



### IV SEMESTER B.TECH. (ELECTRICAL & ELECTRONICS ENGINEERING) END SEMESTER EXAMINATIONS, MAY 2023

#### LINEAR CONTROL THEORY [ELE 2253]

REVISED CREDIT SYSTEM

Time: 3 Hours

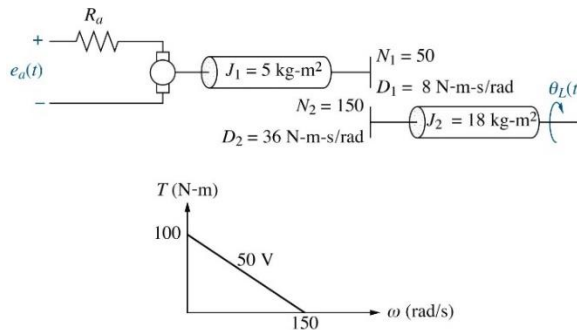
26 May 2023

Max. Marks: 50

#### Instructions to Candidates:

- ❖ Answer **ALL** the questions.
- ❖ Missing data may be suitably assumed.
- ❖ If using semi-log graph sheet, under question no. mention that

- 1A.** Derive the transfer function  $G(s) = \frac{\theta_L(s)}{E_a(s)}$  of the motor with load, torque speed characteristics is given below.



(04)

- 1B.** Analyse the stability of the system with open loop transfer function  $G(s)H(s) = \frac{K}{s(s+1)(s+3)}$  using Root locus.

(04)

- 1C.** A second order servo mechanism with unity feedback, has the open loop transfer function

$$G(s) = \frac{K}{s(s+4)}, \text{ determine the gain } K \text{ so that the steady state error shall not exceed } 0.4 \text{ deg when the input shaft is rotated at } 3\text{rpm.}$$

(02)

- 2A.** The open loop transfer function of a Floppy drive system consist of motor and load is given by  $G(s)H(s) = \frac{K}{s(s+3)(s+5)}$  i) draw the Nyquist plot ii) determine limiting value of gain K for stability iii) Mark phase margin on the plot.

(05)

- 2B.** Design a stable PID controller in the form

$$K \frac{(s + a)^2}{s}$$

using Zeigler – Nichols tuning method for the plant with transfer function

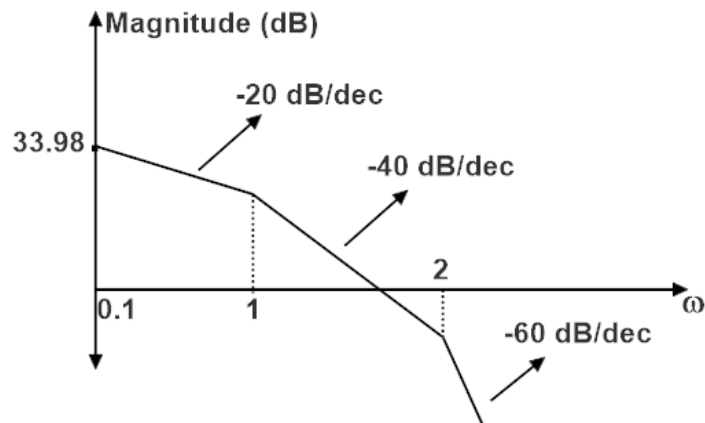
$$G(s) = \frac{4}{s^3 + 6s^2 + 8s + 4}$$

**(03)**

- 2C.** Realize a PID controller using OPAMP circuit, with a suitable example.

**(02)**

- 3A.** For the asymptotic bode magnitude plot shown in **Figure**  
Determine the gain margin (dB) of the system



**(04)**

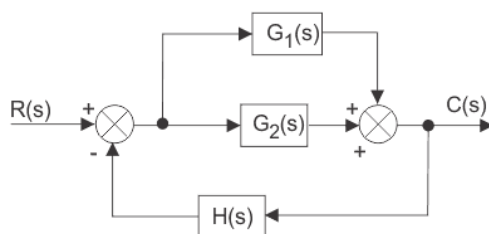
- 3B.** A position control system can be represented by the unity feedback system with plant transfer function

$$G(s)H(s) = \frac{6}{s(s + 1)(s + 2)}$$

Design a lag compensator using frequency domain methods so that the compensated system has a phase margin of  $45^\circ$ . (Use Bode plot or analytical method)

**(04)**

- 3C.** Obtain the transfer function of the block diagram given in Figure.

