

Exam Date & Time: 22-May-2023 (02:30 PM - 05:30 PM)



## MANIPAL ACADEMY OF HIGHER EDUCATION

IV Semester End Semester Examination  
Engineering Mathematics IV (MAT 2256)

**LINEAR CONTROL THEROY [AAE 2257]**

**Marks: 50**

**Duration: 180 mins.**

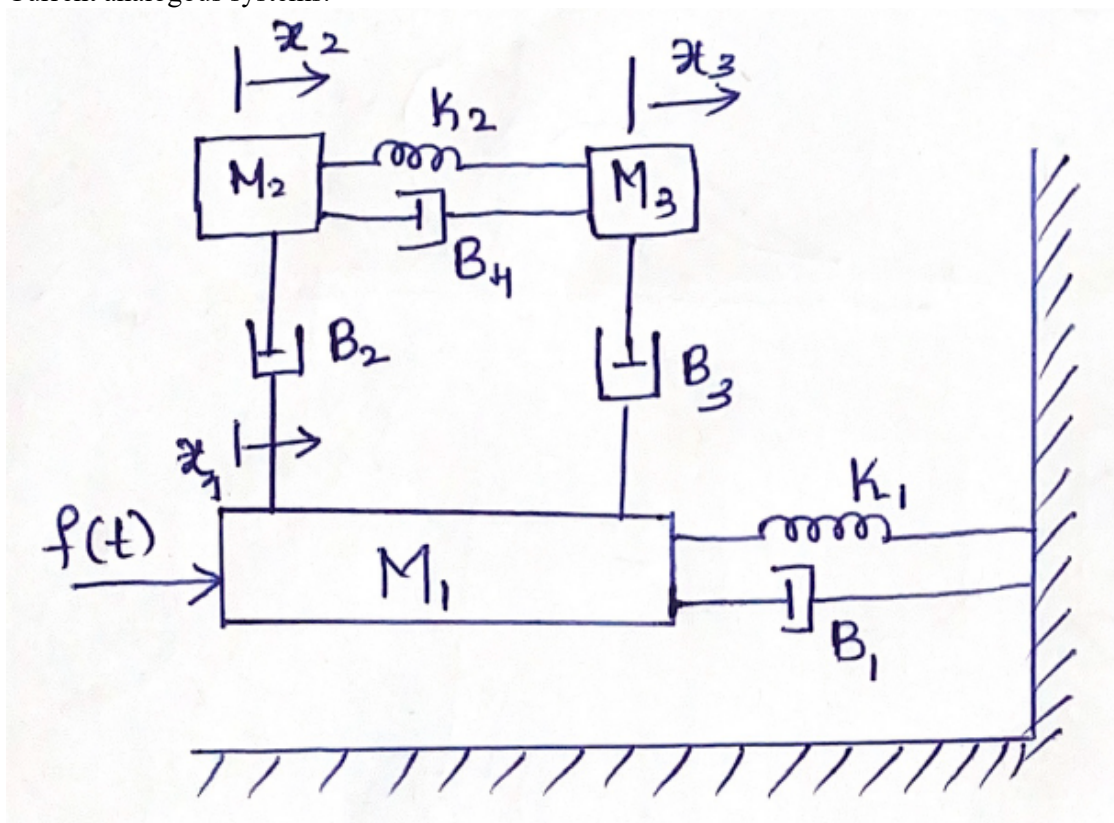
### Descriptive Questions

**Answer all the questions.**

Section Duration: 180 mins

- 1) Write the differential equations governing the system and draw its Force-Voltage and Force-Current analogous systems.

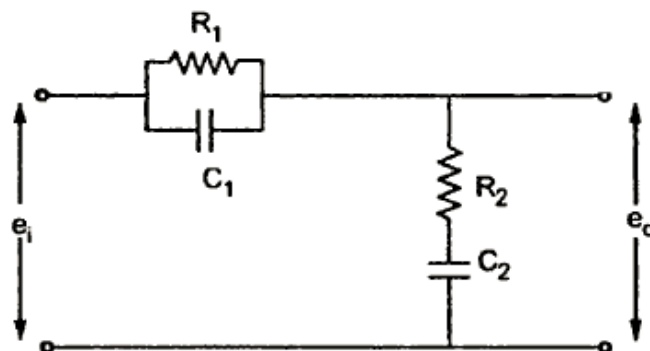
A)



(5)

B)

Find the Transfer Function  $E_o(S)/E_i(S)$  of the given circuit.

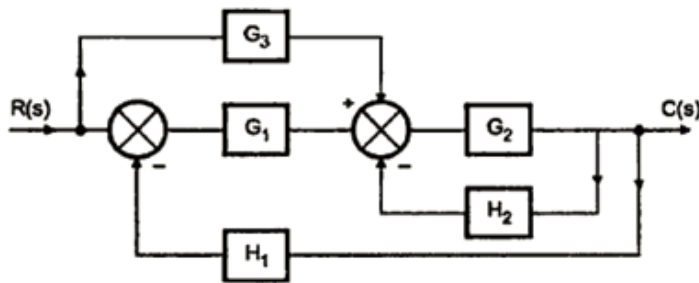


(3)

- C) Distinguish between open and closed loop control systems with respect to traffic light control system with a generalized block diagram. (2)

