

DEPARTMENT OF SCIENCES, IV SEMESTER M.Sc. (Physics)
END SEMESTER EXAMINATIONS, APRIL 2023
General Relativity & Cosmology [PHY 6202]
(CHOICE BASED CREDIT SYSTEM – 2020)

Time: 3 Hours

Date: 26-04-2023

MAX. MARKS: 50

Note (i) Answer ALL questions

(ii) Draw diagrams, and write equations wherever necessary. Show all steps and substitutions.

(iii) Any missing data can be suitably assumed

| | Marks | CO | BL |
|---|-------|----|----|
| 1A Show that dot product of four velocity with itself is Lorentz invariant | 2 | 1 | 2 |
| 1B Find the Killing vectors for the surface of a unit sphere | 4 | 1 | 3 |
| 1C Obtain the transformation equation for Christoffel's symbols of second kind | 4 | 1 | 2 |
| 2A Obtain Bianchi identity | 5 | 1 | 2 |
| 2B State and prove quotient law of tensors | 3 | 1 | 2 |
| 2C Describe Hubble's law with necessary equations | 2 | 3 | 2 |
| 3A An object in motion on a plane has the velocity vector field given by $\mathbf{v}^i = (x^2, y^2)$ in Cartesian co-ordinates. Find the covariant derivative of the vector field in polar co-ordinates (Given: $\Gamma_{22}^1 = -r$, $\Gamma_{12}^2 = \Gamma_{21}^2 = 1/r$) | 5 | 1 | 3 |
| 3B Obtain an expression for deviation in the path of light due to gravitational field | 3 | 2 | 2 |
| 3C Describe cosmological principle and Weyl postulate | 2 | 3 | 2 |
| 4A Obtain all non-vanishing Christoffel symbols of second kind for Schwarzschild metric outside a spherically symmetric, static gravitational field. Show all steps and substitutions. | 4 | 2 | 3 |
| 4B Using the Christoffel symbols obtained in previous question, obtain R_{00}, R_{11} and R_{22} | 3 | 2 | 3 |
| 4C Using the components R_{00}, R_{11} and R_{22} obtained in the previous question, find Schwarzschild solution for Einstein's field equation outside a spherically symmetric, static gravitational field | 3 | 2 | 3 |
| 5A Describe (i) static limit and ergosphere of Kerr blackhole (ii) Kruskal-Szekeres coordinates | 4 | 3 | 2 |
| 5B Describe Newtonian cosmology with necessary equations | 3 | 3 | 2 |
| 5C Describe Einstein's model of the universe with necessary equations | 3 | 3 | 2 |
