



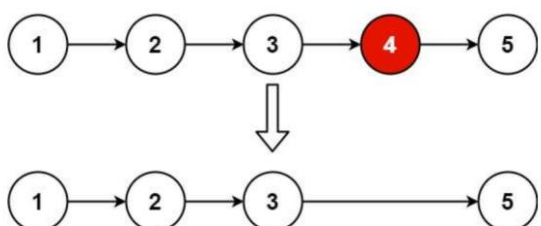
**III SEMESTER B.TECH. END SEMESTER EXAMINATION**  
**DECEMBER 2022**

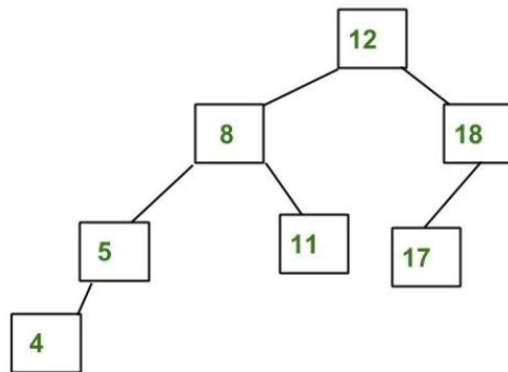
**SUBJECT: DATA STRUCTURES AND ALGORITHMS [MTE 2151]**

Date of Exam: **19/12/2022** Time of Exam: **02:00 PM – 05:00 PM** Max. Marks: **50**

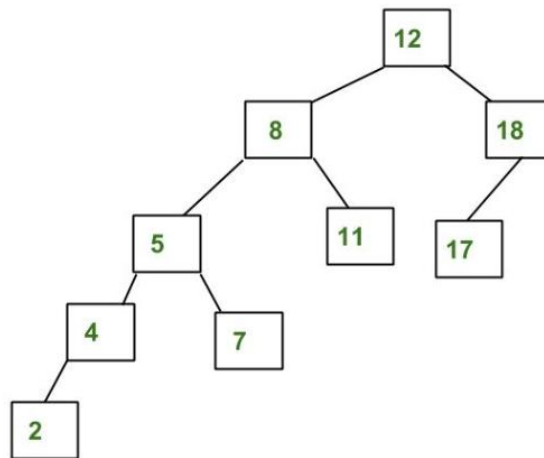
**Instructions to Candidates:**

- ❖ Answer ALL the questions & missing data may be suitably assumed

| Q.N<br>O. | QUESTION   | M | CO | PO    | LO  | BL  |
|-----------|--|---|----|-------|-----|-----|
| 1.        | Illustrate the Enqueue and Dequeue operations on a Queue.  | 2 | 1  | 1,2   | 1,2 | 4   |
| 2.        | Convert $(234)_{10}$ into binary and present the process of conversion using a Stack.  | 3 | 1  | 1,2   | 1,2 | 3,4 |
| 3.        | Develop an algorithm for the removal of the Node 4 in the first singly linked list to result into the second singly linked list as illustrated in the figure below.<br> | 5 | 2  | 1,2,3 | 1,2 | 6   |
| 4.        | Create an algorithm to find the sum of all the elements in an array of size 10.  | 2 | 2  | 1,2,3 | 1,2 | 6   |
| 5.        | Compute the time complexity of the code snippet given below.<br><pre>int a = 0; for (i = 0; i &lt; N; i++) {     for (j = N; j &gt; i; j--) {         a = a + i + j;     } }</pre>   | 3 | 2  | 1,2,3 | 1,2 | 4   |
| 6.        | Which of the following trees has an imbalance (Tree1/ Tree2)? Perform balancing on the trees if any.   | 5 | 2  | 1,2,3 | 1,2 | 4   |



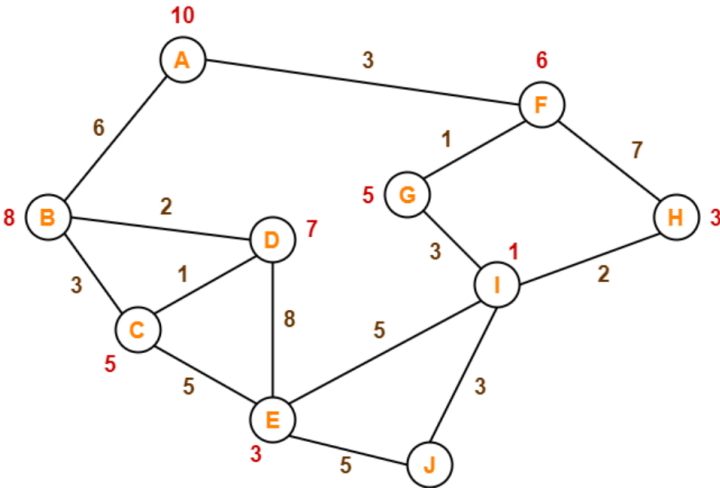
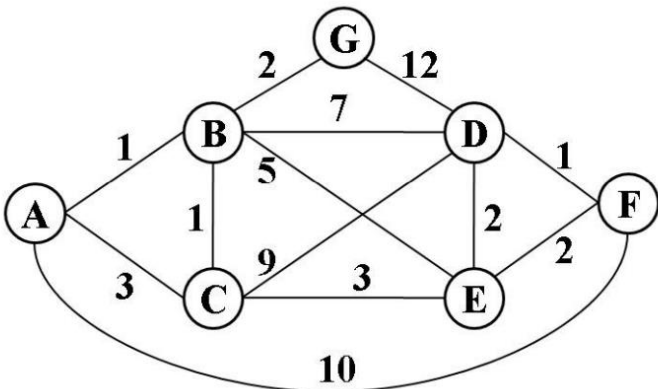
Tree1