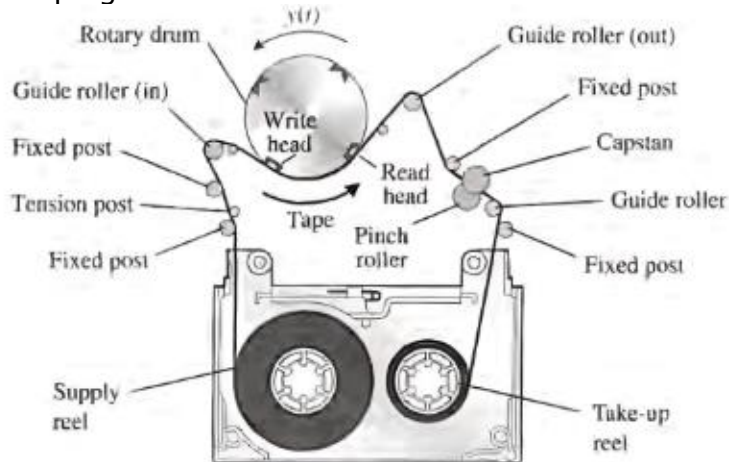


**(02)**

- 4A.** Consider the audio tape driver mechanism shown in the figure. The open loop transfer function for the negative feedback system is

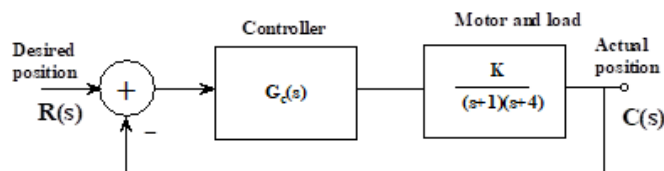
$$G(s)H(s) = \frac{K}{(s+1)(s+4)}$$

Determine the peak time and settling time for a step input. Maintain a damping ratio of 0.8 .



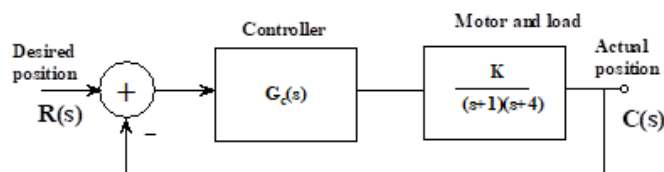
(03)

- 4B.** Consider the audio tape speed control system shown in figure. Design a PD controller that will yield a peak time of 1.047 seconds and a damping ratio 0.8 for a step input.



(04)

- 4C.** Consider the audio tape speed control system shown in figure 2. Design a PI controller that will yield a damping ratio 0.8 with zero error for a step input.



(03)

- 5A.** Obtain the state model in physical variable form of an armature voltage-controlled DC motor used for robotic application. Take armature current and angular velocity  $\frac{d\theta}{dt}$  as the state variables and output as angular velocity,  $\frac{d\theta}{dt}$ .

(04)

- 5B.** The state model of a sun tracker used for solar photovoltaic array system is represented by  $\dot{x}(t) = \begin{bmatrix} 0 & 1 & 1 \\ 0 & -2 & 2 \\ -1 & -1 & -4 \end{bmatrix} x(t) + \begin{bmatrix} 0 \\ 0 \\ 2 \end{bmatrix} r(t)$ ;  $y(t) = [1 \ 0 \ 0]x(t)$ ; Estimate the transfer function of the system and draw the state diagram.

(03)

- 5C.** The state model of a satellite control system is represented by

$$\dot{x}(t) = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -6 & -11 & -6 \end{bmatrix} x(t) + \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} r(t); \quad y = [0 \ 0 \ 1]x(t)$$

Verify complete state controllability and observability of the system.

(03)