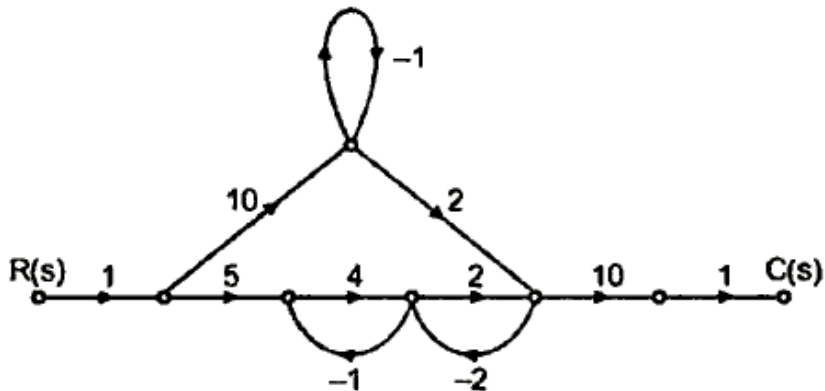
- 2) Reduce the Block Diagram given below and obtain the Transfer Function  $C(s)/R(s)$ .

A)



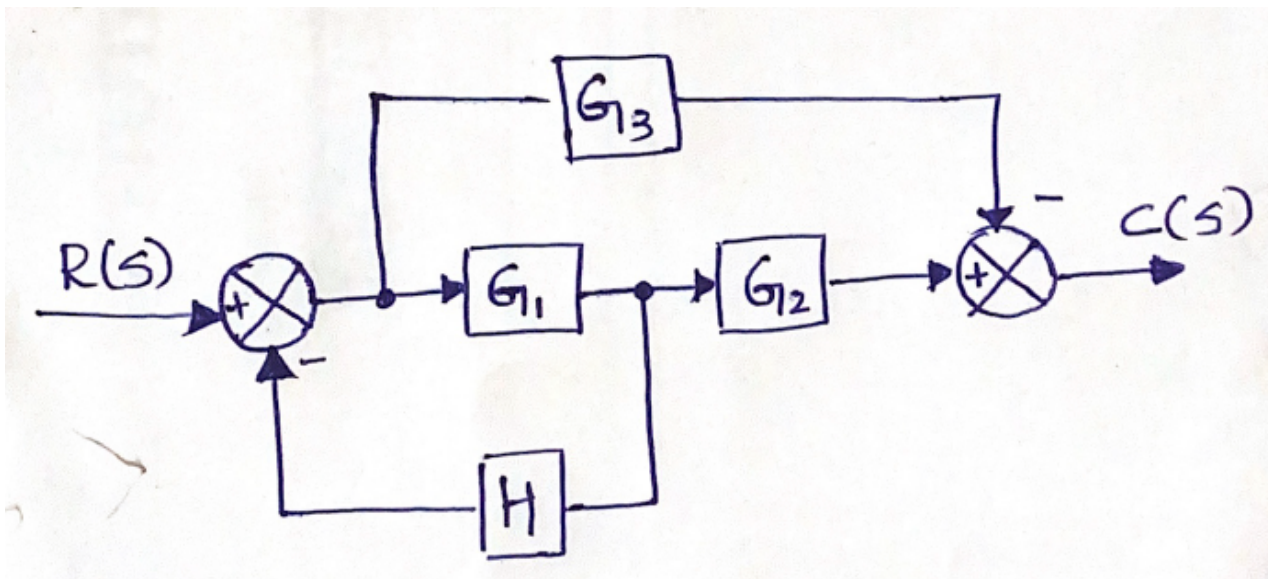
(5)

- B) For the Signal Flow Graph shown in the below figure, obtain the Transfer Function  $C(S)/R(S)$



(3)

- C) Reduce the Block Diagram to a Signal Flow Graph and obtain the Transfer Function  $C(S)/R(S)$



(2)

- 3) Compute the necessary values required to sketch **Root Locus Plot** for the Open Loop Transfer Function,

A) 
$$G(S)H(S) = \frac{K}{S(S+5)(S+10)}$$
 (5)

- B) Comment on stability for the characteristic equation  $s^6 + 3s^5 + 4s^4 + 6s^3 + 5s^2 + 3s + 2 = 0$  using (3)

Routh-Hurwitz criteria.

- C) Sketch **Root Locus Plot** in graph sheet for the **Q. No (3A)** and comment on the stability (2)
- 4) Compute the necessary values required to draw **Bode Magnitude and Phase Plot** for the Open Loop Transfer Function (5)
- A)  $G(S) = \frac{10(S + 10)}{S(S + 2)(S + 5)}$  (5)
- B) Plot the **Bode Magnitude and Phase plot** for the **Q. No. (4A)** in Semilog sheet and comment on the Stability. (3)
- C) Draw the approximate **Nyquist Plot** for the Transfer Function (2)
- $G(S) = \frac{50}{(S + 10)(S + 20)}$  (2)
- by observing the Type and Order of the system.
- 5) A closed loop servo is represented by the differential equation  $\frac{d^2 c}{dt^2} + 8 \frac{dc}{dt} = 64e$
- A) Where  $e = r - c$   
 $c$  = Displacement of the output shaft  
 $r$  = Displacement of input shaft (5)
- Find rise time, % overshoot, peak time, peak overshoot, settling time for a step input of 12 units.
- B) Find the Transfer Function from the State Space Model. (3)
- $$\dot{X} = \begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} -1 & -1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 1 \\ 0 \end{bmatrix} u$$
- $$Y = \begin{bmatrix} 0 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$$
- C) Discuss in detail with the suitable Transfer Function and Circuit Diagram, how the Lag-Lead Compensators help to improve the steady state response of the system. (2)

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