptron is as follows:} \qquad 3 \qquad 3 \qquad 1 \qquad 1$

	expressed by the fuzzy membership function for "moderately hot," or $H' = \left\{ \frac{0}{60} + \frac{0.2}{70} + \frac{1}{80} + \frac{1}{90} + \frac{1}{100} \right\}$ Using max-min composition, find the resulting fuzzy fan speed. Formula: $\mu_{P \circ Q}(x, z) = \max_{y \in V} \min[\mu_P(x, y), \mu_Q(y, z)]$					
5B	Let U and V be universe of discourse and A and B are fuzzy sets in U and V. A fuzzy If-Then rule is formed as: x is A' If x is A then y is B Use generalized Modes Ponens to derive a conclusion in the form y is B', where, $A \rightarrow B$ is interpreted using Mamdani Product implication $U = \{x_1, x_2, x_3\}$ $V = \{y_1, y_2\}$ $A = \{\frac{0.5}{x_1} + \frac{1}{x_2} + \frac{0.6}{x_3}\}$ $B = \{\frac{1}{y_1} + \frac{0.4}{y_2}\}$ $A' = \{\frac{0.6}{x_1} + \frac{0.9}{x_2} + \frac{0.7}{x_3}\}$	4	5	1	1	3
5C	Given two fuzzy sets A and B in universe of discourse X and Y, develop the fuzzy relation with minimum operator. $A = \left\{ \frac{0.2}{1} + \frac{0.3}{2} + \frac{0.7}{3} \right\}  B = \left\{ \frac{0.9}{1} + \frac{0.4}{2} \right\}$	2	5	1	1	3