Tree2

|     |  |   |   |       |     |     |
|-----|--|---|---|-------|-----|-----|
| 7.  | Elaborate on the Chaining scheme in Maps with a suitable exam.   | 2 | 2 | 1,2,3 | 1,2 | 3,4 |
| 8.  | Describe the difference between average-case and worst-case analysis of algorithms, and give an example of an algorithm whose average-case running time is different from its worst-case running time and state the reason.  | 3 | 3 | 1,2,3 | 1,2 | 4   |
| 9.  | A $k$ -multiset is a set of $n$ elements in which $k$ distinct elements each appear exactly $n/k$ times.<br><br>For example, $\{1,1,2,2,3,3,4,4,5,5\}$ is a sorted 5-multiset of size $n=10$ .<br><br>Write a Pseudo-code to sort a $k$ -multiset of size $n$ .<br><br>For convenience, you may assume that $n = 2^i$ and that $k = 2^j$ for some $i \geq j$ . | 5 | 3 | 1,2,3 | 1,2 | 4   |
| 10. | Suppose you are given an array $A$ of size $n$ that either contains all zeros or $2n/3$ zeros and $n/3$ ones in some arbitrary order.  | 2 | 3 | 1,2,3 | 1,2 | 3   |



|     |   |   |   |       |     |   |
|-----|---|---|---|-------|-----|---|
|     | Give an exact lower bound in terms of $n$ (not using asymptotic notation) on the worst-case running time of any deterministic algorithm that is tasked to determine whether A contains any ones.  |   |   |       |     |   |
| 11. | <p>Consider the problem of searching for genes in DNA sequences using Horspool's algorithm. A DNA sequence consists of a text on the alphabet {A, C, G, T} and the gene or gene segment is the pattern.</p> <p>a. Construct the shift table for the following gene segment of your chromosome 10: <b>TCCTATTCTT</b></p> <p>b. Locate the above pattern in the following DNA sequence:<br/><b>TTATAGATCTCGTATTCTTTTATAGATCTCCTATTCTT</b></p> | 3 | 4 | 1,2,3 | 1,2 | 4 |
| 12. | <p>For the input 30, 20, 56, 75, 31, 19 and hash function <math>h(K) = K \bmod 11</math></p> <p>a. Construct the open hash table (chaining mechanism).</p> <p>b. Find the largest number of key comparisons in a successful search in this table.</p> <p>c. Find the average number of key comparisons in a successful search in this table.</p>  | 5 | 4 | 1,2,3 | 1,2 | 4 |
| 13. | <p>Deduce the shortest path from A to J using the A* algorithm. The weights along the edges are costs incurred for traversing the edge and the weight along the nodes represents the heuristics of the corresponding node.</p>    | 2 | 5 | 1,2,3 | 1,2 | 4 |
| 14. | <p>Compute the shortest path from Node A to Node F using the Dijkstra's algorithm</p>    | 3 | 5 | 1,2,3 | 1,2 | 4 |



15. Given a binary matrix where 0 represents water and 1 represents land, and connected ones form an island.

The below image highlights water in blue and land in gray in a  $10 \times 10$  matrix. There are a total of **five islands** present in the below matrix. They are marked by the numbers 1–5 in the image below.

|   |   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|
| 1 |   | 2 |   |   |   | 3 | 3 | 3 | 3 |
|   |   | 2 |   | 2 |   | 3 |   |   |   |
| 2 | 2 | 2 | 2 |   |   | 3 |   |   |   |
| 2 |   |   | 2 |   | 3 |   |   |   |   |
| 2 | 2 | 2 | 2 |   |   |   | 5 | 5 | 5 |
|   | 2 |   | 2 |   |   | 5 | 5 | 5 | 5 |
|   |   |   |   |   | 5 | 5 | 5 |   |   |
|   |   |   | 4 |   |   | 5 | 5 | 5 |   |
| 4 |   | 4 |   | 4 |   |   | 5 |   |   |
| 4 | 4 | 4 | 4 |   |   |   | 5 | 5 | 5 |

Develop an algorithm using searching techniques to count the total islands.

5

5

1,2,3

1,2

4